Heliophysics Shocks



Merav Opher, George Mason University mopher@gmu.edu



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Outline

- 1. Why Shocks Happen: Non Linear Steepening
- 2. MHD jump conditions: Rankine-Hugoniot jump conditions
- 3. Definition and Classification of Shocks/ Discontinuities
- 4. Contact and Tangential Discontinuities/ Examples
- 5. Shocks
- 6. Observation of Shocks: Termination Shock, CME Shocks, Planetary Shocks
- 7. Open questions: research being done

1. Why Shocks Happen: Non Linear Steepening

- When gradients of pressure, density and temperature become large than dissipative processes (viscosity, thermal conduction) "steepening" or "wave-steepening" occur.
- The nonlinear convective terms balance the broadening effects of dissipation



Example: propagation of sounds wave in an adiabatic medium

Propagation of a sound wave is
 For an adiabatic equation of state:

$$v_s^2 = \frac{dP}{d\rho}$$

 $P/\rho^{\gamma} = constant$



- A propagating wave solution of the ideal fluid equations leads to *infinite gradients* in a finite *time*. There is no solution for the ideal MHD equations
- The breakdown in ideal equations occurs in a very *thin* region and the fluid equations are valid everywhere else. On in this very thin region is difficult to describe the plasma in details.
- The simple picture: is a discontinuity dividing two roughly uniform fluids



Region 2 (downstream) Region 1 (upstream)

The transition must be such as to conserve MASS, Magnetic Flux and Energy

2. Jump Conditions which are independent of the physics of the shock itself: Rankine-Hugoniot Relations

(a) Conservation of Mass: $\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = \mathbf{0}$ through regions 1 and 2 gives: $\rho_1 \mathbf{u}_1 \cdot \mathbf{n} = \rho_2 \mathbf{u}_2 \cdot \mathbf{n}$

that can be written as $\{\rho \mathbf{u} \cdot \mathbf{n}\} = 0$ where the symbol $\{\}$

represent differences between the two sides of the discontinuity.

(b) Conservation of Momentum

$$\begin{aligned} \frac{\partial(\rho \mathbf{u})}{\partial t} + \nabla \cdot \left[\rho \mathbf{u} \mathbf{u} + \left(p + \frac{B^2}{2\mu_0}\right) \mathbf{I} - \frac{\mathbf{B}\mathbf{B}}{\mu_0}\right] &= 0 \end{aligned}$$
gives
$$\left\{\rho \mathbf{u}(\mathbf{u} \cdot \mathbf{n}) + \left(\mathbf{p} + \frac{\mathbf{B}^2}{2\mu_0}\mathbf{n} - \frac{\mathbf{B}}{\mu_0}(\mathbf{B} \cdot \mathbf{n})\right)\right\} = 0 \end{aligned}$$

(C) Conservation of energy $\frac{\partial}{\partial t} \left(\frac{1}{2} \rho U^2 \frac{P}{\gamma - 1} + \frac{B^2}{2\mu_0} + \nabla \cdot (\frac{1}{2} \rho \mathbf{U}^2 \mathbf{u} + \frac{\gamma \mathbf{P}}{\gamma - 1} \mathbf{u} + \frac{1}{\mu_0} \mathbf{E} \times \mathbf{B} \right) = 0$ gives $\left\{ \left(\frac{1}{2} \rho U^2 + \frac{\gamma P}{\gamma - 1} \right) (\mathbf{u} \cdot \mathbf{n}) + \frac{1}{\mu_0} (\mathbf{E} \times \mathbf{B}) \cdot \mathbf{n} \right\} = 0$ (d) The Magnetic flux conservation

 $\nabla \cdot \mathbf{B} = \mathbf{0}$

gives $\{\mathbf{B} \cdot \mathbf{n}\} = \mathbf{0}$ and $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$ gives $\{\mathbf{E} \times \mathbf{n}\} = \mathbf{0}$

Let us consider the normal *n* and tangential *t* component relative to the discontinuity surface so the JUMP conditions can be written as:

The equations (*) are called the Rankine-Hugoniot jump conditions

3. Definition and Classification of Shocks/Discontinuities

	$U_n = 0$	$U_n \neq 0$
$\{\rho\} = 0$	trivial	rotational discontinuity
$\{\rho\} \neq 0$	contact discont.	shock wave

4.Contact Discontinuity

- Happens where there is no flow across the discontinuity, i.e, U_n=0 and {ρ}≠0
- E.g. classic contact discontinuity



 (a) If Bn≠0 contact discontinuity -> only the density changes across the discontinuity (rarely observed In plasmas)

Tangential Discontinuity

(b) When
$$B_n=0 => \{U_T\} \neq 0$$

 $\{B_T\} \neq 0$
and $\{p+B^2/2\mu_0\}=0$

The fluid velocity and magnetic field are parallel to the surface of the discontinuity but change in magnitude and direction. The sum of thermal and magnetic pressure is constant also.

Heliopause: Tangential Discontinuity

INTO THE UNKNOWN

The interstellar magnetic field is distorting the heliosphere







Planetary Magnetosphere: Tangential Discontinuity



If there is no much reconnection so Un ~ 0; $B_n \sim 0$ so solar wind plasma and magnetic field do not penetrate into the magnetosphere

Rotational Discontinuity: Un \neq 0 and { ρ }=0

From jump conditions $(a) \Rightarrow \{U_n\} = 0$ and $\{p + \mathcal{B}_{\underline{r}}^2\} = 0$ $V_1 \cdot \hat{n} = V_2 \cdot \hat{n} = V_0$ $P_1 = P^2$..some math...we get that if $U_n^2 = \frac{\mathcal{B}_n^2}{\mathcal{A}_0 \mathcal{P}_m}$

B_t remain *constant* in magnitude but rotates in the plane of the discontinuity.

Example: if the *reconnection rate* between the solar wind Magnetic field and the planetary magnetic field is substantial; then The plasma can penetrate significantly into the magnetosphere: The magnetopause becomes a rotational discontinuity

5. SHOCK WAVES

Shock waves are characterized by a fluid flows across the discontinuity $U_n \neq 0$ and a non zero jump discontinuity $\{\rho\} \neq 0$

Frames of reference for MHD shocks:

(I) normal incident frame (coordinate system moving along the shock front with speed U_t)

(II) de Hoffman-Teller frame (the plasma is parallel to the magnetic field on both sides and the reference frames moves parallel to the shock front with the de Hoffman-Teller speed)



Strength of the Shock

• Jump equations: 12 unknowns (4 upstream parameters are specified: ρ , v_S, B_t, B_n) so we have 7 equations for 8 unknowns -> we need to specify one more quantity $\delta = \frac{\rho_2}{\rho_1}$

Alfren Mach number Un Mopm Br Other quantities: Sonic Mach number tand = BE ange & Between the B & shock norma

Shock Adiabatic Equation

• You can combine using the shock equations to a one single equation that gives the shock propagating speed U_{n1} as a function of shock strength δ and upstream parameters



Type of Shocks

- Weak Shock Limit δ=1 (solution of the shock equation are slow, intermediate and fast shocks) (slow correspond to slow MHD wave; fast to fast MHD wave and intermediate to transverse Alfven wave)
- Strong Shock Limit: $\delta \rightarrow \delta_m$
- Parallel Shock: θ=0°
- Perpendicular Shocks: $\theta = 90^{\circ}$
- Quasi-perpendicular shocks θ >45°

Thickness of Shocks

- The thickness of the shocks and the detailed substructure within the shock depends on the angle θ_{BN} , M_{A1} , M_{A2}
- The transition region of a quasi-perpendicular shock is usually thin and well defined
- The transition region of a quasi-parallel shock is usually more complex and often appears thick



Broadband electric field noise: Plasma wave turbulence excited by unstable particle distribution in the shock Jupiter's bow shock

Narrow band at 6kHz: Electron plasma oscillations Excited by a beam of electrons that escapes into the region upstream the shock

6. Observations of MHD Shocks



Earth Bow Shock (at a distance $15.4R_E$ upstream from Earth) This example $\theta_1=76^\circ$ (between B and n) $U_1=294$ km/s > $v_A=37.8$ km/s



Voyager 2 crossing the Termination Shock in August 2007

Termination Shock: Perpendicular Shock



Voyager 2 crossed the Termination Shock in August 2007- (in-situ measurements of a shock)

J.Richardson et al.



Voyager 1 in the north Voyager 2 in the south





Crossing of TS by V2: closer to the Sun than V1



Welcome to the Voyager Web Site

Voyager 2 Proves Solar System Is Squashed

San Francisco, CA. - NASA's Voyager 2 spacecraft has followed its twin Voyager 1 into the solar system's final frontier, a vast region at the edge of our solar system where the solar wind runs up against the thin gas between the stars.

However, Voyager 2 took a different path, entering this region, called the heliosheath on August 30, 2007. Because Voyager 2 crossed the heliosheath boundary, called the solar wind

Voyager 2 Latest Data

> Cosmic Ray Subsystem

Low-energy Charged Particles

Plasma Science

Browse Data

Cosmic Ray Subsystem

Plasma Science

Plasma Waves

Low-energy

Charged Particles

Magnetometer

Vovager

Other Science

Data Calibration &

Validation

lanetary Voyage

termination shock, about 10 billion miles away from Voyager 1 and almost a billion miles closer to the sun, it confirmed that our solar system is " squashed" or " dented"- that the bubble carved into interstellar space by the solar wind is not perfectly round. Where Voyager 2 made its crossing, the bubble is pushed in closer to the sun by the local interstellar magnetic field.

"Voyager 2 continues its journey of discovery, crossing the termination shock multiple times as it entered the outermost layer of the glant heliospheric bubble surrounding the Sun and joined Voyager 1 in the last leg of the race to interstellar space." said Voyager Project Scientist Dr. Edward Stone of the California Institute of Technology, Pasadena, Calif.





From the Archives

iranda, moo

Uranus More archive image



Earth's Greeting to the





Shocks Driven by Coronal Mass Ejections







Propagating Shocks

Shock geometry can vary if near
 The nose or flanks



Universal Characteristics of Shocks





Synthetic Coronagraph Images of the CME: LASCO C2 and HI2





ReverseForwardShockShock

Lugaz, Manchester and Gombosi ApJ 2005

Radio Type II emission associated with CME shocks



Measuring Shocks



Shock brightness to density (ρ) Shock strength, $\gamma=1+\rho/\rho0$ SPM model for the density of the back ground corona ($\rho0$).

Vourlidas & Ontiveros 2008



Development of Coronal Shocks Seen in the UV

John Raymond

Smooth, Faint arcs are often seen in White Light. convincing identification as shocks requires MHD Simulation matching profile (Manchester et al., Vourlidas et al.)



UVCS Shock Observations Analyzed so far

Date	Reference	Н	V	n ₀ L	og T _O	Х
06/11/98	Raymond et al.	1.75	1200	1x10 ⁶	8.7	1.8
06/27/99	Raouafi et al.	2.55	1200		<8.2	1.0
03/03/00	Mancuso et al.	1.70	1100	1x10 ⁷	8.2	1.8
06/28/00	Ciaravella et al.	2.32	1400	2x10 ⁶	8.1	
07/23/02	Mancuso&Avetta	1.63	1700	5x10 ⁶	8.0	2.2

Modest heights, Modest compression, High T_O

5 other shocks not yet fully analyzed (Ciaravella et. al. 2006)

Shocks Geometry: Magnetic Connectivity



CMEs and Composition of SEPs



OPEN QUESTIONS/Research being done

8. Open Questions

How do magnetic effects affect shock evolution? (Loesch et al. 2010; Liu et al. 2009)



Which type of flows do we get in CME sheaths? *(Evans et al. 2010)*

How does reconnection affect shock structures in the lower corona?

Formation of Shocks and Solar Energetic Particles

Background Solar Wind with Alfven Waves (Evans, Rona, Opher, Gombosi, 2010; Evans et al. 2008; 2009)

What is the Alfvén Speed Profile in the Lower



• Ten Models (Solar Minimum)

Evans et al. ApJ (2008)

- 6 Global MHD: Manchester et al. 2004; Cohen et al. 2007; Roussev et al. 2004; Riley 2006; Lionello et al. 2001; Usmanov & Goldstein 2006
- 2 Local Studies: Cranmer et al. 2007; Verdini & Velli 2007
- 2 Semi-analytic: Guhathakurta et al. 2006; Mann et al. 2003
- Different Strategies to Accelerate Solar Wind
 - Empirical Heating Functions
 - Non-uniform Polytropic Index
 - Inclusion of Alfvén Waves



M1 Manchester et al. M2 Cohen et al. M3 Roussev et al. M4 Riley M5 Lionello et al.

M6 Guhathakurta et al. M7 Mann et al. M8 Cranmer et al. M9 Usmanov & Goldstein M10 Verdini & Velli

Initial Steady State in the Corona

•Solar surface is colored with the radial magnetic field.

•Field lines are colored with the velocity.

•Flux rope is shown with white field lines.



Surface Alfven Waves

 Dissipate in regions with strong gradients in B, ρ (boundary of open/closed field lines)

$$L_{SW} = L_0 \left(\frac{r_0}{r}\right)^{5/2} \left(\frac{v_A}{v_{A0}}\right)^2 \left(1 + M_A\right)$$



Evans et al. ApJ 2008, 2009



is comparable to heating due to variable polytropic index



Surface Alfven Wave-Driven Wind



Evans et al. 2010

Future plans: Incorporate into a frequency-dependent model

Two Hours After Eruption in the Solar Corona



65 Hours After Eruption in the Inner Heliosphere





Manchester et al. 2004



Flows In CME-Sheath

- Background solar wind:
 - 3D MHD Code BATS-R-US (U. of Mic
 - Cohen et al. 2007 Polytropic Model
 - CR1922 (May 1997)
- CME Initiation
 - Modified Titov-Demoulin FR
 - Torus line current only
 - 3 Orientations of B_{ejecta}
 - 2 along neutral line; 1 across
 - Same initial free energy





Evans, Opher & Gombosi ApJ 2010

BCOR

CME-Pause

• Viewpoint: looking back towards Sun



→We expect the CME-sheath flows to deflect around the pause differently

Flow deflection angle along a velocity streamline

$$\theta_F = \tan^{-1} (V_N / V_T)$$
 (RTN coordinates)

	$\theta_{\rm F}$ at CME-shock	θ_{F} at CME-pause
Case A	-86°	-66°
Case B	-82°	-47°
Case C	-77°	35°

θ_r is different by 15-78° at the CME-pause

2. Flow deflection angle evolution

Rotation slows to <2°/ R_{\odot} when R_{shock} =6 R_{\odot} (for cases A & C)

Flows in the CME sheath are sensitive to B_{ejecta} , and can be used as a diagnostic for its orientation

Evolution of a Flux Rope in the Lower Corona



Liu et al. ApJ (2008)

Bright Front and Dark Void



CME: near the nose: Quasi-Parallel Shocks



Liu et al. ApJ 2008





Evolution of Flows, Field Lines in CME sheath



Magnetic Field Lines Rotation

Liu et al. A&A 2010



Behavior of the Magnetic Field in the Sheath



Magnetic Effects at the Edge of the Solar System

AMNH, "Journey to the Stars", 2009

V1 is beyond 100 AU at 34.1° (latitude) and 173° (longitude) (HGI coord).

V2 is beyond 90 AU at -26.2° (latitude) and 216° (longitude)



Paradigm Shift

Importance of tails



Shock is colder than expected



Particle acceleration



No evidence of the source of anomalous cosmic rays

Magnetic holes

Bulaga et al. 2007

Heliospheric Asymmetries

Position of the Termination Shock at V1 and V2
Particle Data: Streaming lons from the shock (TSPs)

-Radio Data: 2-3kHz

-Flows in the Heliosheath at V2

Opher, et al *ApJL*Opher et al. *Science*Opher *et al NaturePrested et al.JGR* *Science* 11 May 2007: Vol. 316. no. 5826, p. 793 DOI: 10.1126/science.316.5826.793a

THIS WEEK IN SCIENCE



The two Voyag a series of radi beyond the hel extent of the s bubble that en These radio so from the inters interplanetary heliopause, bu required assun direction of the field in this rec

the local field introduces asymmetries that affect the loemission and the streaming direction of ions from the t the solar wind. Others have assumed that the magnetic the calactic plane, as it is on large scales in the Milley M

Importance of Magnetic Field







Subsonic flows sensitive to the boundary ahead

Opher et al. Nature (2009)

Model with ionized+neutral H (5 fluid model)

The flow angle θ =tan⁻¹(V_N/V_T) in the Heliosheath from day 277 of 2007 to day 245 of 2009



The period between 2007.95 and 2008.62 (blue points) seems to be dominated by transients



Interstellar magnetic field

More Open Questions

Tilted Heliospheric Current Sheet

Role of reconnection; turbulence, solar cycles

(Opher, Drake, Swisdak 2010)

Acceleration of particles

Role of tails (pickup ions)

Kinetic neutrals-MHD

(Alouani, Opher, Izmodenov 2010)



Krimigis et al.

Dissipation of the sectored heliospheric magnetic field: a mechanism for the generation of ACRS Drake, Opher, Swis

Drake, Opher, Swisdak, ApJ 2009; Lazarian & Opher ApJ 2009



example of MHD-coupled with PIC code

Learning from the heliosphere about astrospheres and shocks





http://physics.gmu.edu/~mopher mopher@gmu.edu



