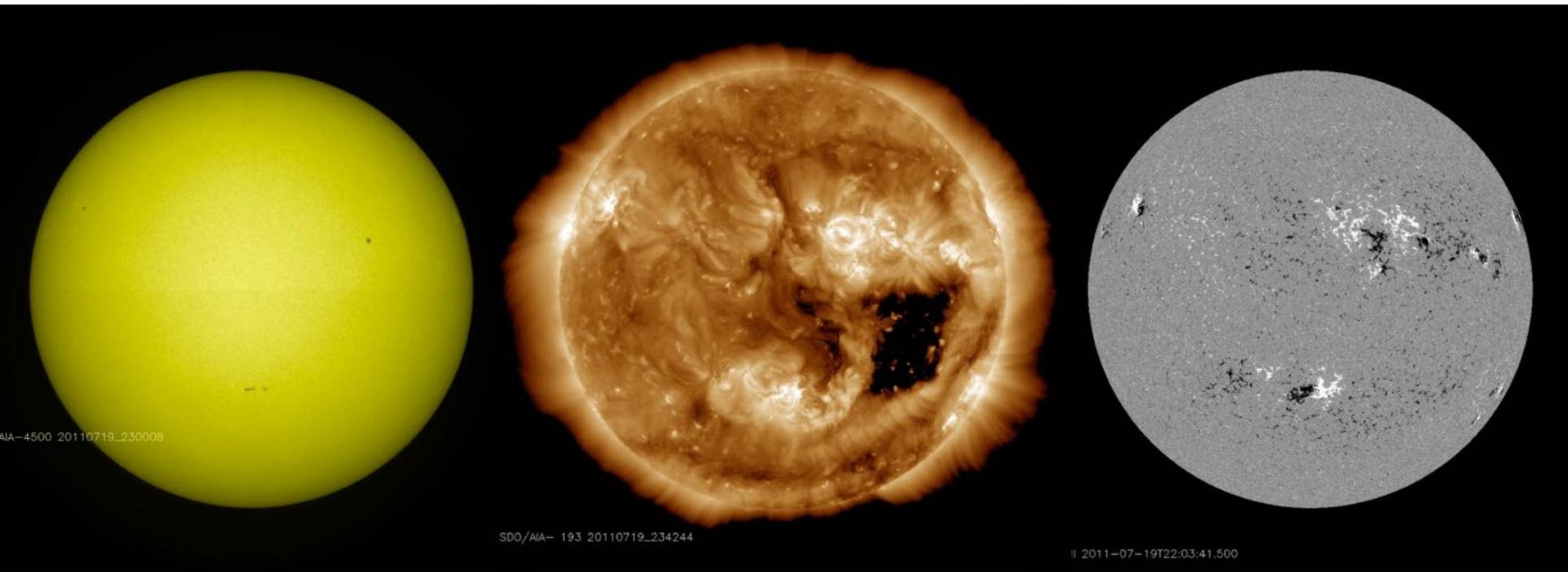


Q: Why does the Sun have a Corona? A Wind?

Dana Longcope

Montana State University

With liberal “borrowing” from Hansteen,
Schrijver, Gosling, Jokipii, Giacalone, Lean, ...

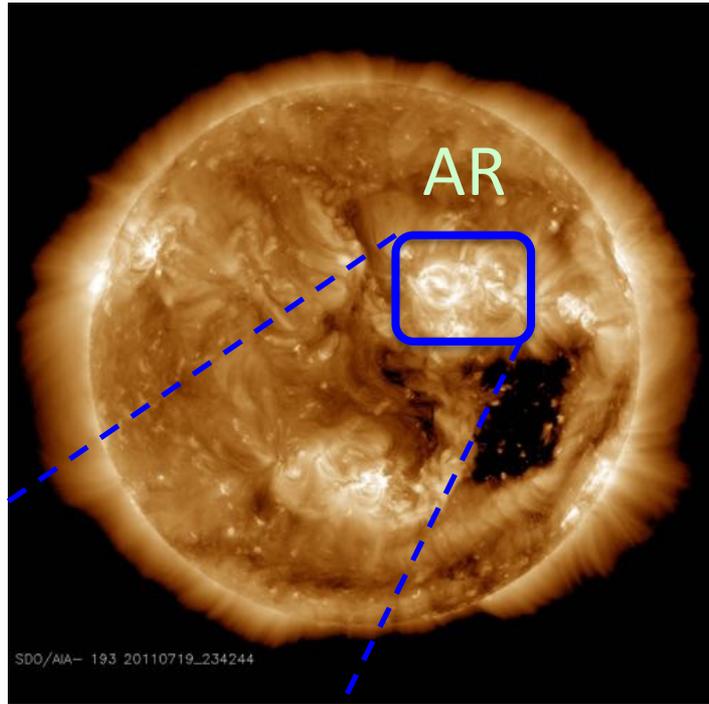


Coronal (EUV) imaging – the basics:

- what you see is all the same T (1.5×10^6 K)
- bright = dense plasma – n_e^2
- heating **can*** make plasma dense & thus bright
- heating is evidently magnetic

* if magnetic field lines are closed – magnetic bottle

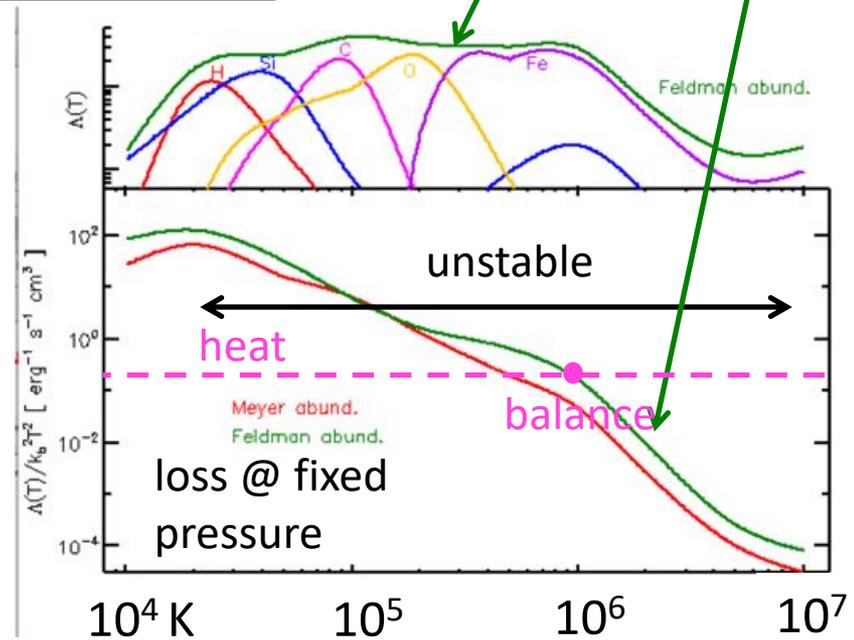
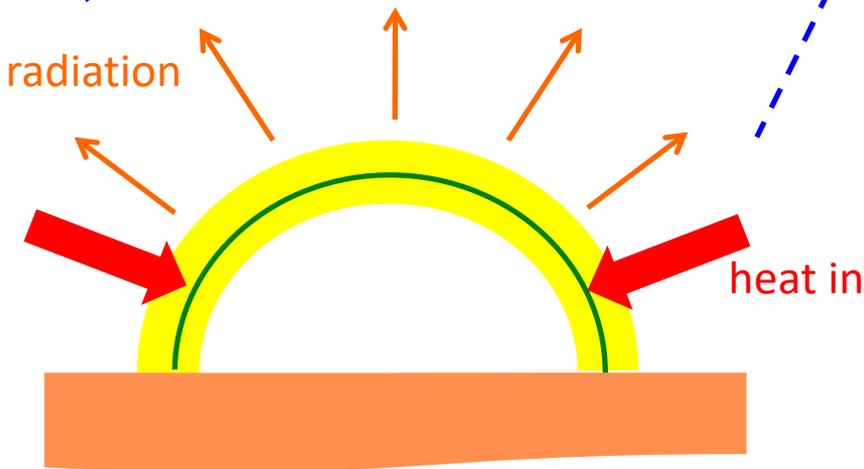
B large enough to restrict plasma motion: only along field lines



0d picture:
balance between heat & radiation
@ fixed pressure

Radiative losses per volume:
Vol. I: Eq. (8.6)

$$n_e n_H \Lambda(T) = p^2 \frac{\Lambda(T)}{k_b^2 T^2}$$

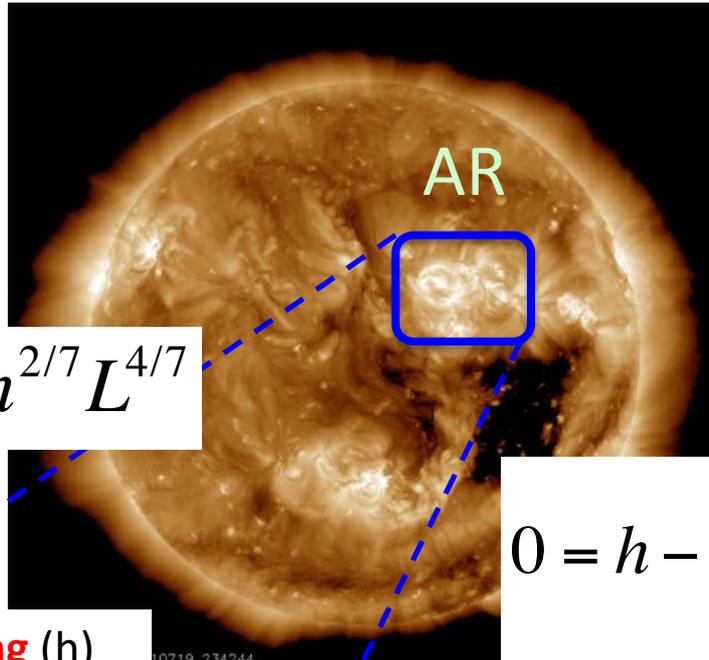


balance:
(RTV)

$$p \sim h^{6/7} L^{5/7}$$

$$T_{\max} \sim (pL)^{1/3} \sim h^{2/7} L^{4/7}$$

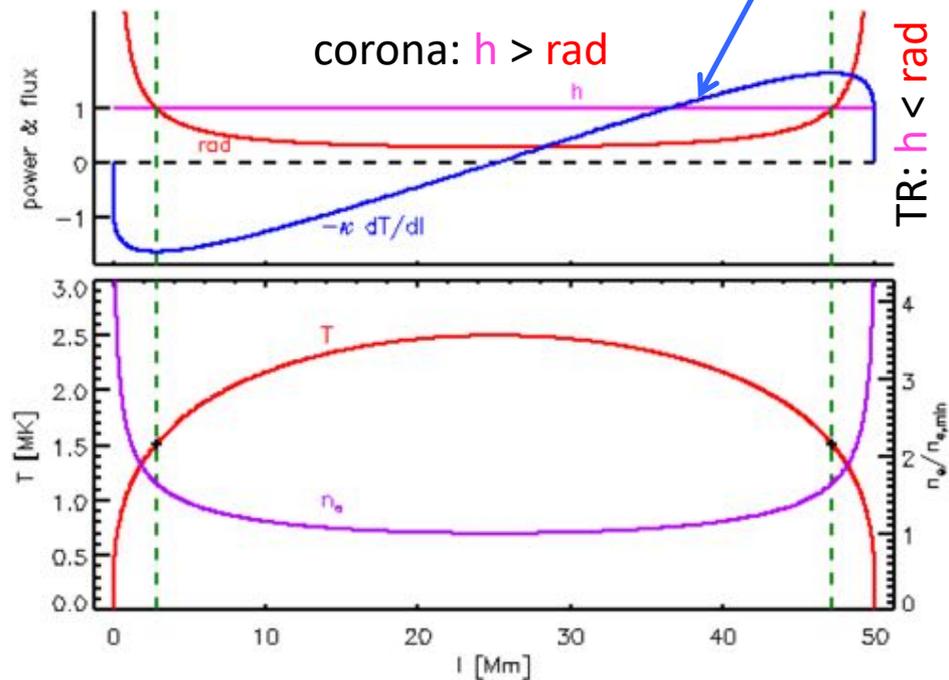
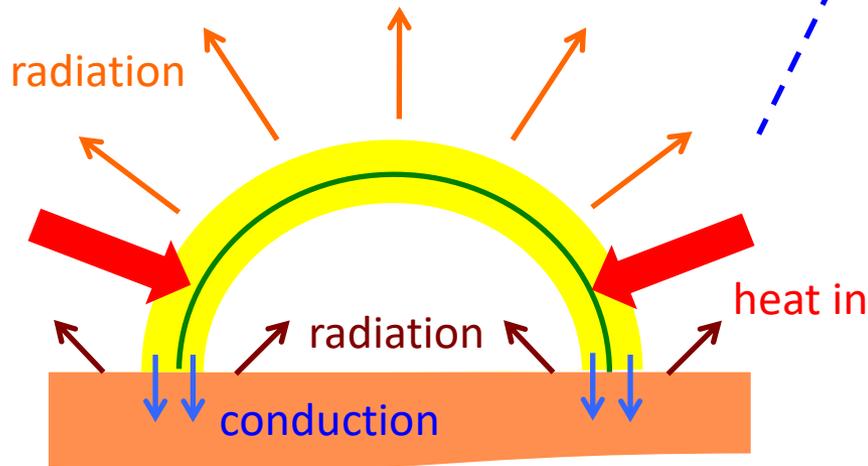
$$I \sim n_e^2 \sim h^{8/7} L^{2/7}$$



Need 1d:
include thermal
conduction to
move heat to
chromosphere

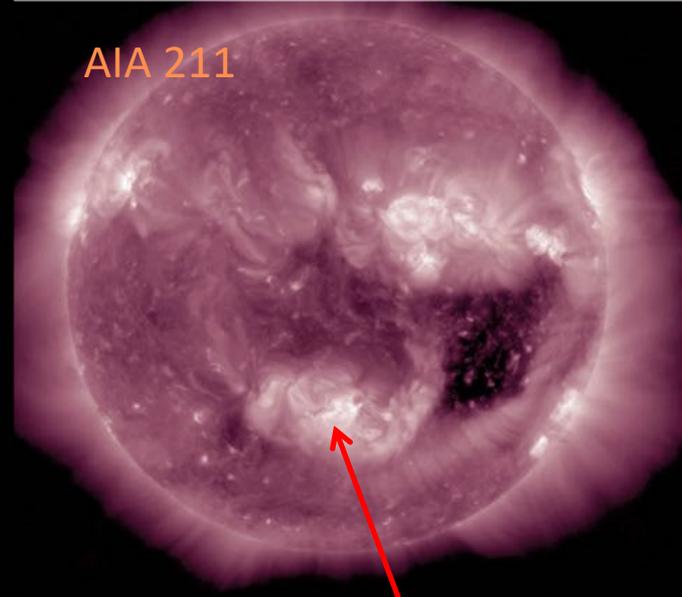
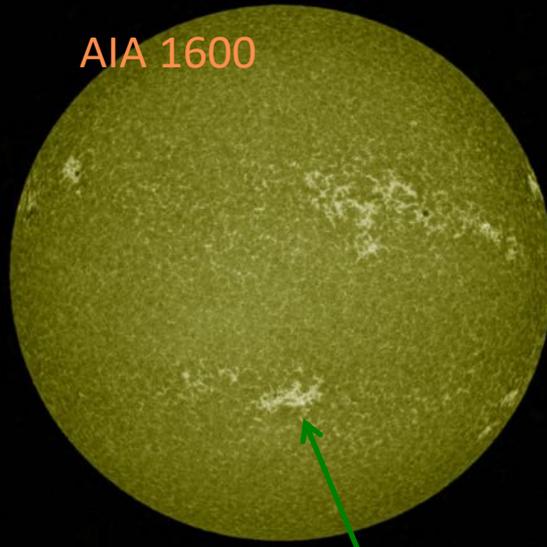
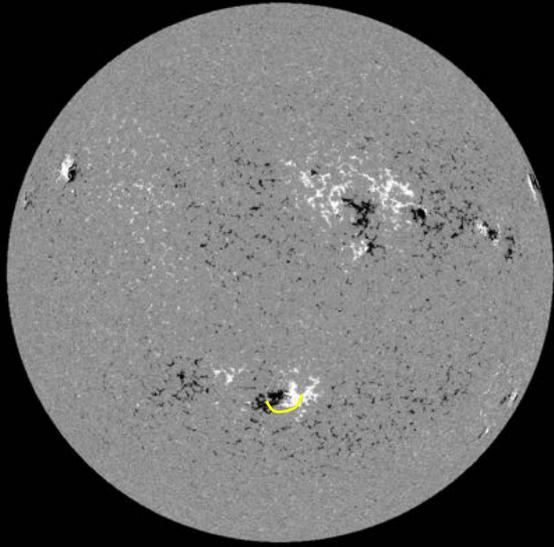
$$0 = h - p^2 \frac{\Lambda(T)}{k_B^2 T^2} + \frac{\partial}{\partial \ell} \left(\kappa \frac{\partial T}{\partial \ell} \right)$$

more heating (h)
→ little hotter
much brighter

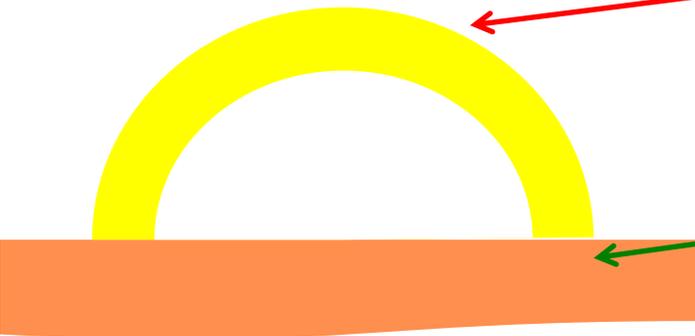
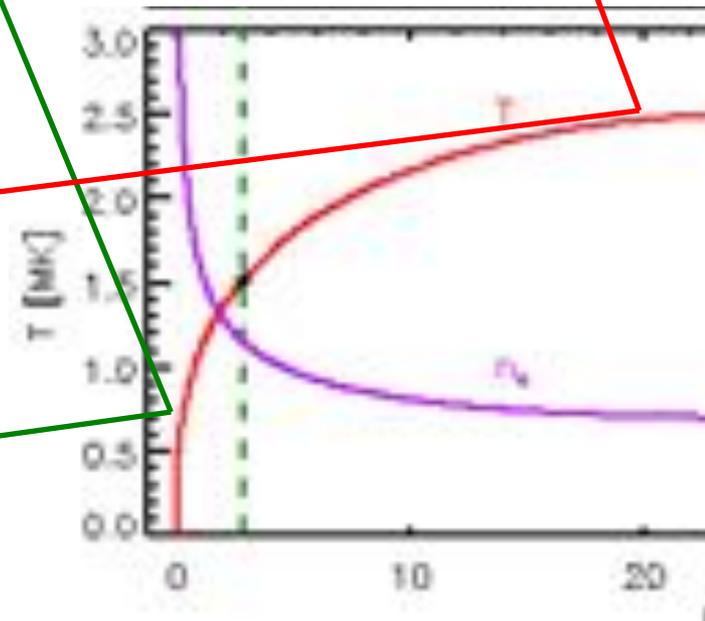


TR: $h < \text{rad}$

corona: $h > \text{rad}$

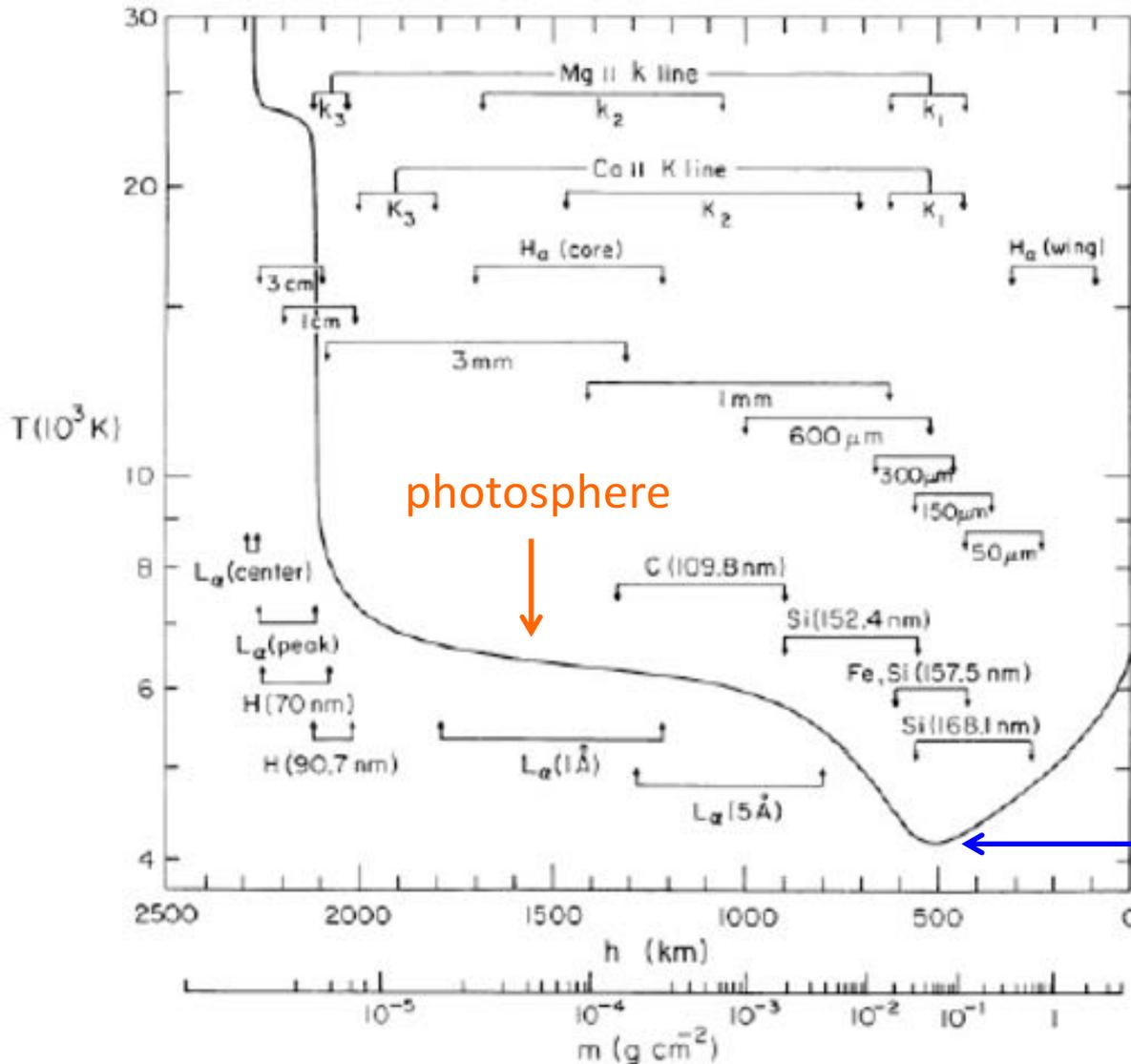


MI 2011-07-19T22:03:41.500



Below the TR – hairy details

Vernazza *et al.* 1981

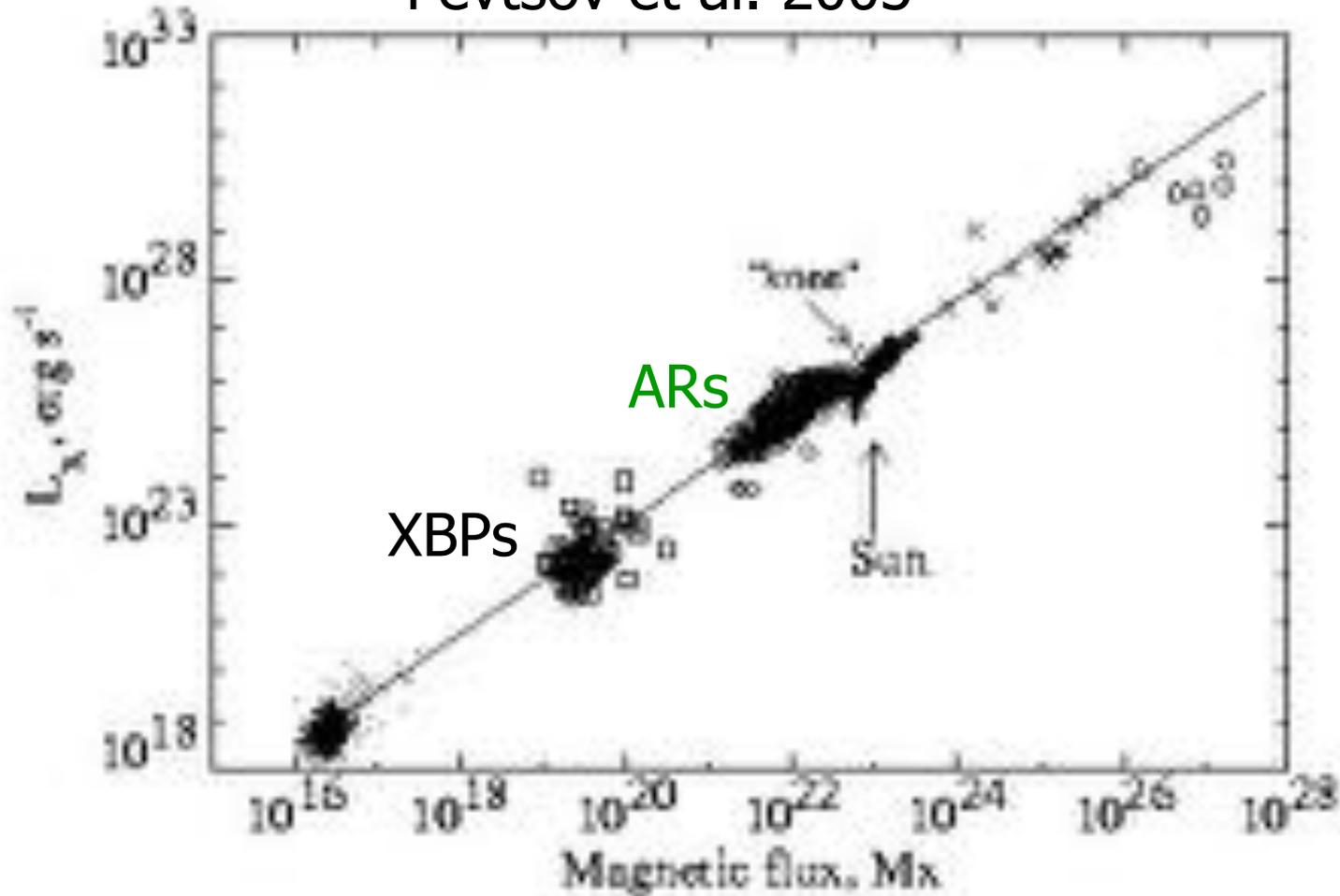


- Radiation: not optically thin
- Ionization level varies with T

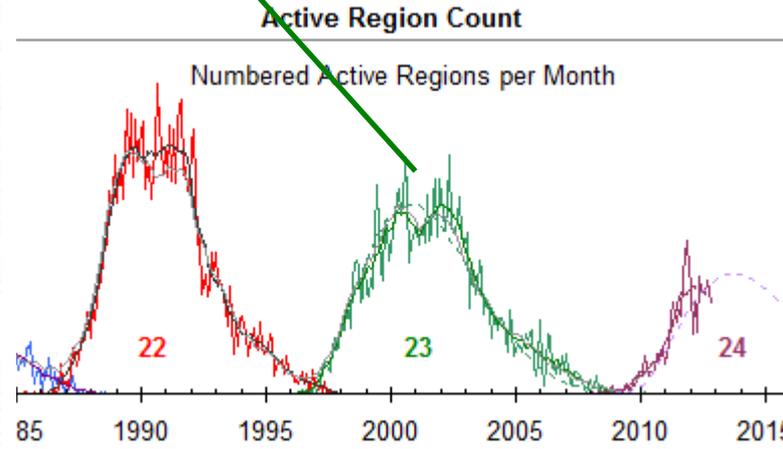
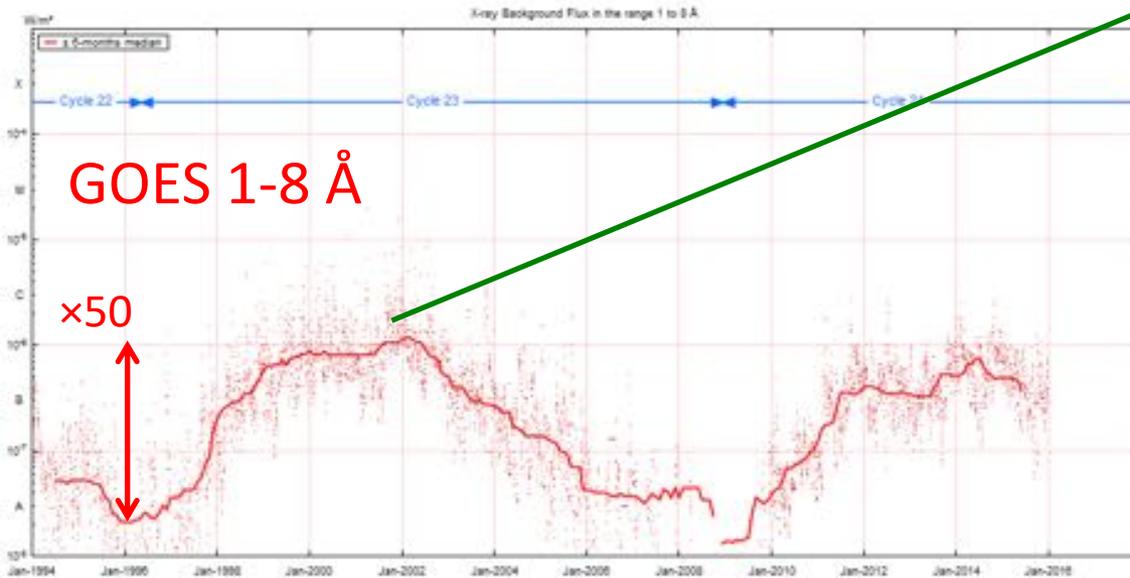
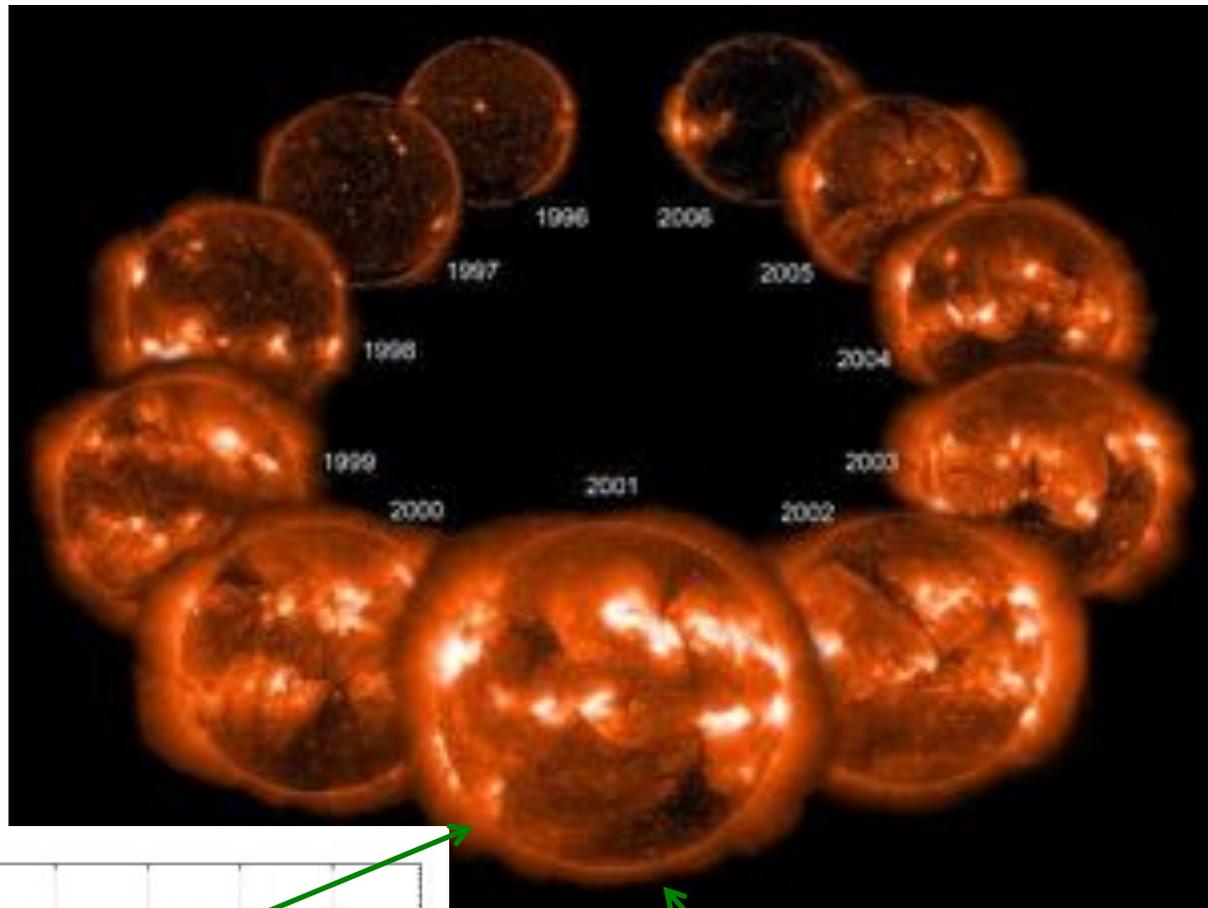
temperature minimum

Heating is Magnetic

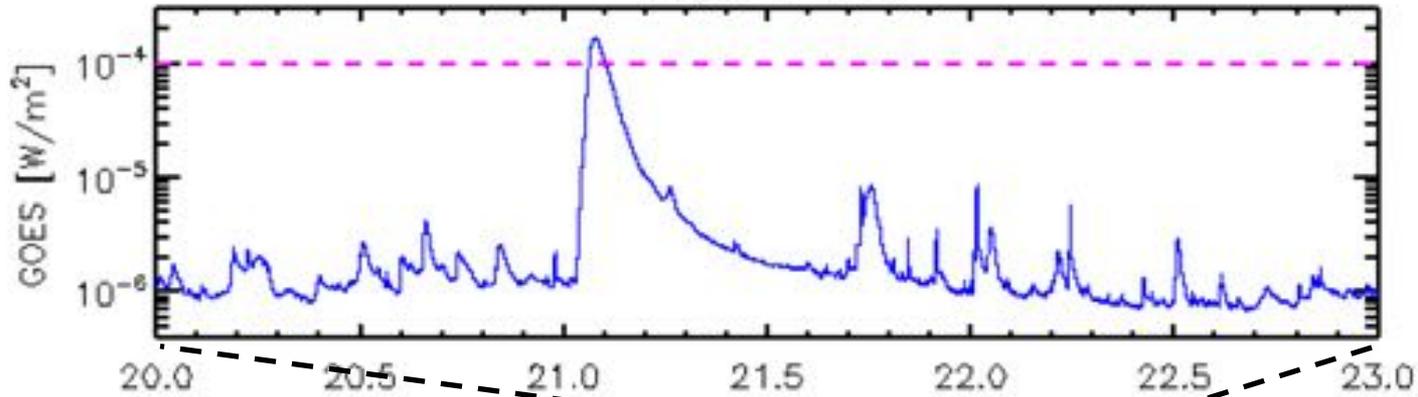
Pevtsov et al. 2003



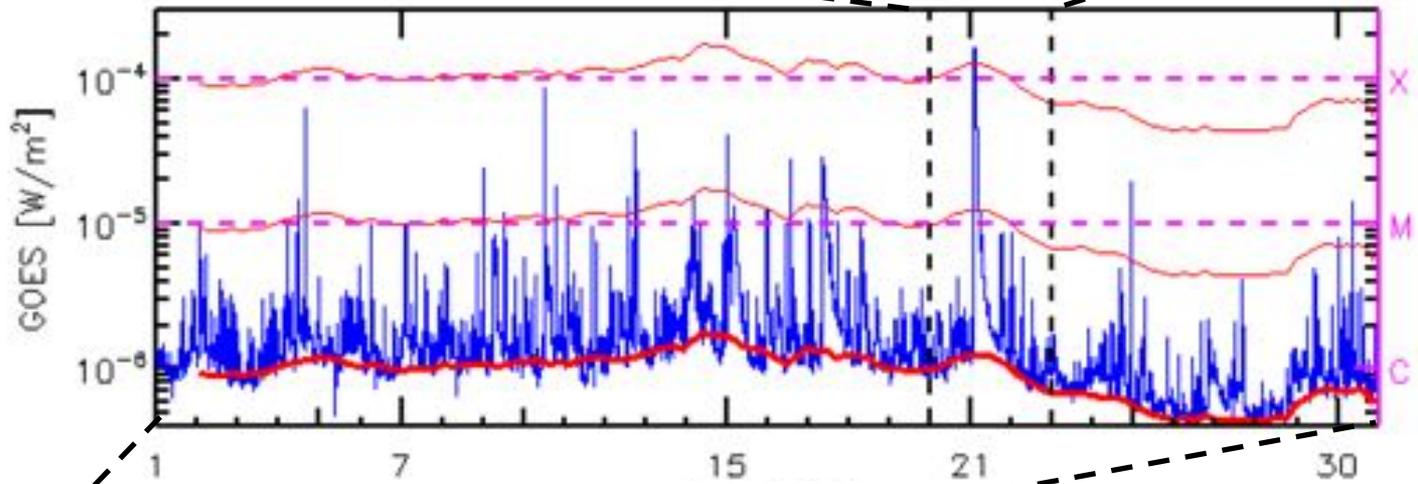
Field
varies –
corona
varies



GOES 1-8 Å

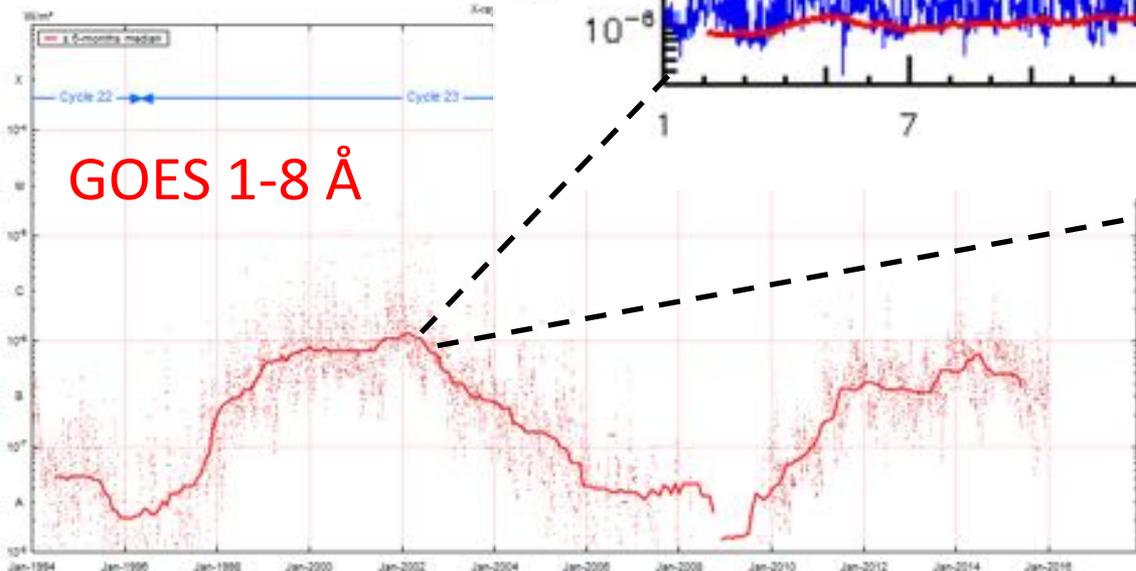


X-rays:
highly
variable –
flares



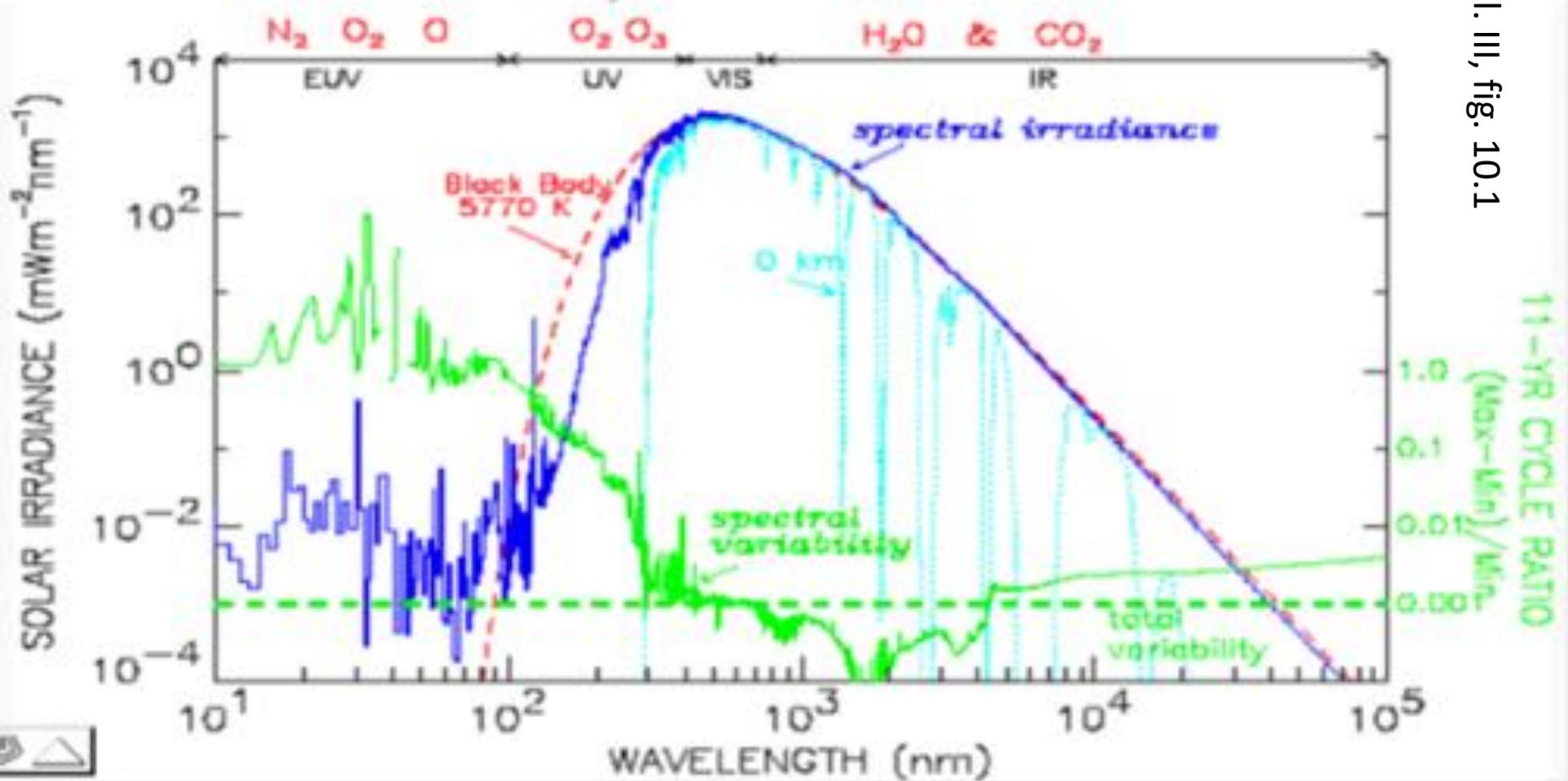
April 2002

GOES 1-8 Å

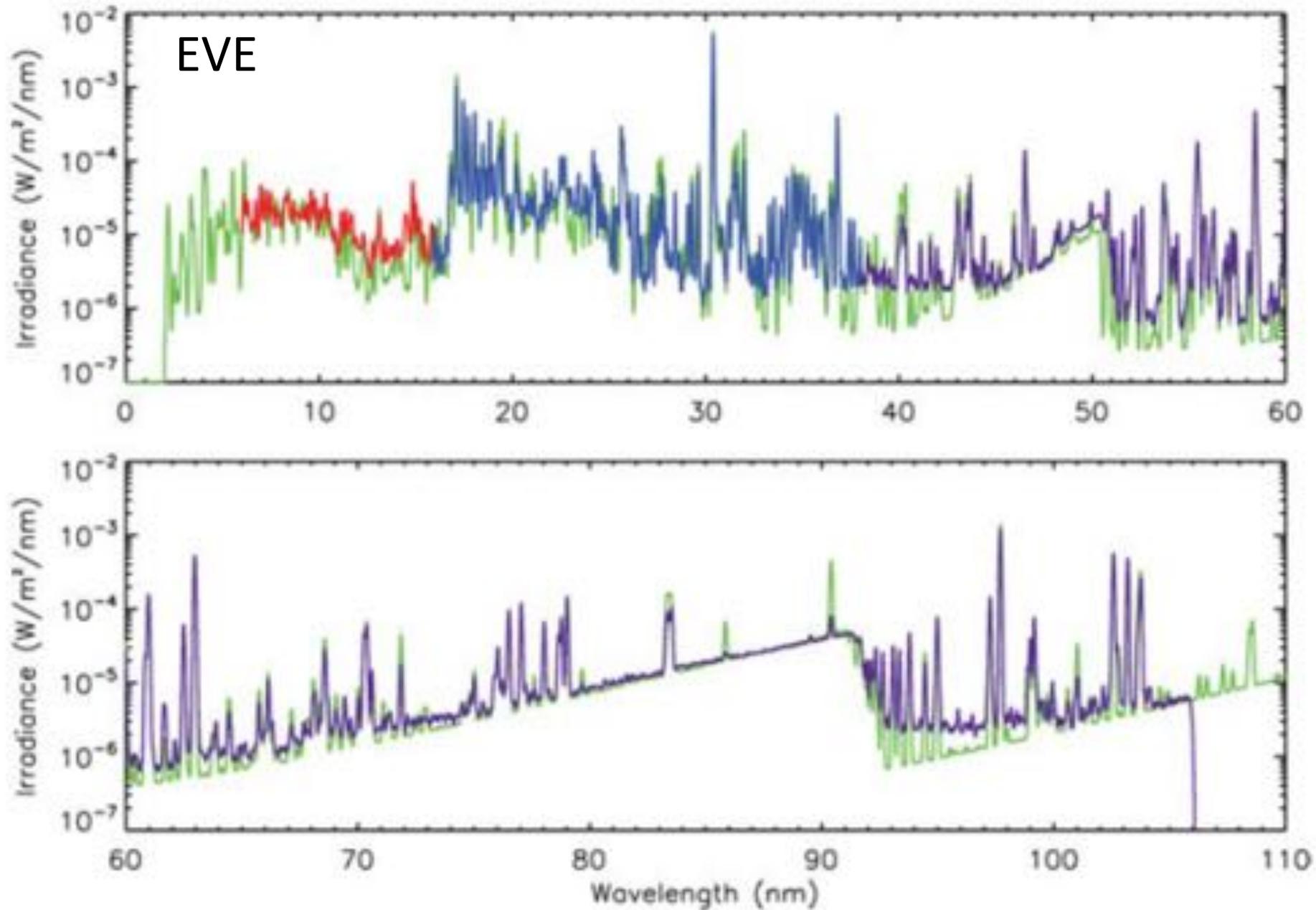


do smaller
flares heat
the corona?

Corona produces EUV & X-ray

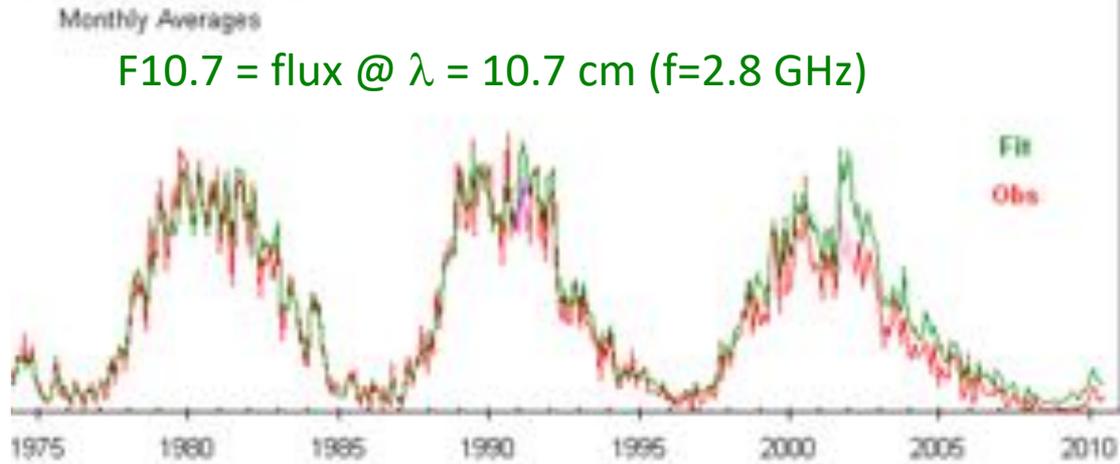
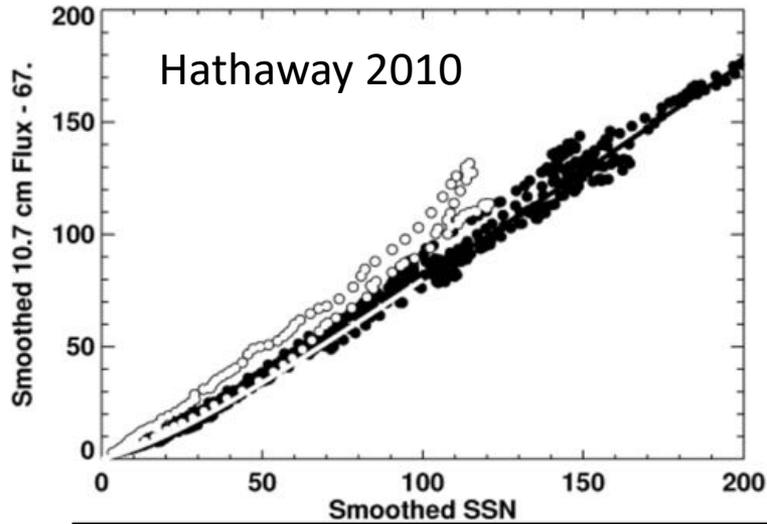


Vol. III, fig. 10.1

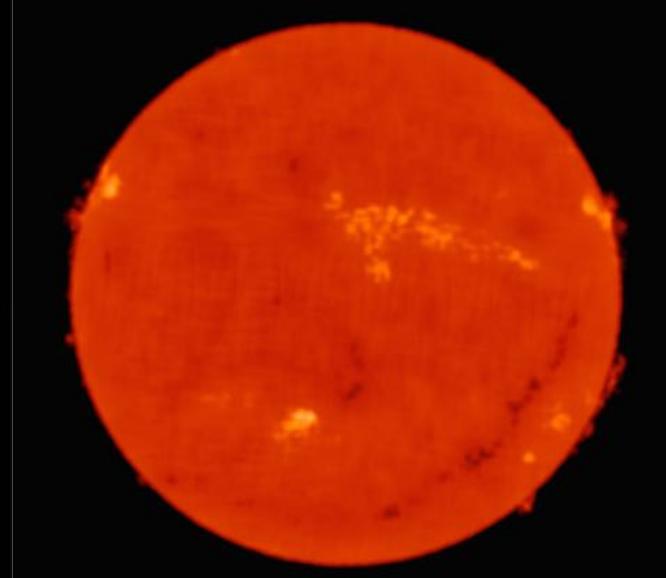


Corona produces μ -waves

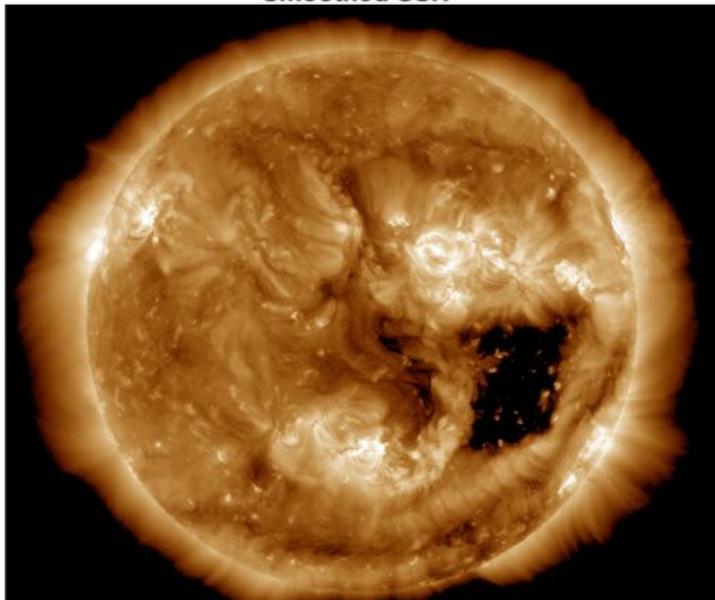
Sunspot Number (Observed) and Fitted from F10.7 Flux



NOBEYAMA RADIO HELIOGRAPH 17GHz (R+L)

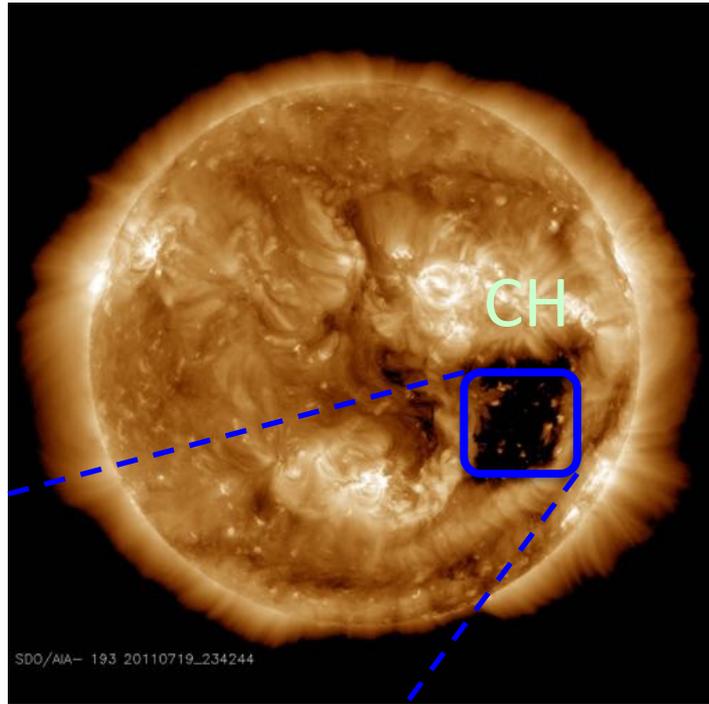


2011-07-19 02:44:35.084



SDO/AIA- 193 20110719_234244

B large enough to restrict plasma motion: only along field lines



Wind: from open flux

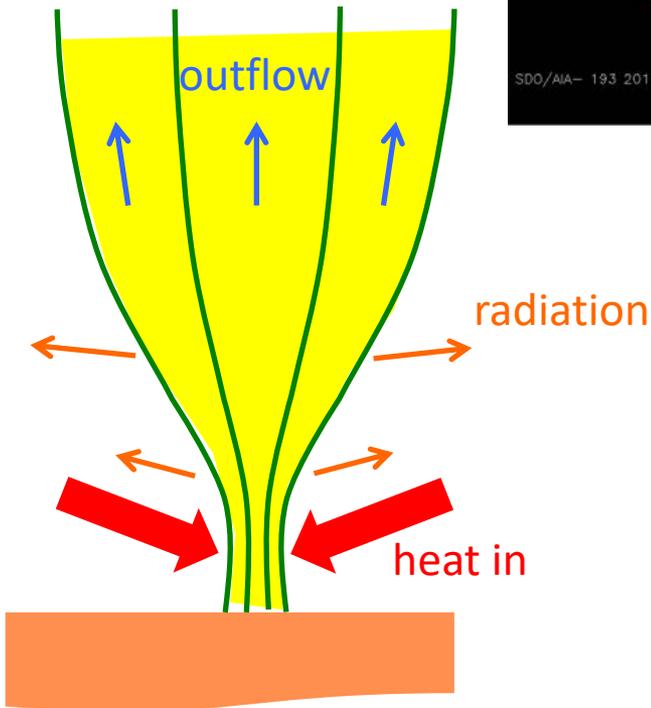
specific enthalpy

$$w(\rho) \propto \frac{\gamma}{\gamma - 1} \rho^{\gamma-1}$$

Advective energy loss –

$$\frac{1}{2} \rho \mathbf{v} \mathbf{v}^2 + \rho \mathbf{v} w(\rho)$$

>> radiative loss



Bernoulli's law: $\frac{Q}{\dot{M}} = \text{const.}$

Energy loss = $A\rho v \left[\frac{1}{2} v^2 + w(\rho) + \Psi(s) \right] = Q = \text{fixed \& given}$

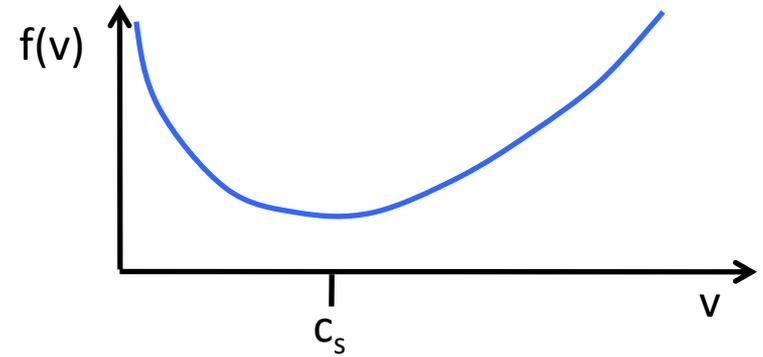
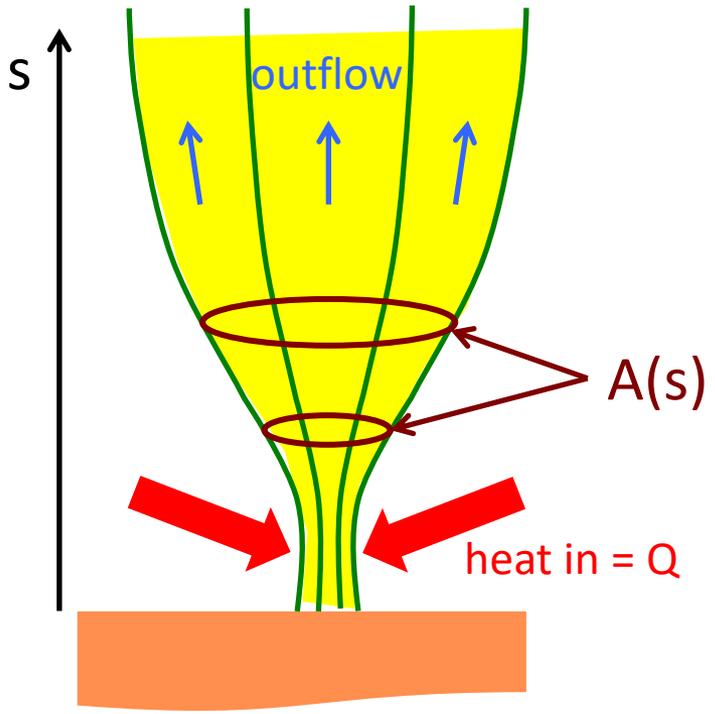
mass loss fixed & unknown

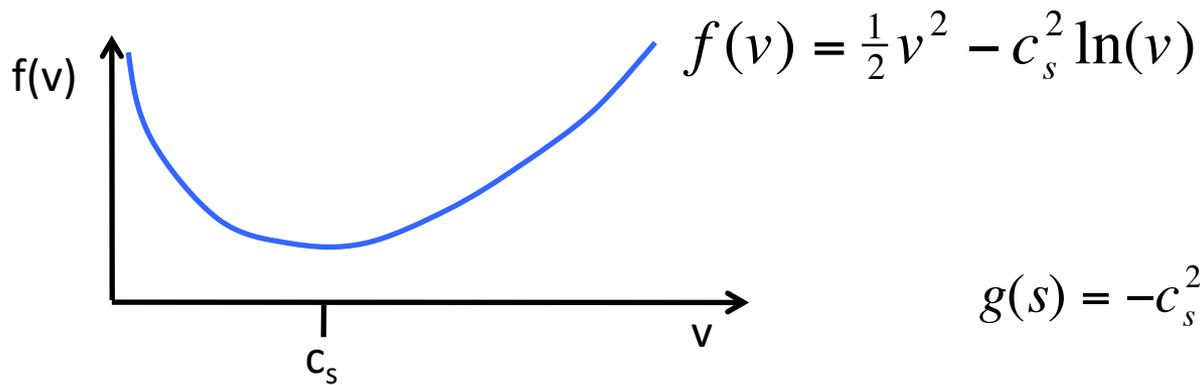
Simple case: Isothermal ... $\gamma \rightarrow 1$

$w(\rho) \propto \frac{\gamma}{\gamma - 1} \rho^{\gamma-1} \rightarrow c_s^2 \ln(\rho) + \text{const.}$

$\rightarrow \left[\frac{1}{2} v^2 - c_s^2 \ln(v) \right] - c_s^2 \ln[A(s)] + \Psi(s) = \text{const.}$

$= f(v) + g(s) = \text{const.}$





$$g(s) = -c_s^2 \ln[A(s)] - \frac{R_o v_{\text{esc}}^2}{2r(s)}$$

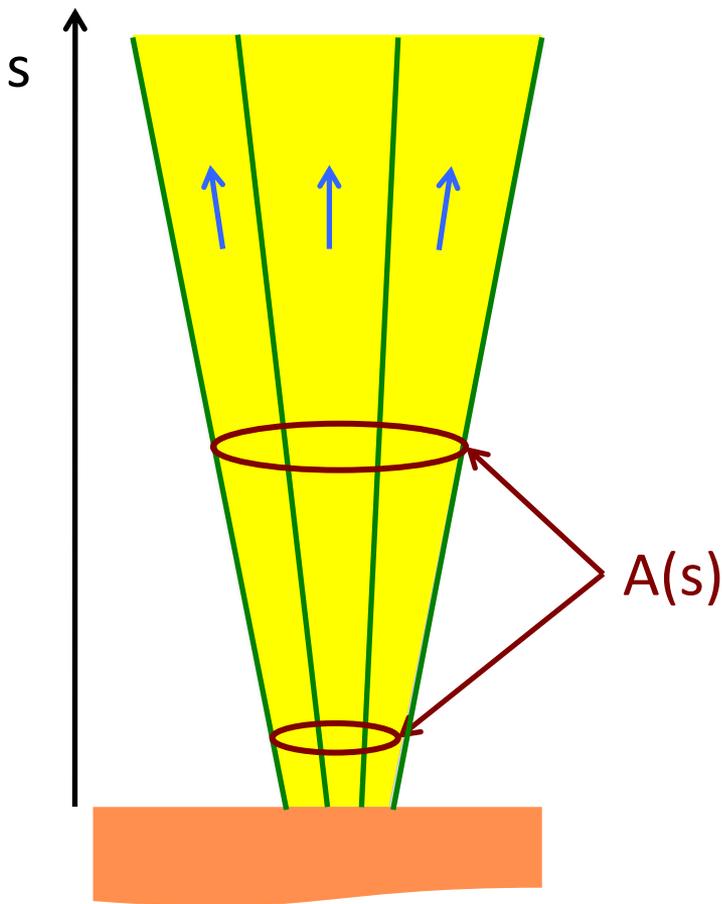
tube:

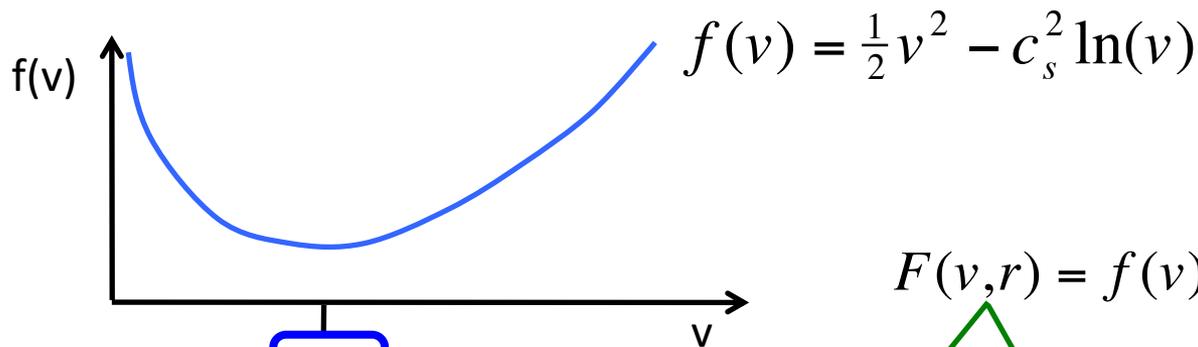
cone w/ vertical axis

$$A(s) \sim s^2$$

$$s = r$$

$$g(r) = -2c_s^2 \ln(r) - \frac{R_o v_{\text{esc}}^2}{2r}$$





c_s

tube:

cone w/ vertical axis

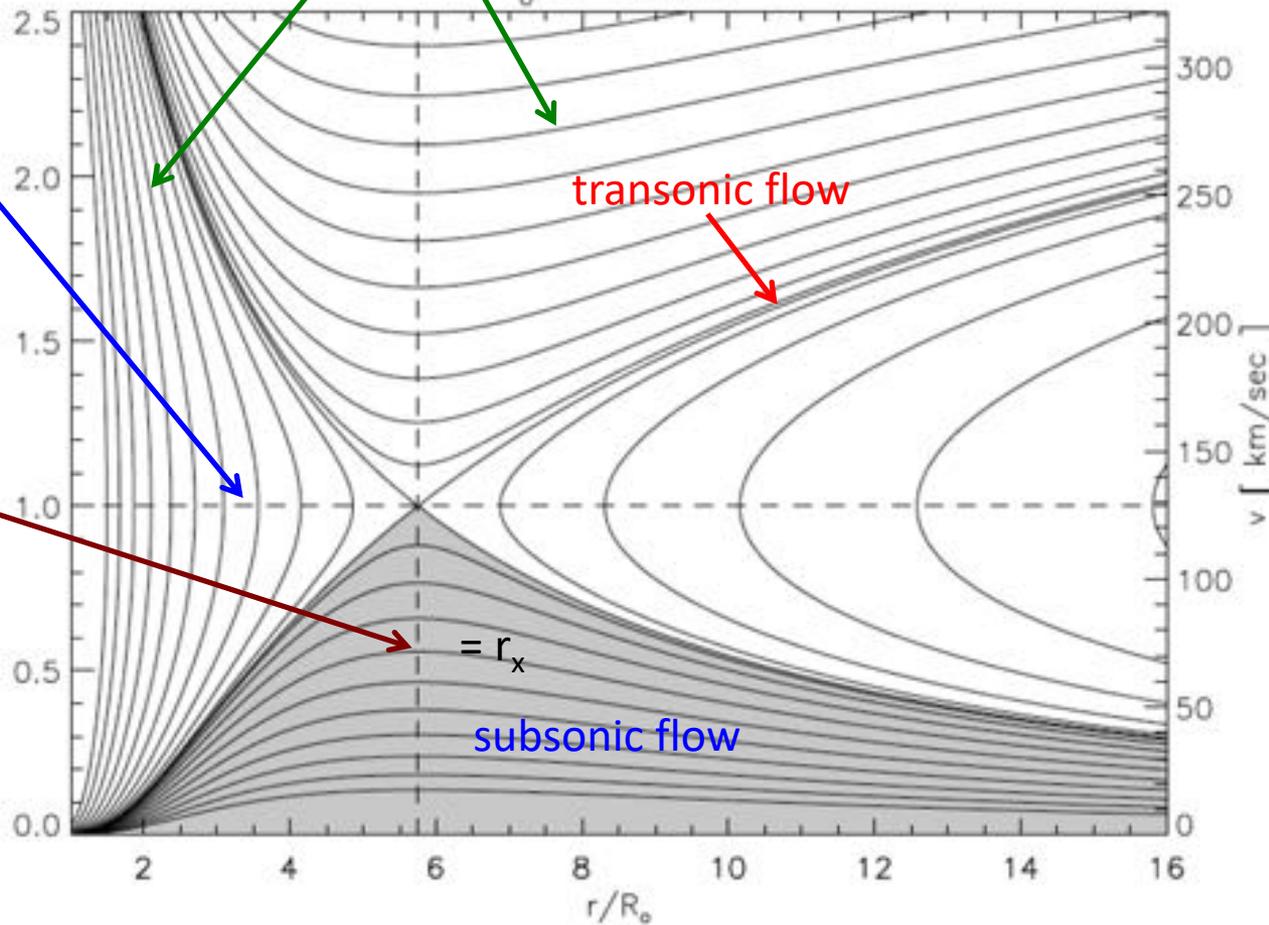
$A(s) \sim s^2$

$s = r$

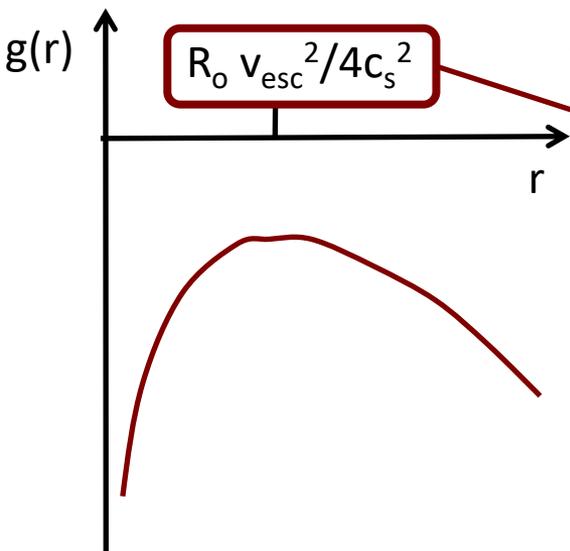
$g(r) = -2c_s^2 \ln(r) - \frac{R_o v_{esc}^2}{2r}$

$F(v, r) = f(v) + g(r) = \frac{Q}{\dot{M}} = \text{const.}$

$T_0 = 1.0 \text{ MK}$



$R_o v_{esc}^2 / 4c_s^2$



tube:

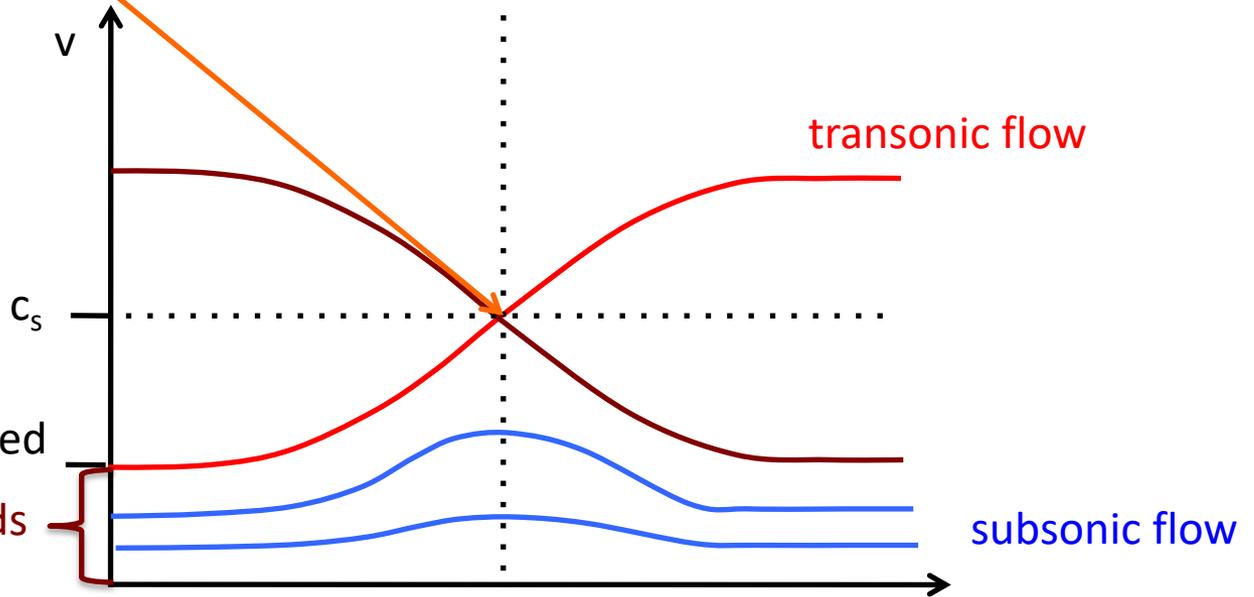
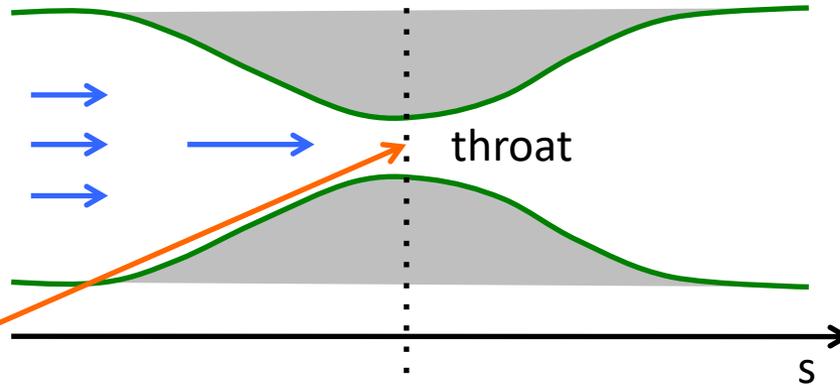
$$g(s) = -c_s^2 \ln[A(s)] + \Psi(s)$$

horizontal nozzle

$$\Psi(s) = \text{const.}$$

$$g(s) = -c_s^2 \ln[A(s)]$$

saddle @ max. $g(s)$
@ throat of nozzle



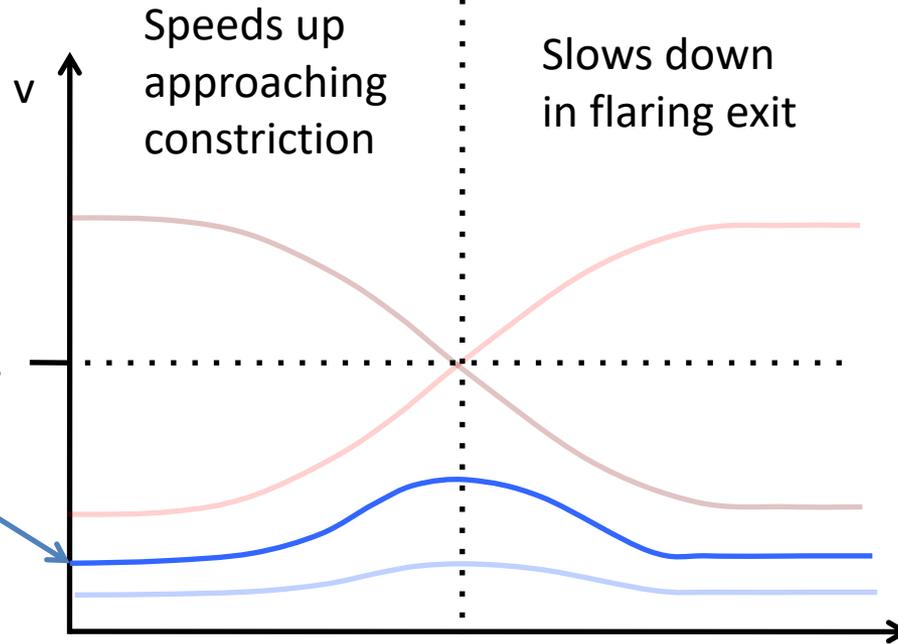
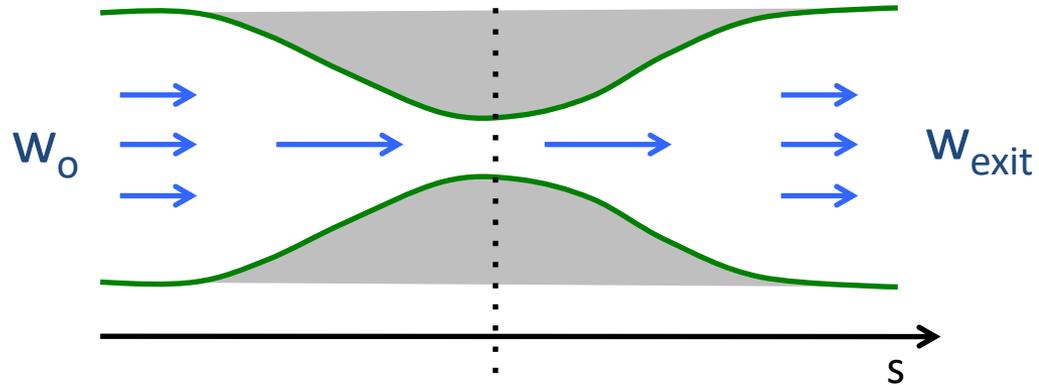
tube:

horizontal nozzle

$$\Psi(s) = \text{const.}$$

$$g(s) = -c_s^2 \ln[A(s)]$$

$$g(s) = -c_s^2 \ln[A(s)] + \Psi(s)$$



Inflow = mass loss rate

set by back-pressure

W_{exit}

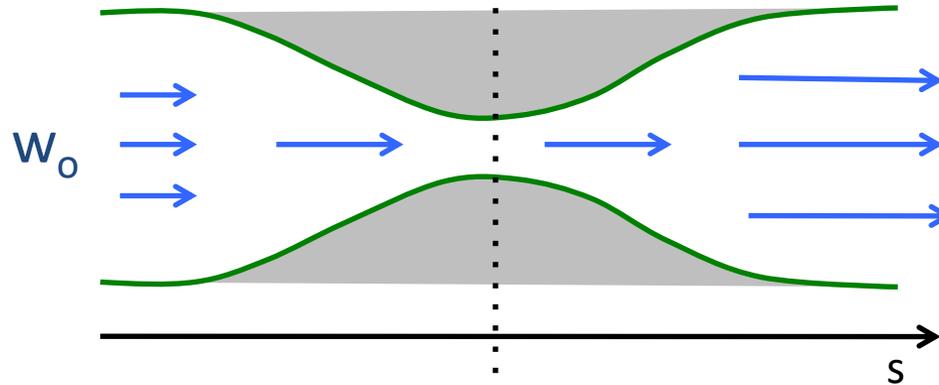
tube:

horizontal nozzle

$$\Psi(s) = \text{const.}$$

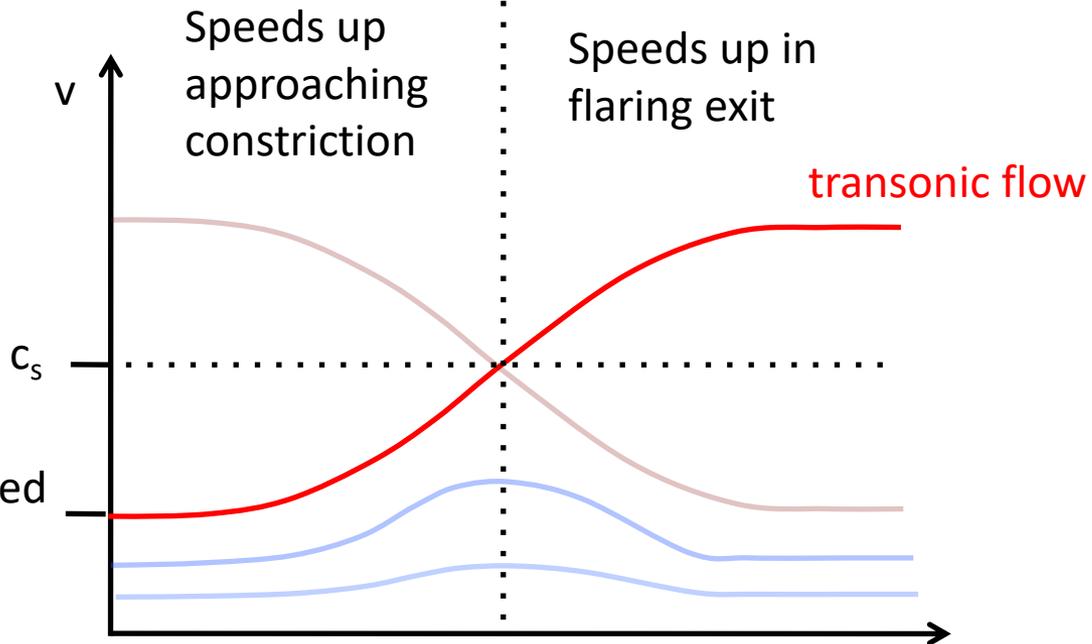
$$g(s) = -c_s^2 \ln[A(s)]$$

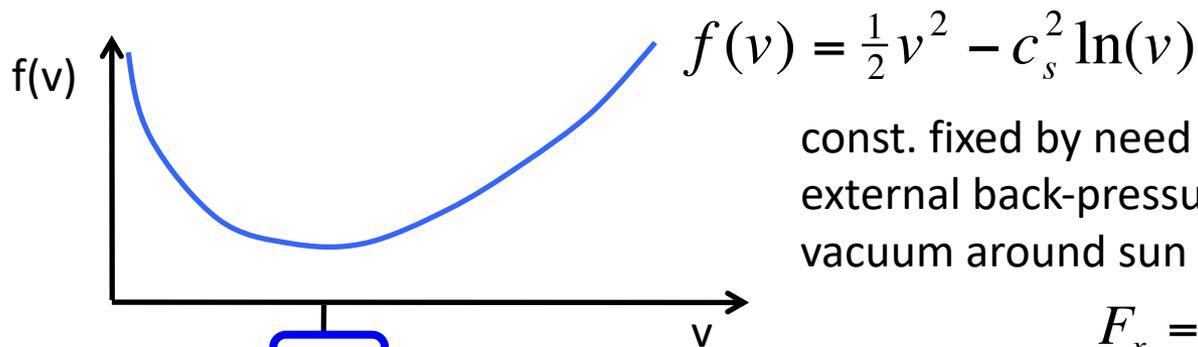
$$g(s) = -c_s^2 \ln[A(s)] + \Psi(s)$$



occurs for
back-pressure
insufficient to
keep flow
sub-sonic

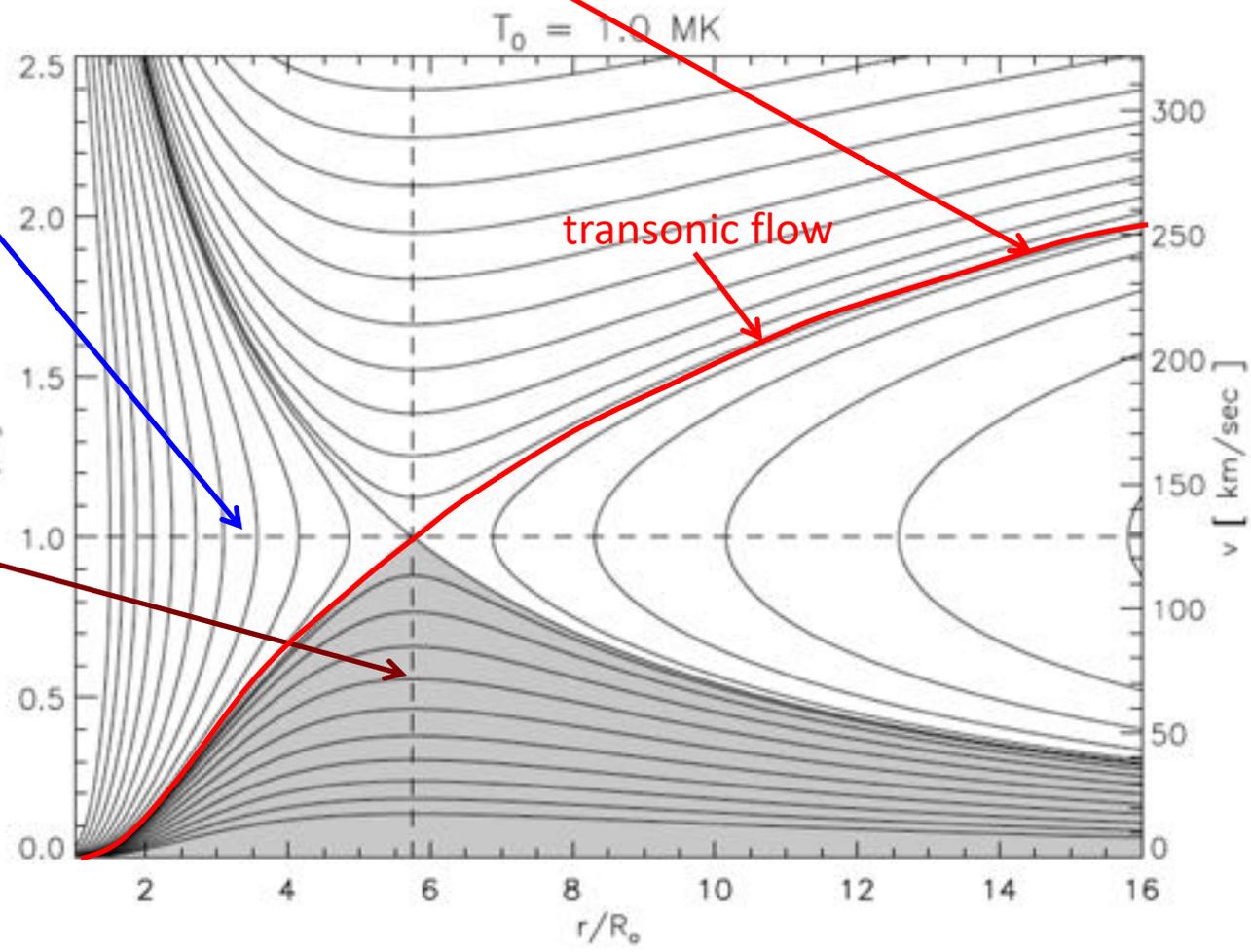
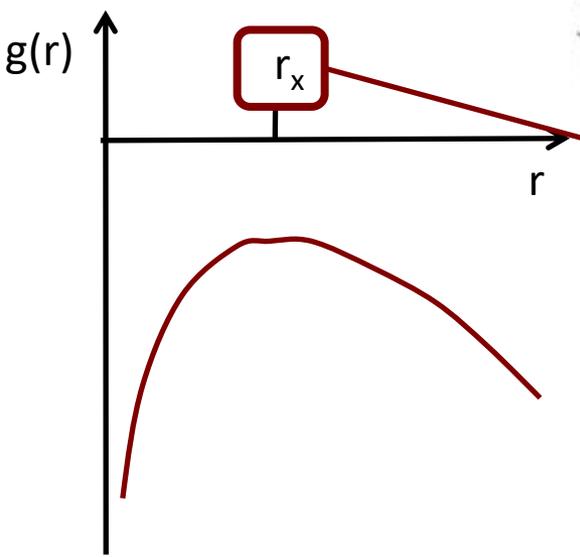
max. inflow speed





$$F_x = f(c_s) + g(r_x) = \frac{Q}{\dot{M}}$$

$$g(r) = -2c_s^2 \ln(r) - \frac{R_o v_{esc}^2}{2r}$$



→ Mass loss rate is set by heating rate*

$$\dot{M} = \frac{Q}{F_x}$$

→ density everywhere is set by mass loss rate

$$\rho(r_x) = \frac{\dot{M}}{A(r_x)c_s}$$

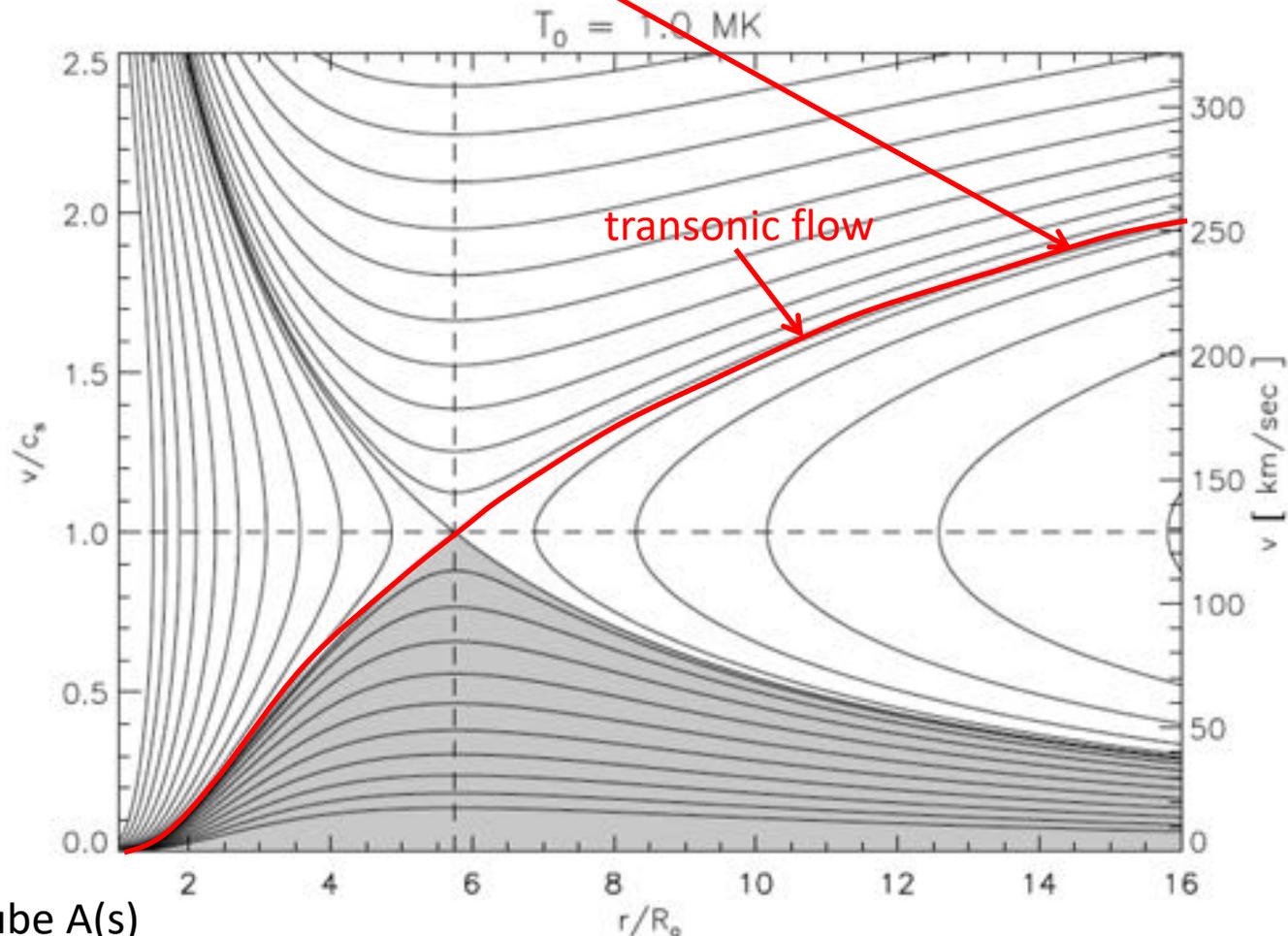
→ density @ base is set by heating rate*...

... and it will be lower than density on closed loops w/ same heating (Why?)

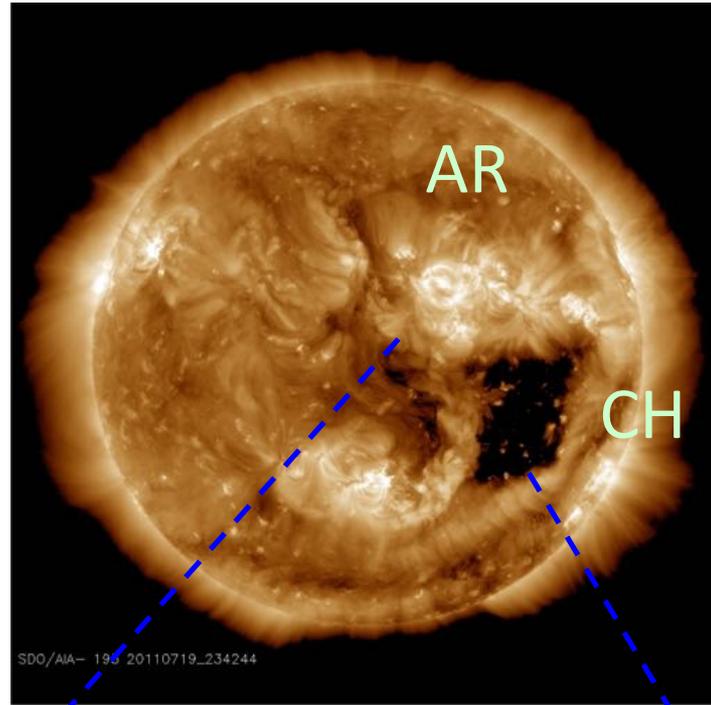
* ... and geometry of flux tube A(s)

const. fixed by need to become transonic when external back-pressure is insufficient – i.e. vacuum around sun

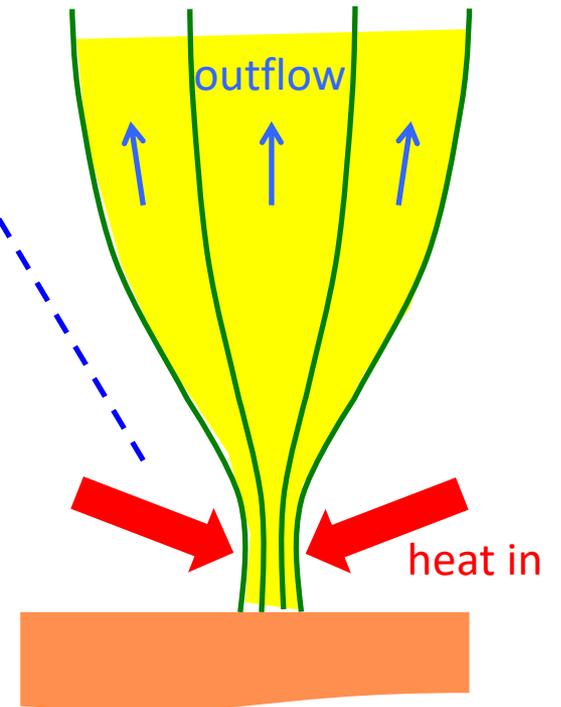
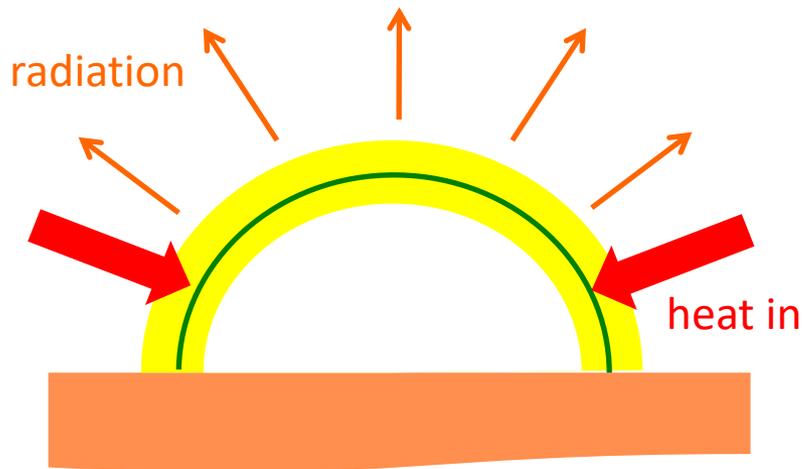
$$F_x = f(c_s) + g(r_x) = \frac{Q}{\dot{M}}$$



B large enough to restrict plasma motion: only along field lines



Different coronae from different magnetic topology: open vs. closed



Why are some field lines open & others closed?

Magnetic field dominates:
nothing capable of countering its force so...

$$(\nabla \times \mathbf{B}) \times \mathbf{B} = 0$$
$$\Rightarrow \nabla \times \mathbf{B} = \alpha \mathbf{B} \quad (\text{i.e. } \parallel \mathbf{B})$$

simplest version: $\alpha = 0$ (by fiat)

$$\Rightarrow \nabla \times \mathbf{B} = 0 \quad \Rightarrow \mathbf{B} = -\nabla \chi \quad \text{potential field}$$

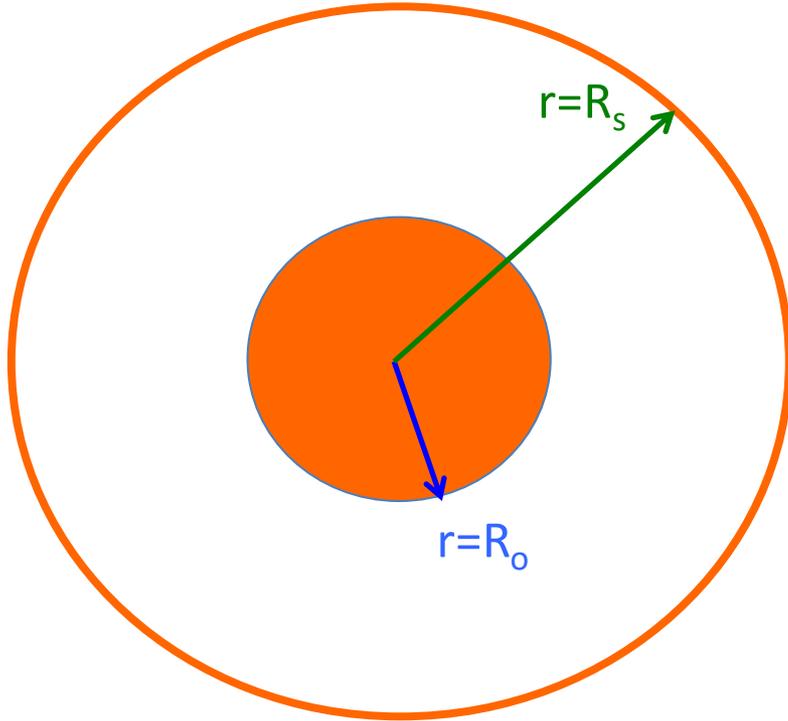
(cf. electrostatics)

$$\nabla \cdot \mathbf{B} = 0 \quad \Rightarrow \quad \nabla^2 \chi = 0 \quad \text{harmonic potential}$$

(cf. electrostatics in vacuum)

$$\mathbf{B} = -\nabla\chi \quad \& \quad \nabla^2\chi = 0$$

potential field outside
sphere $r=R_0$

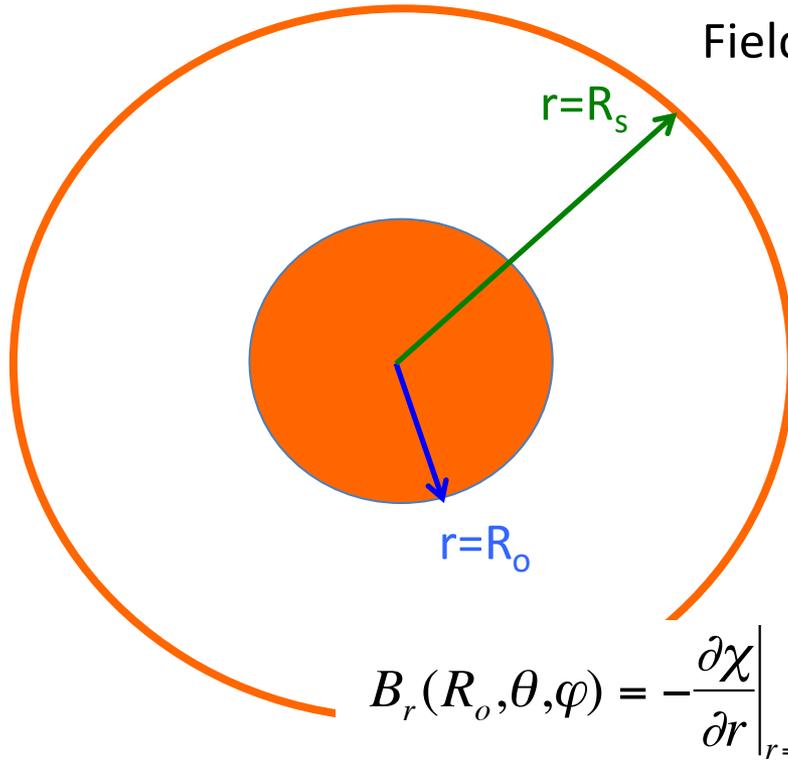


$$\mathbf{B} = -\nabla\chi \quad \& \quad \nabla^2\chi = 0 \quad \text{potential field outside sphere } r=R_o$$

Field: purely radial @ $r=R_s$ (by fiat)

$$(B_\theta, B_\varphi) = 0 \quad \Rightarrow \quad \left(\frac{\partial\chi}{\partial\theta}, \frac{\partial\chi}{\partial\varphi} \right) = 0$$

$$\Rightarrow \quad \chi(R_s, \theta, \varphi) = 0 \quad \text{Dirichlet}$$



$$\chi(r, \theta, \varphi) = \sum_{\ell, m} A_{\ell, m} \left[\left(\frac{R_s}{r} \right)^{\ell+1} - \left(\frac{r}{R_s} \right)^\ell \right] Y_{\ell, m}(\theta, \varphi)$$

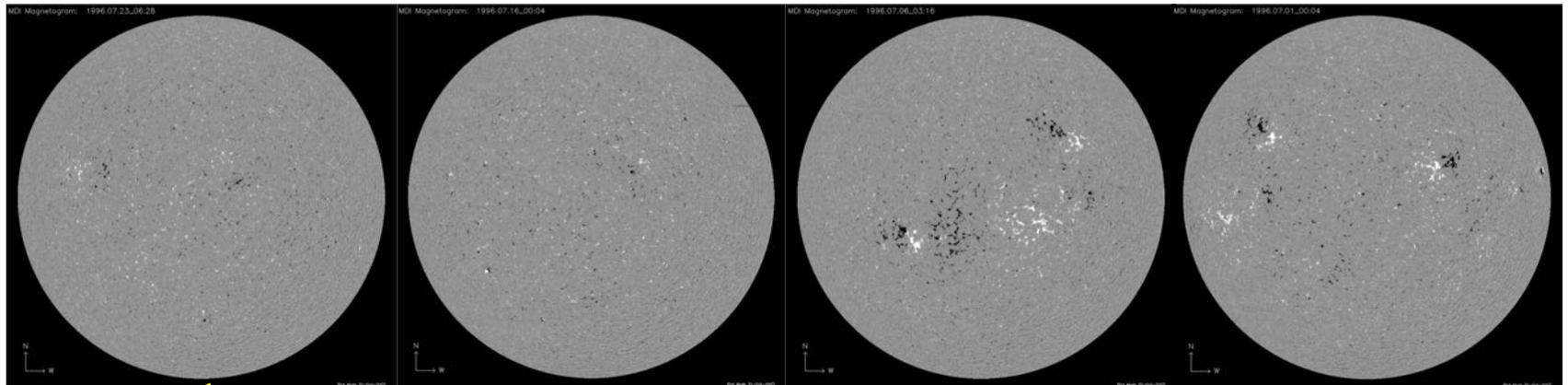
$$B_r(R_o, \theta, \varphi) = - \left. \frac{\partial\chi}{\partial r} \right|_{r=R_o}$$

Observed (Neumann)

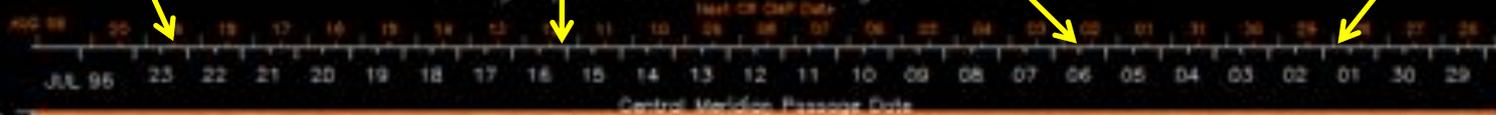
$$B_r(R_o, \theta, \varphi) = \sum_{\ell, m} \frac{A_{\ell, m}}{R_s} \left[(\ell + 1) \left(\frac{R_s}{R_o} \right)^{\ell+2} + \ell \left(\frac{R_o}{R_s} \right)^{\ell-1} \right] Y_{\ell, m}(\theta, \varphi)$$

- Observe $B_r(\theta, \phi)$
@ photosphere
- decompose w/ spherical harmonics
- coeffs. $\rightarrow A_{l, m}$

← time



MDI Synoptic Chart for Carrington Rotation 1911



$B_r(\theta, \phi)$ "measured" over entire sphere

- accumulate strips over 27-day rotation
- hope that not much changes
- fill in poles (somehow)

Sine Latitude

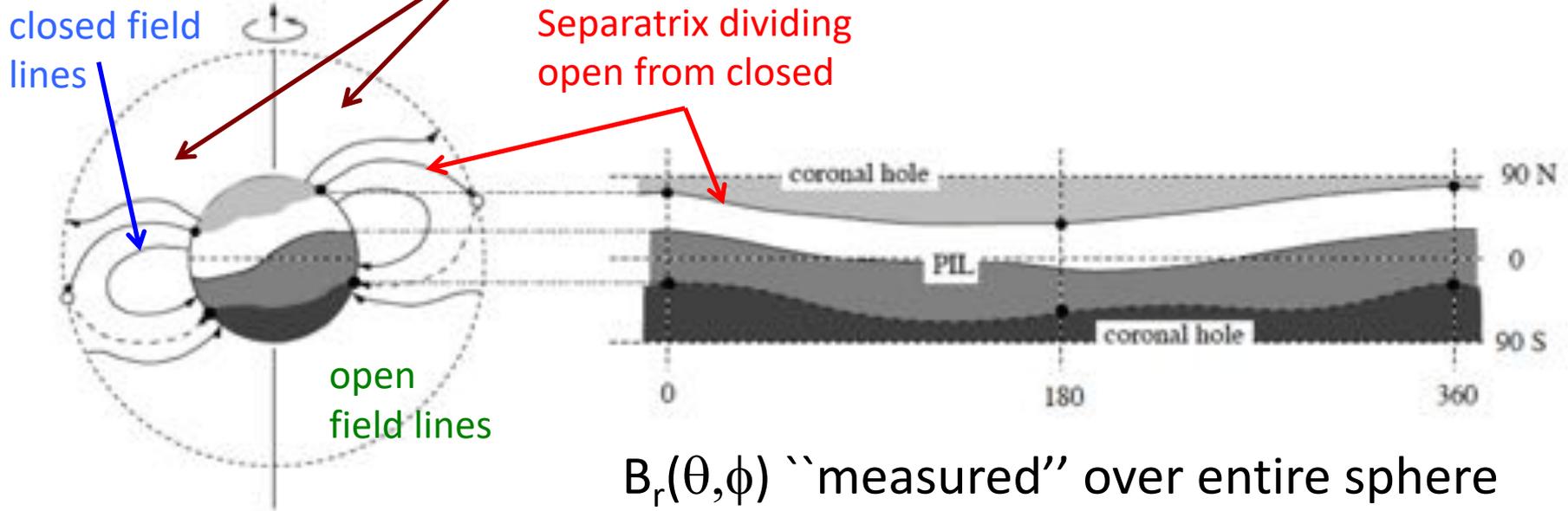
Latitude

Carrington Longitude

$$\chi(r, \theta, \varphi) = \sum_{\ell, m} A_{\ell, m} \left[\left(\frac{R_s}{r} \right)^{\ell+1} - \left(\frac{r}{R_s} \right)^{\ell} \right] Y_{\ell, m}(\theta, \varphi)$$

PFSS model

(potential field source surface)



Solar wind flows from open field crossing $r=R_s$... the 'source' of the wind
 → the 'source surface'

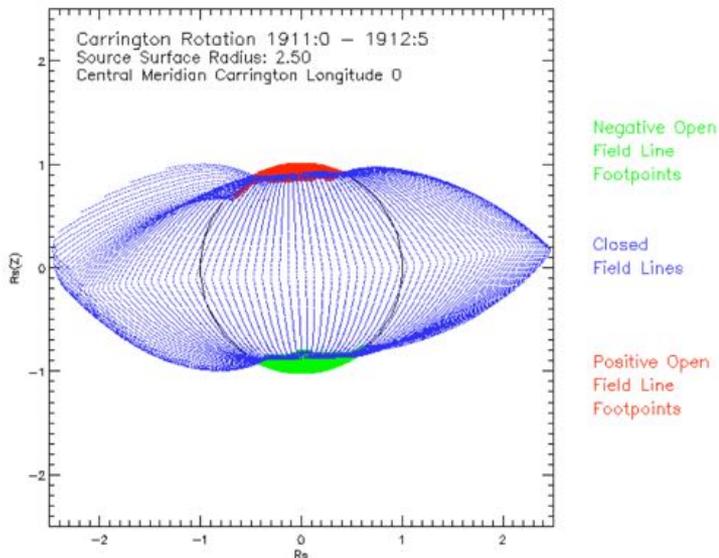
- $B_r(\theta, \phi)$ "measured" over entire sphere
- accumulate strips over 27-day rotation
 - hope that not much changes
 - fill in poles (somehow)
 - decompose w/ spherical harmonics
 - coeffs. → $A_{l, m}$

Assumptions of the PFSS

- No currents in coronal field (simplest equilibrium)

$$\nabla \times \mathbf{B} = 0 \quad R_o < r < R_s$$

- Field becomes open (radial) @ fixed radius $r=R_s$
- Not much change during 27-day accumulation

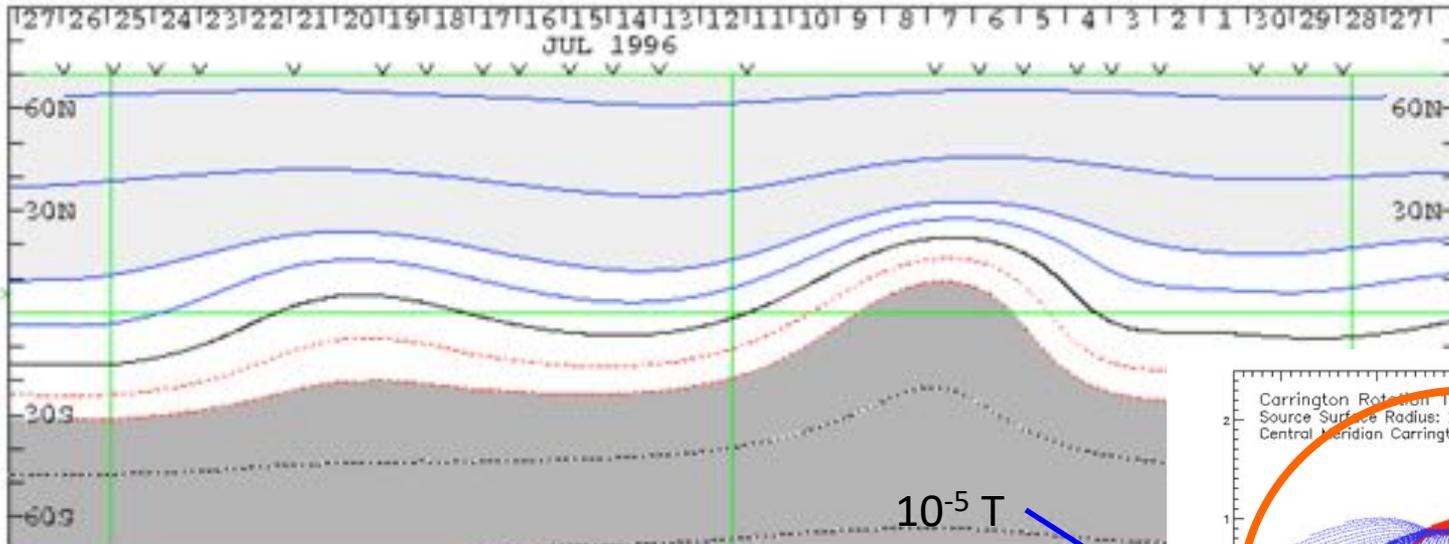


➔ **Model** distinguishing open/closed coronal field

➔ Field **actually** open will be source of solar wind, less dense & dark in EUV & SXR

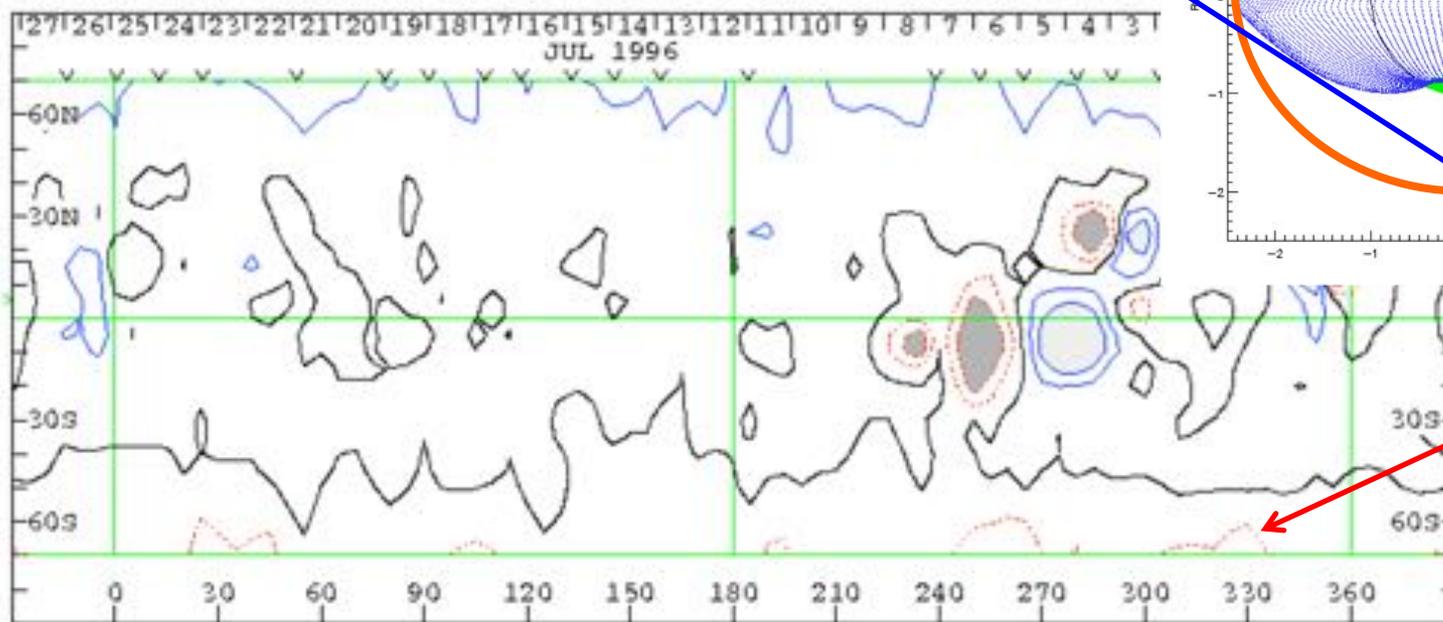
W30 - Source Surface Field

0, ±1, 2, 5, 10, 20 MicroTesla

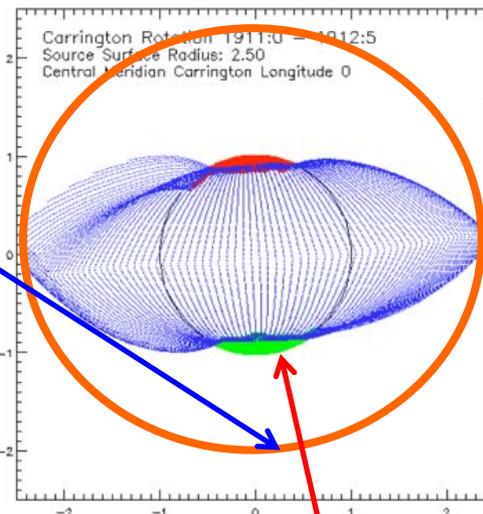


W30 - Photospheric Magnetic Field

0, ±100, 200, 500, 1000, 2000 Gauss



1911



Heliosphere

$$\vec{B} = B_R \hat{R} + B_\phi \hat{\phi}$$

$$\vec{V} = V_R \hat{R}$$

Source surface

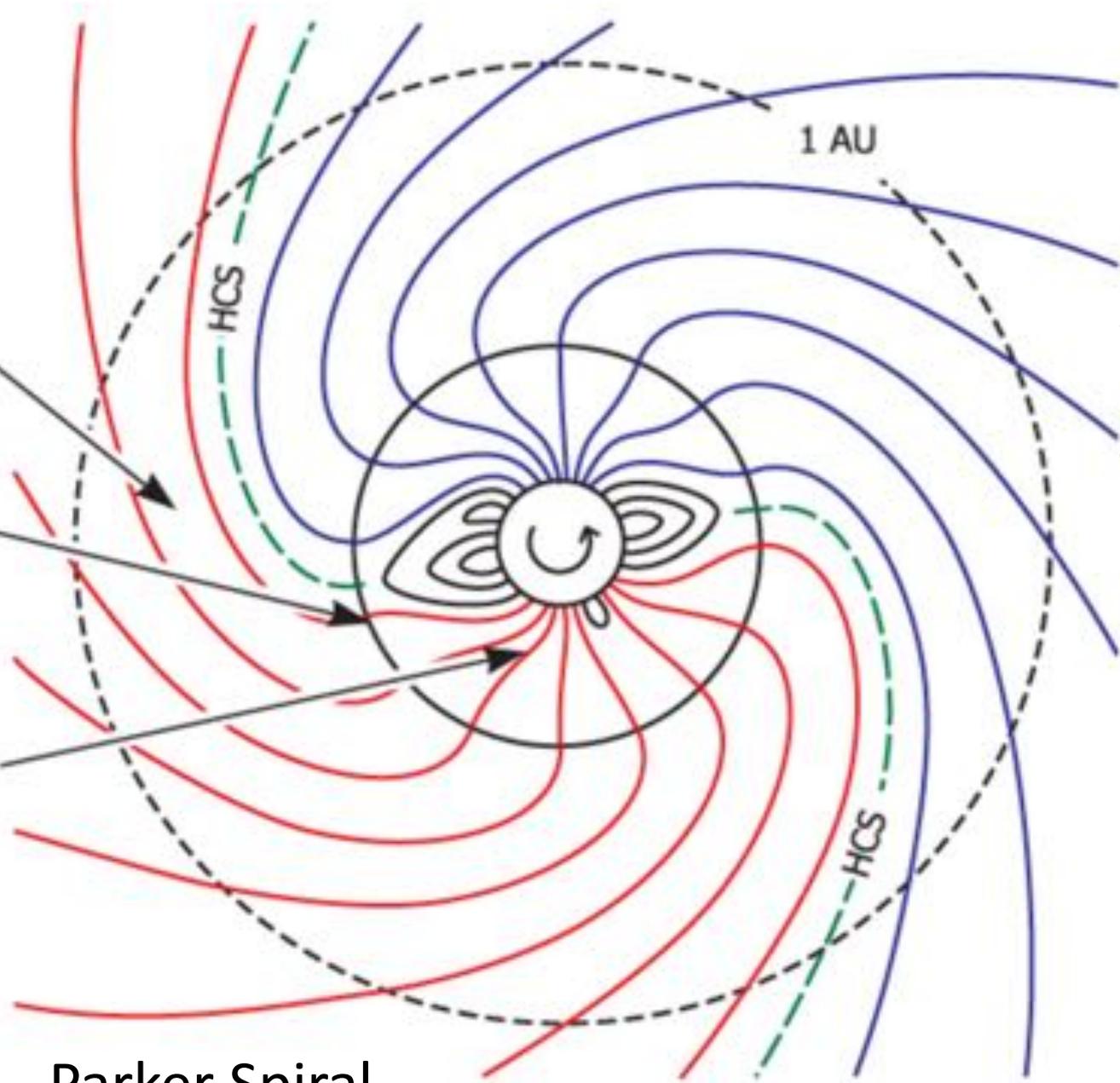
$$\vec{B} = B_R \hat{R}$$

$$\vec{V} = V_R \hat{R}$$

Super-radial expansion

$$\vec{B} = B_R \hat{R} + B_\theta \hat{\theta} + B_\phi \hat{\phi}$$

$$\vec{V} = V_R \hat{R} + V_\theta \hat{\theta} + V_\phi \hat{\phi}$$

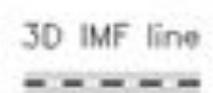
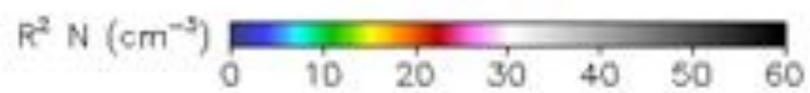
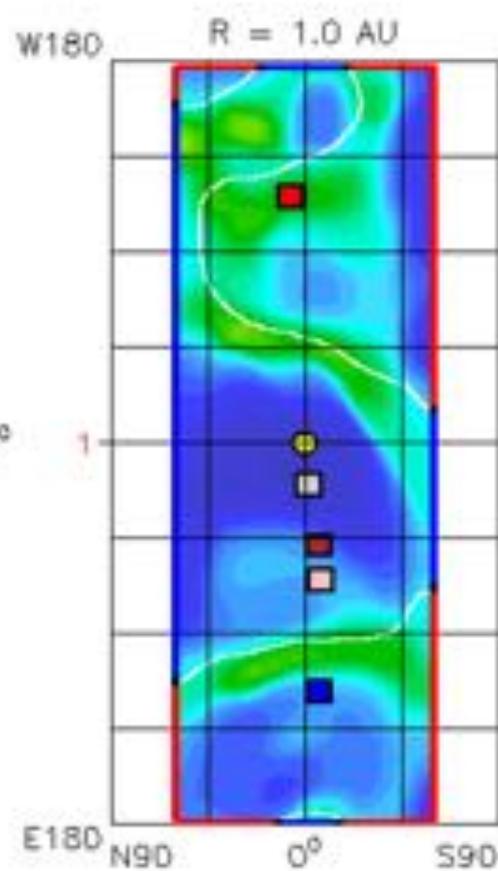
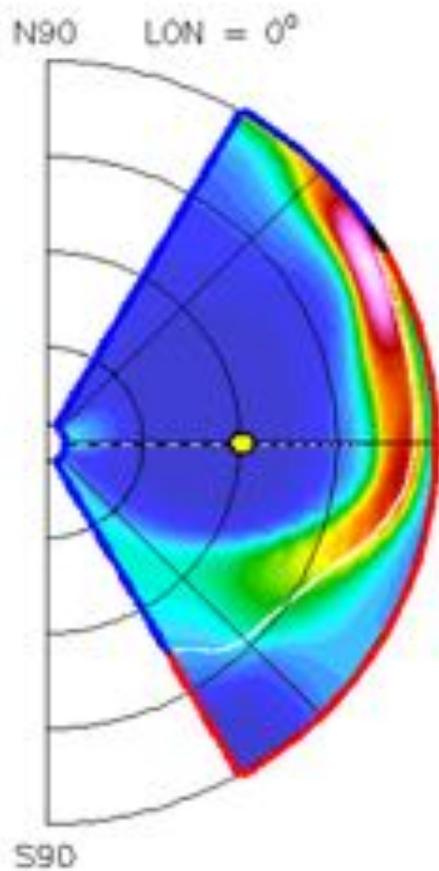
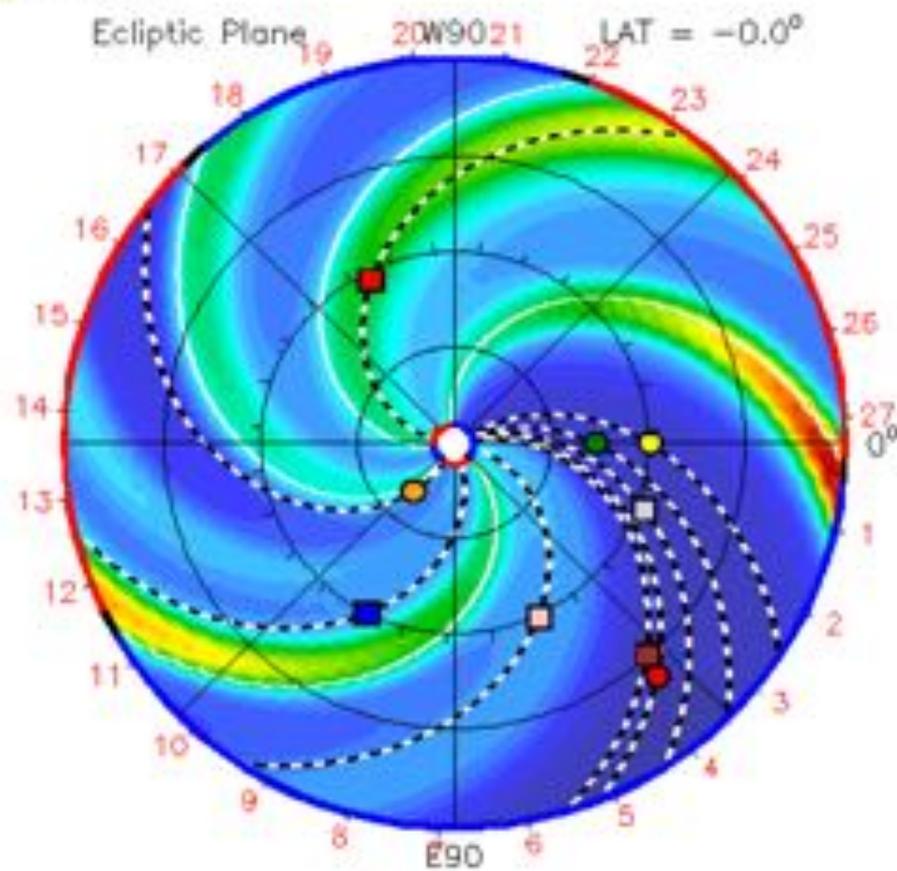


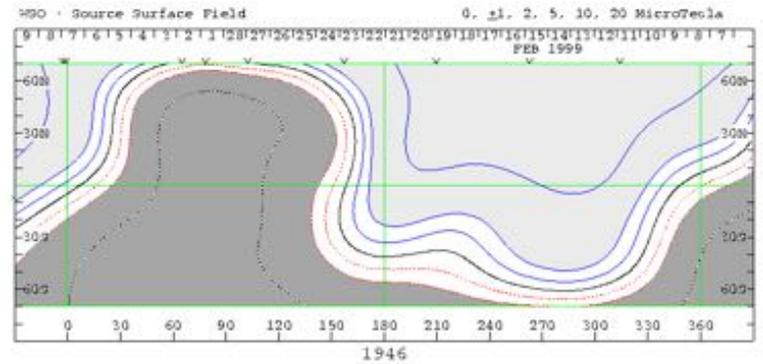
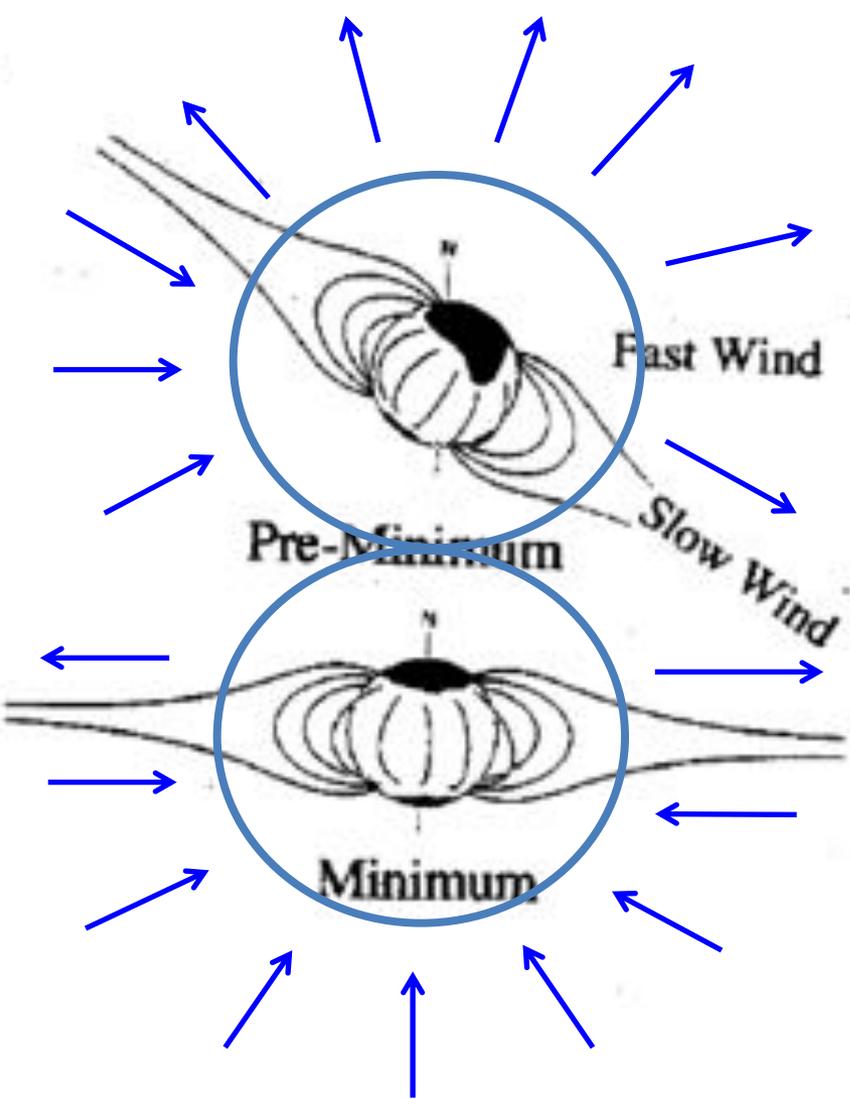
Parker Spiral

2012-06-06T00:00

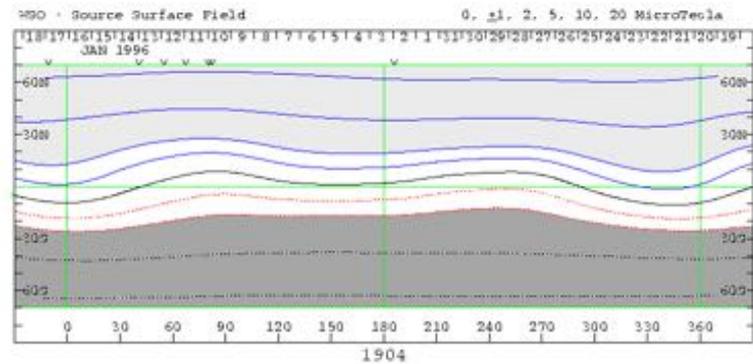
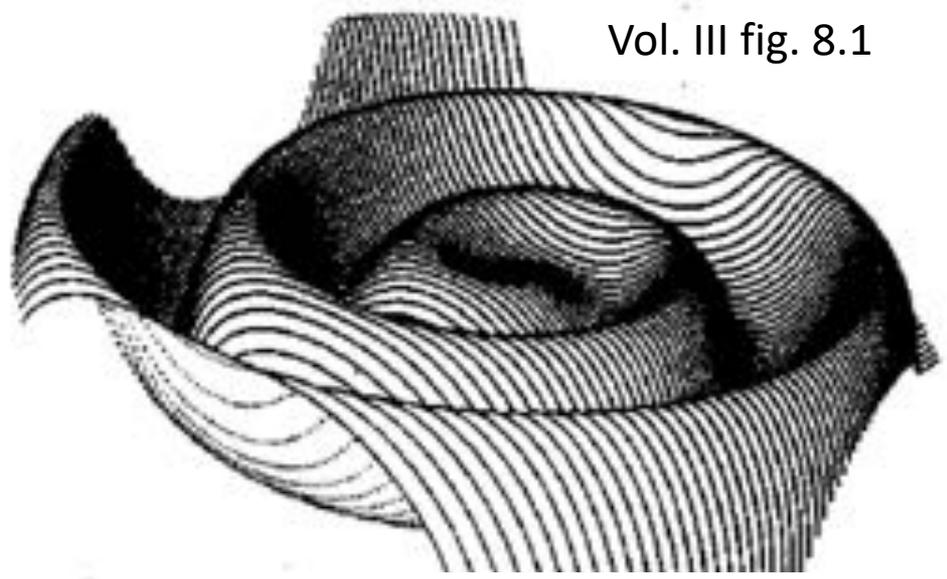
2012-06-06T00 +0.00 day

- Earth ● Mars ● Mercury ● Venus □ Kepler ■ MSL □ Spitzer ■ Stereo_A
■ Stereo_B

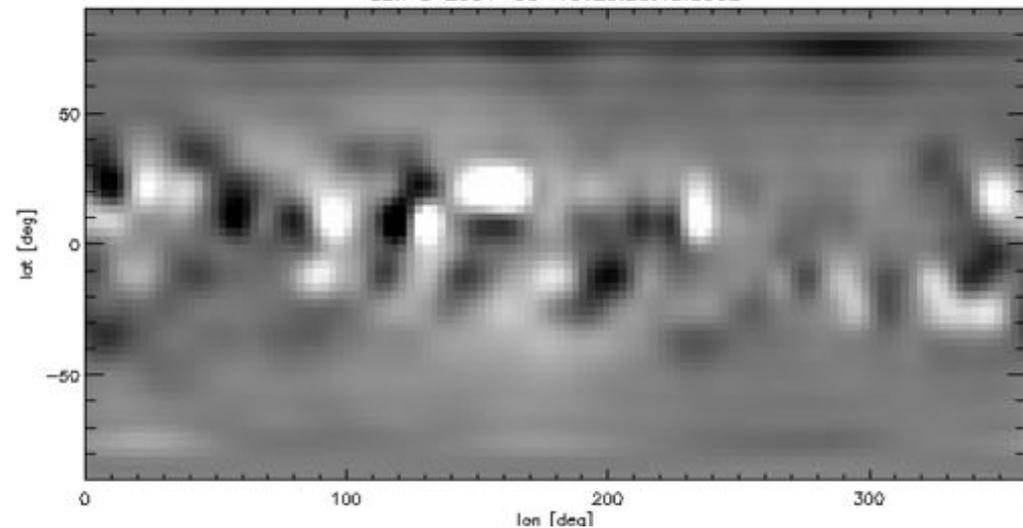




Vol. III fig. 8.1



Sun 2001-05-19T20:26:15.000Z

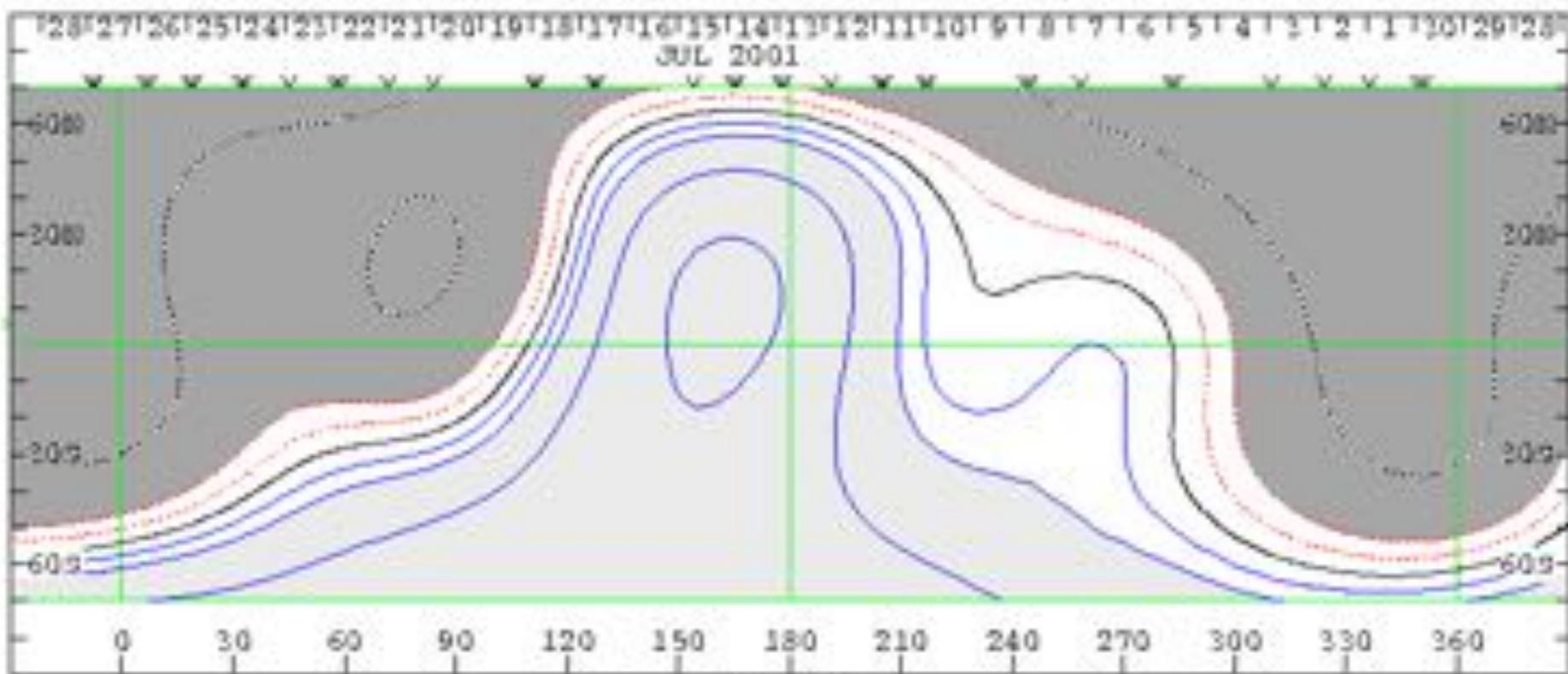


$$r = R_{\odot}$$

$$r = 2.5 R_{\odot}$$

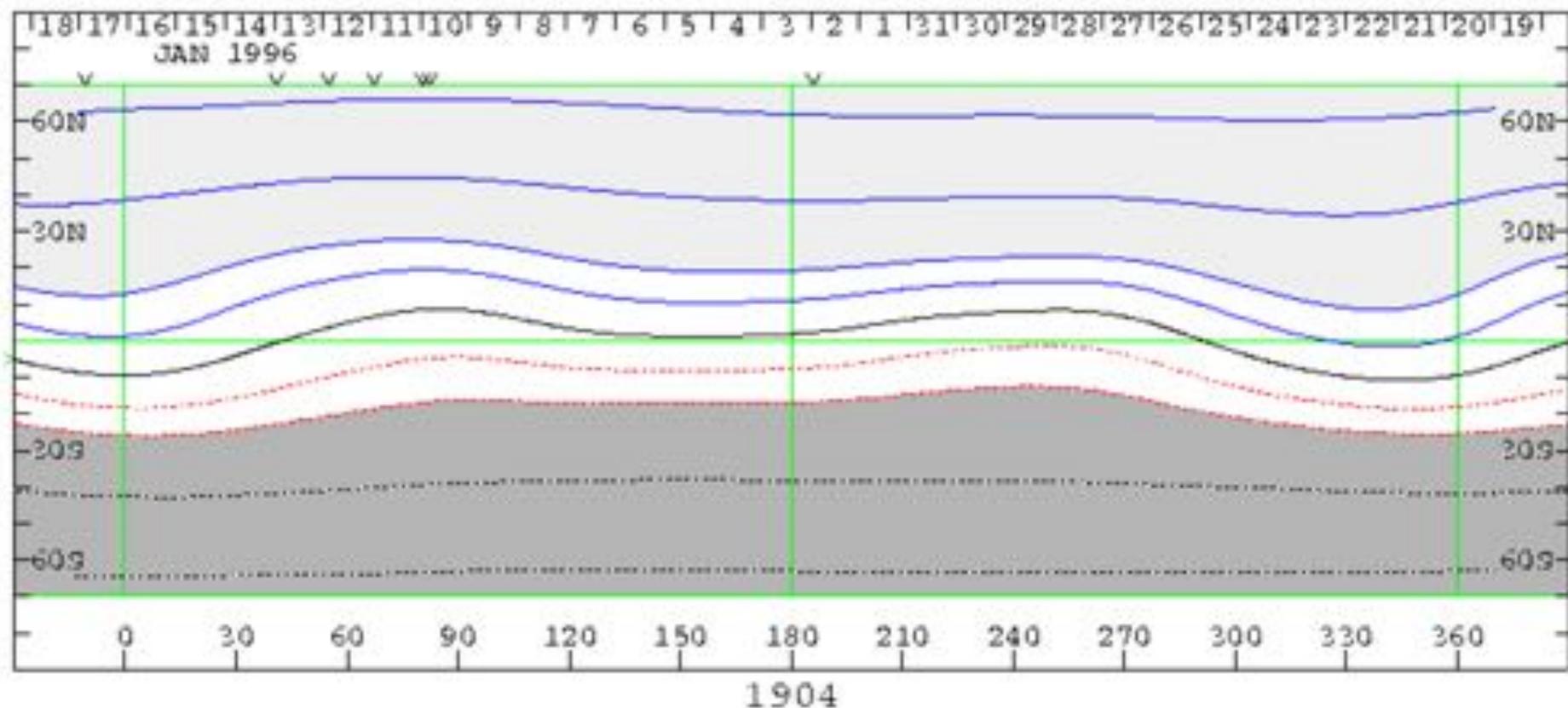
WFO - Source Surface Field

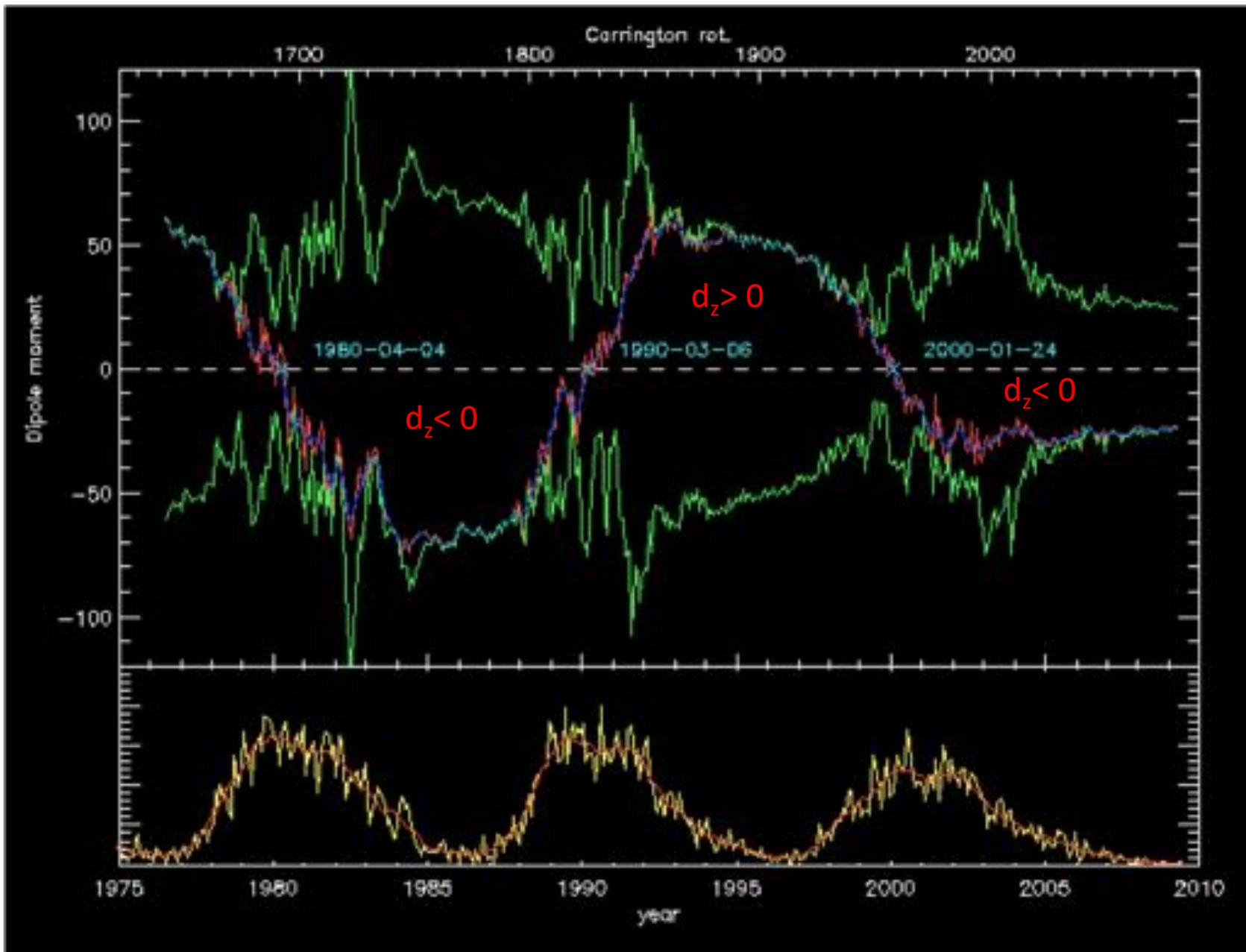
0, 1, 2, 5, 10, 20 MicroTesla



W30 - Source Surface Field

0, ± 1 , 2, 5, 10, 20 MicroTesla



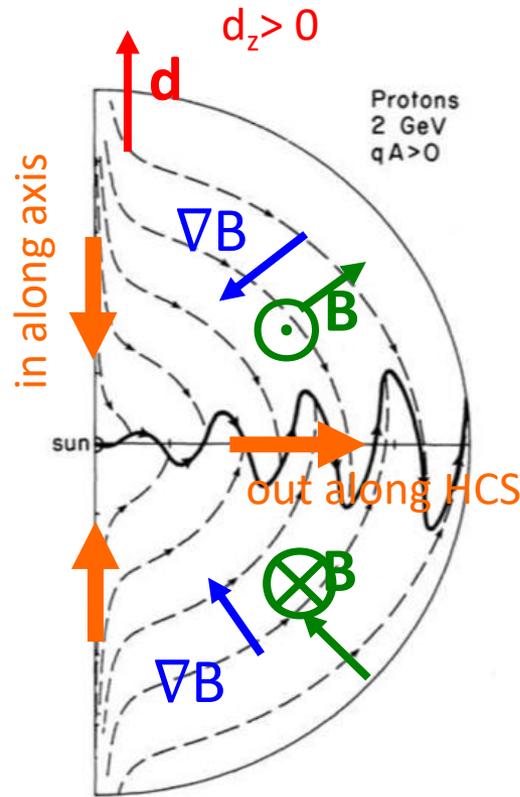


cosmic rays

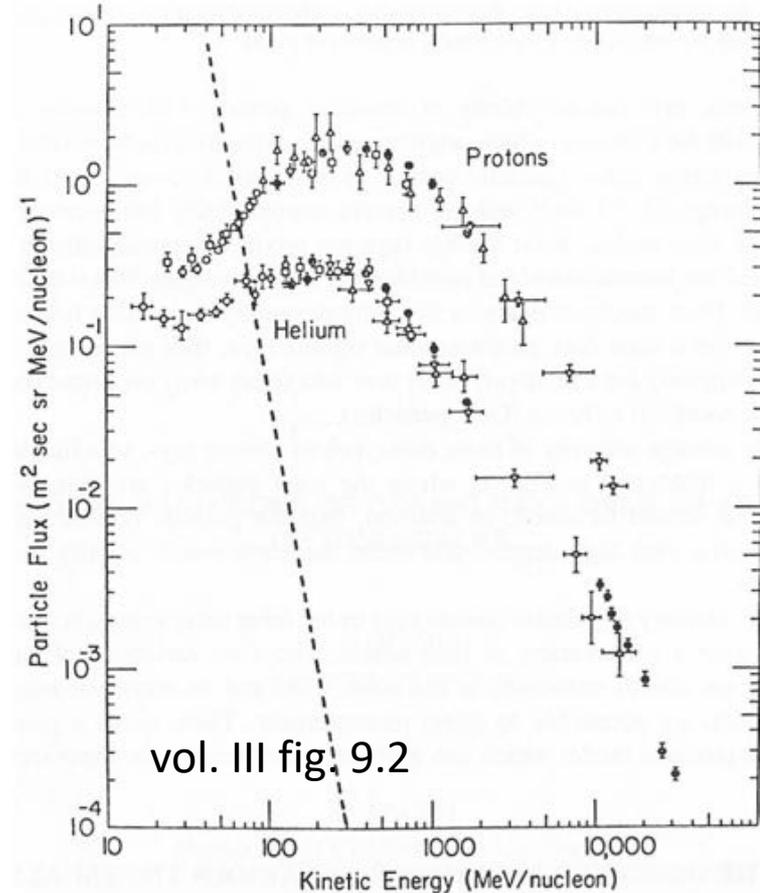
- Originate far away in galaxy – in supernova remnant shocks
- Enter solar system isotropically
- No collisions with SW particles
- Deflected by SW \mathbf{B}
 - Advected outward
 - Diffused by \mathbf{B} fluctuations
 - Drift:
 - in along axis
 - out along HCS

$$\mathbf{v}_d = \frac{pcw}{3q} \nabla \times \left(\frac{\mathbf{B}}{B^2} \right)$$

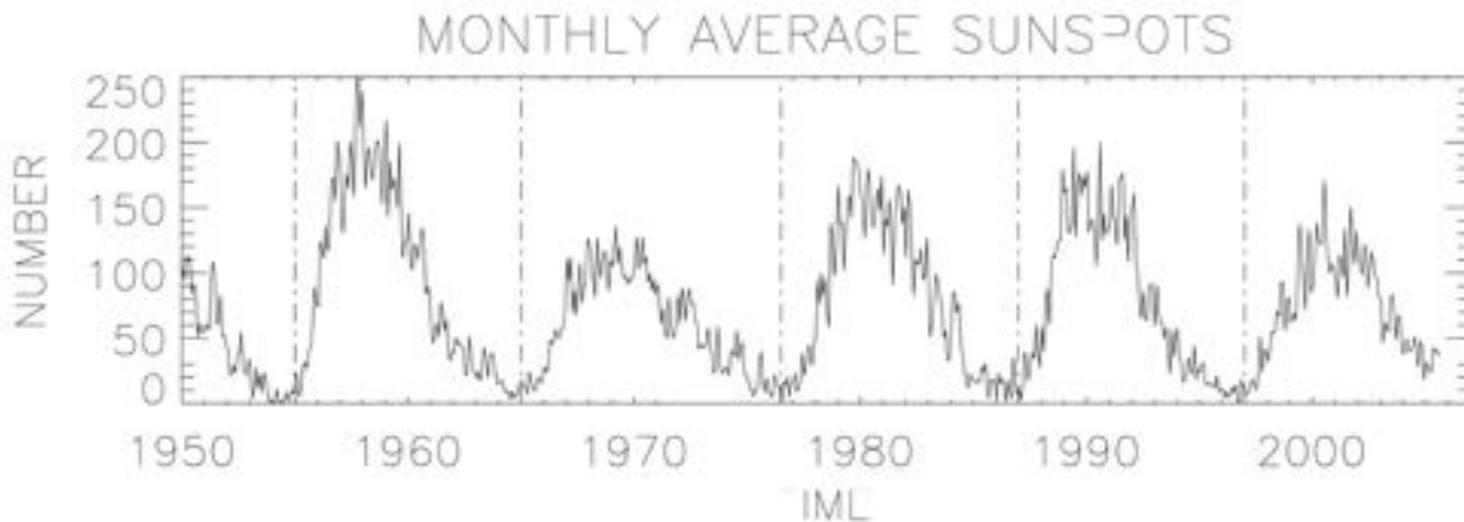
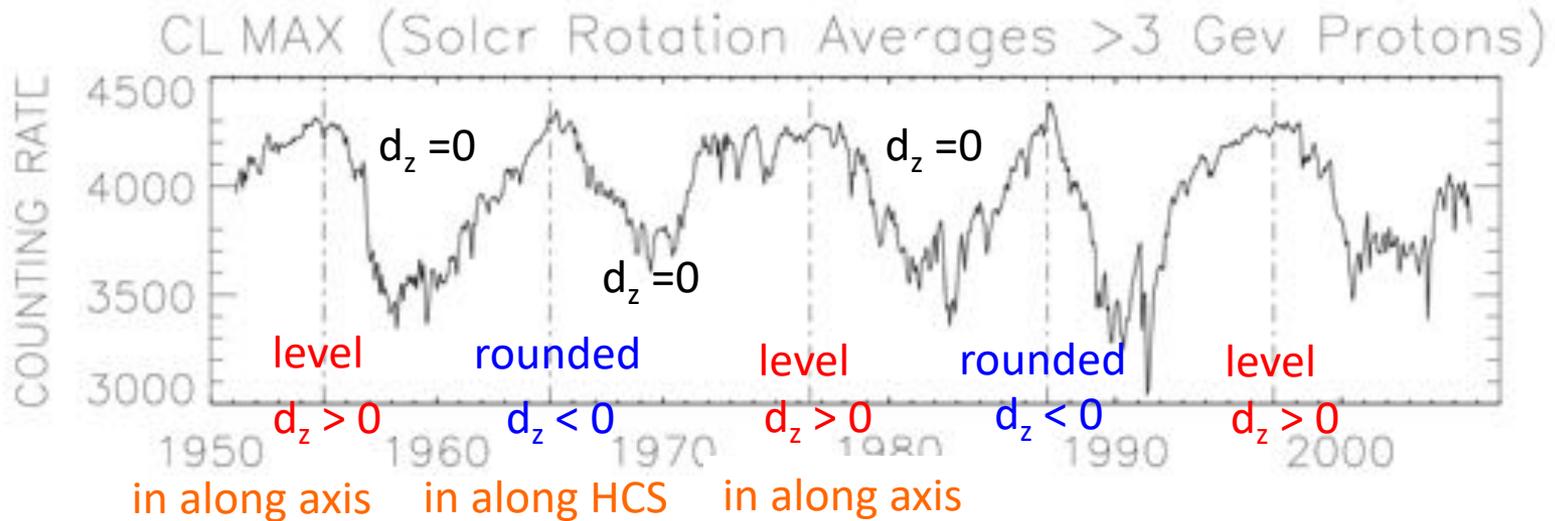
$$\approx \frac{2pcw}{3q} \frac{\mathbf{B}}{B^3} \times \nabla B$$



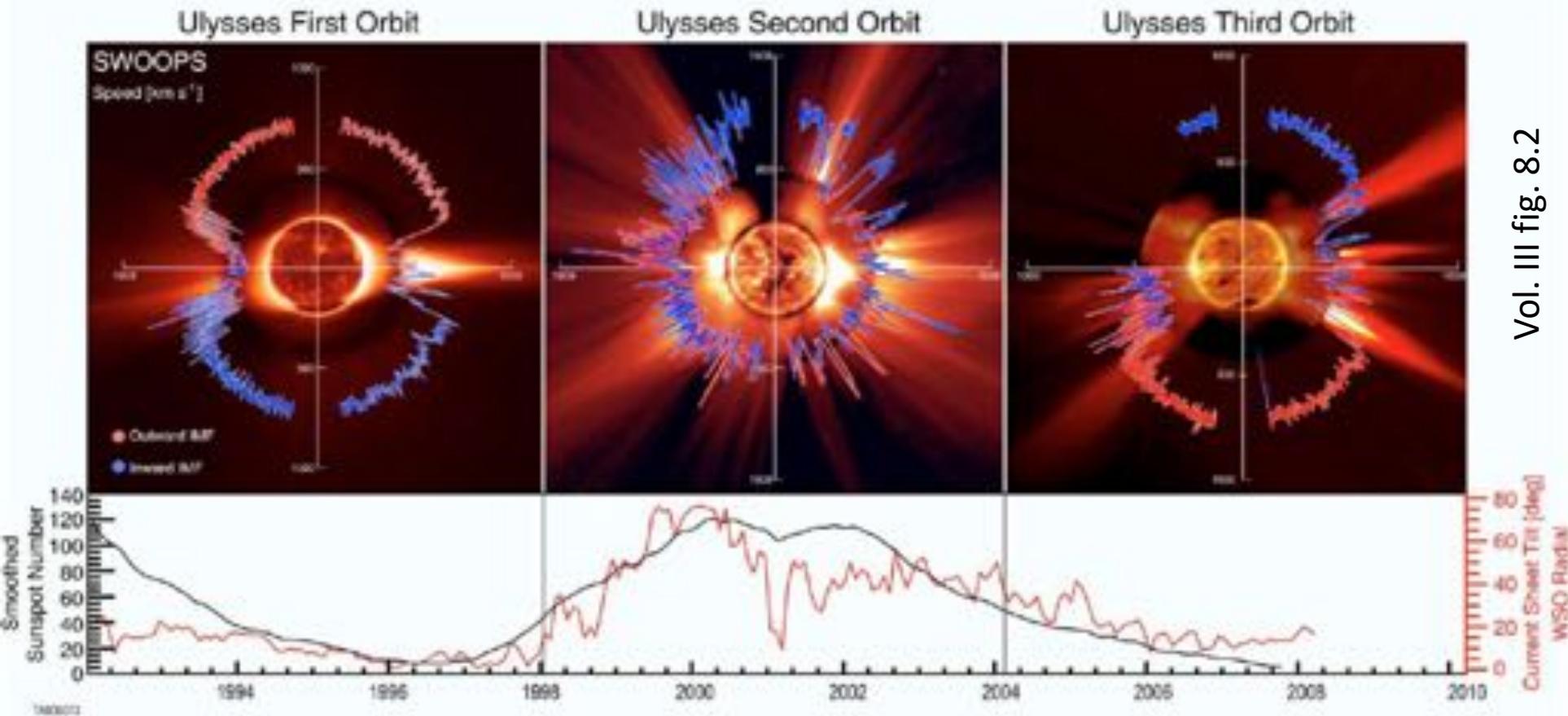
vol. III fig. 9.8



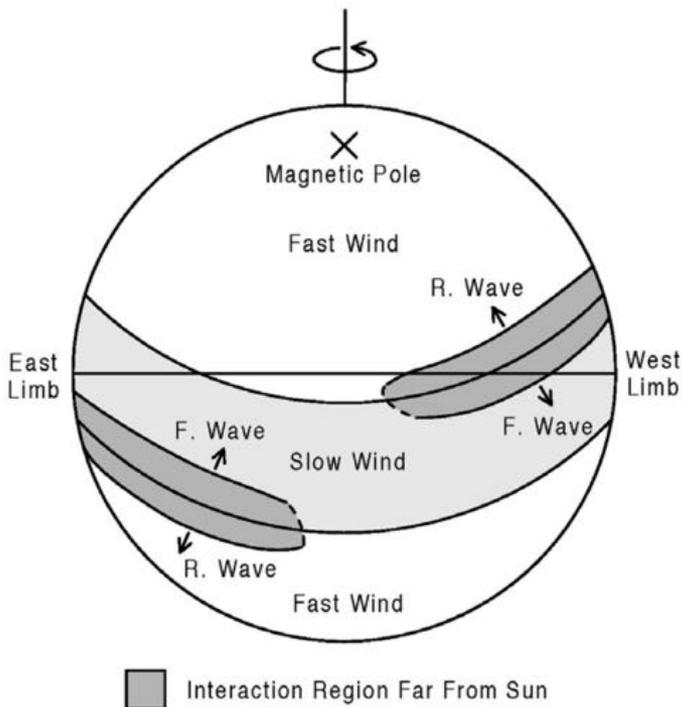
Effect on cosmic rays



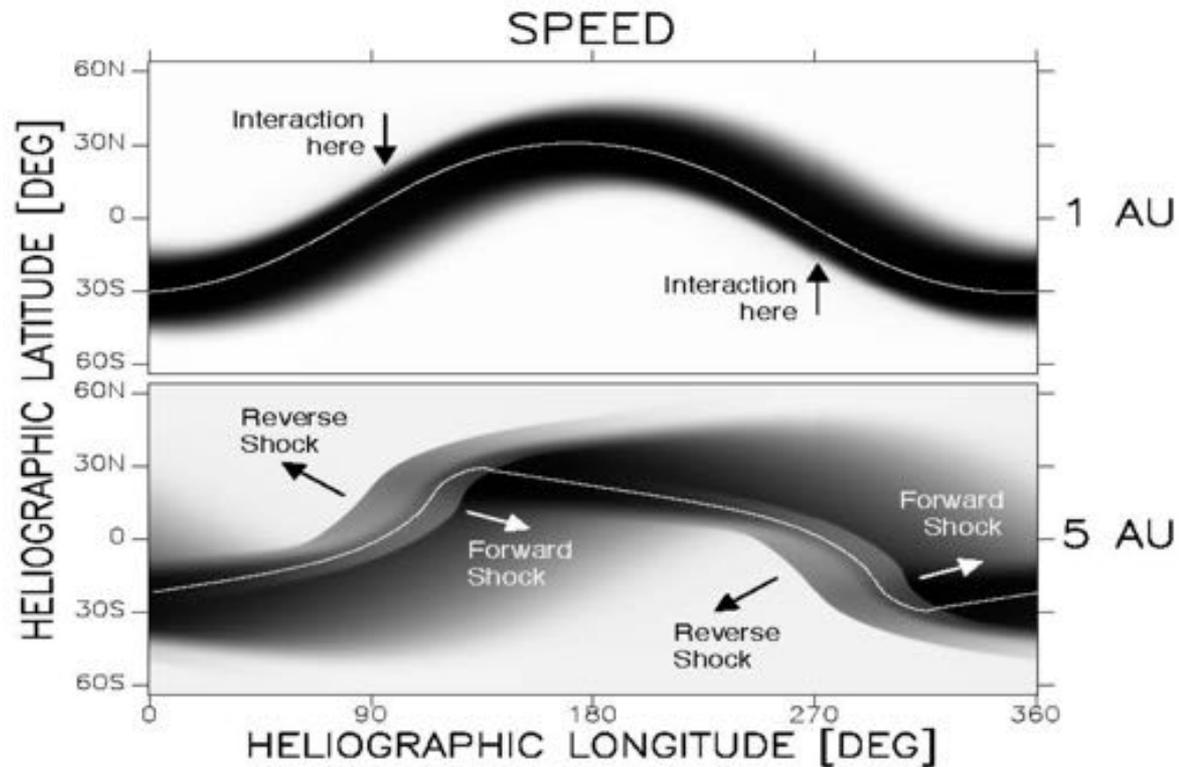
The wind through the cycle



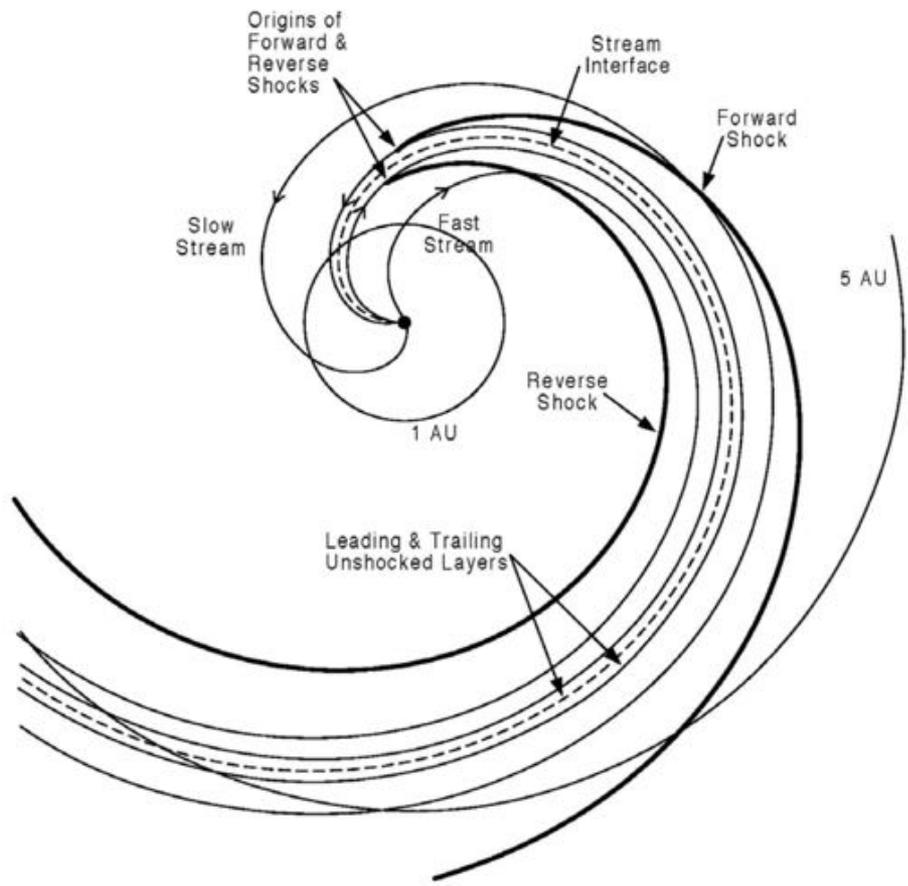
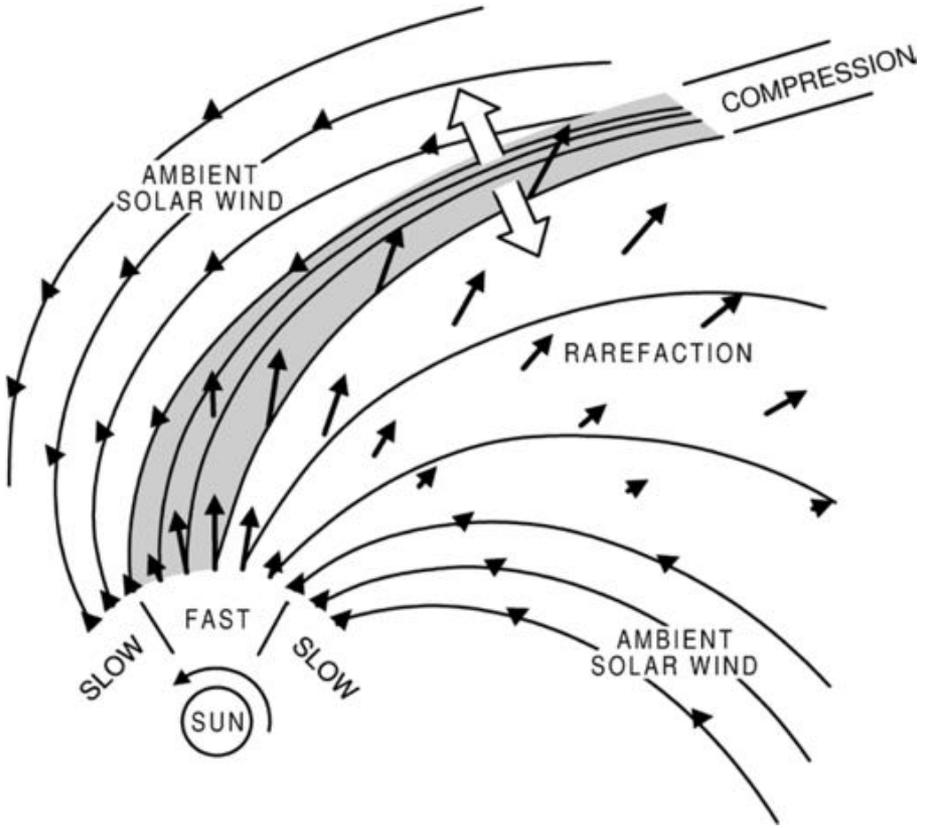
Effect of a "warped" HCS



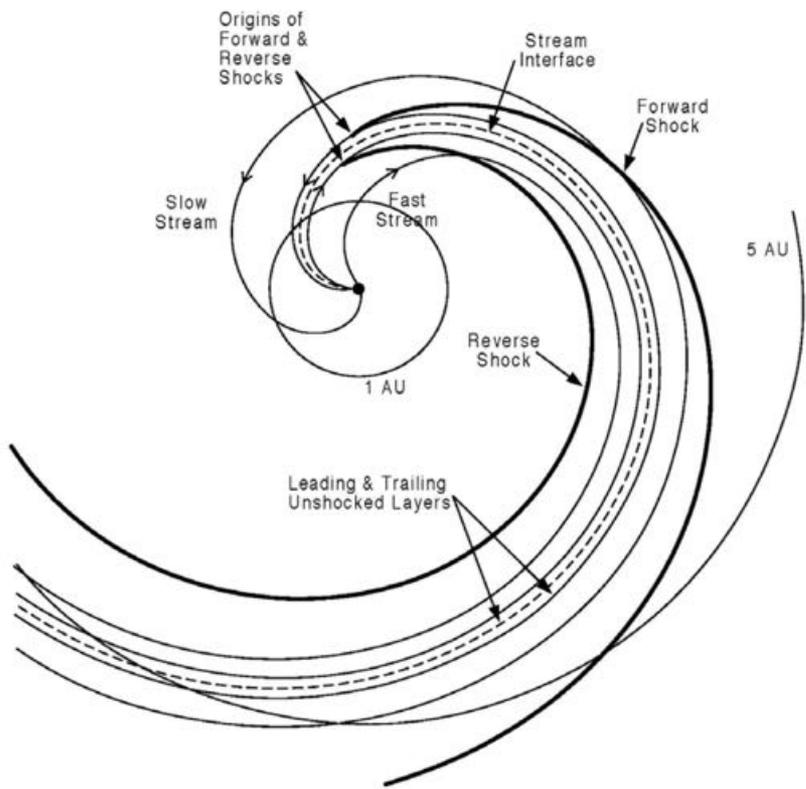
Vol. III fig. 8.6



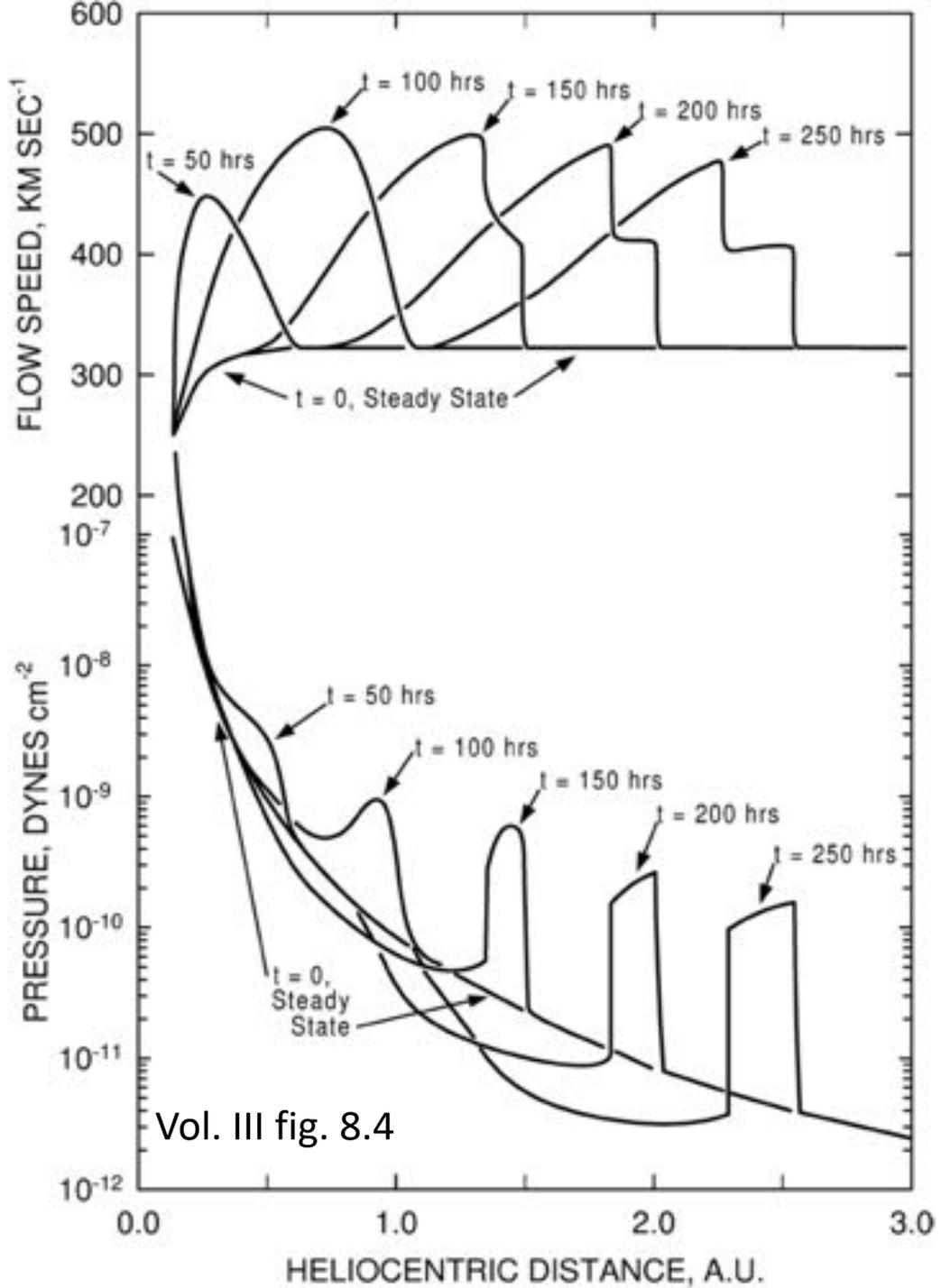
Vol. III fig. 8.7



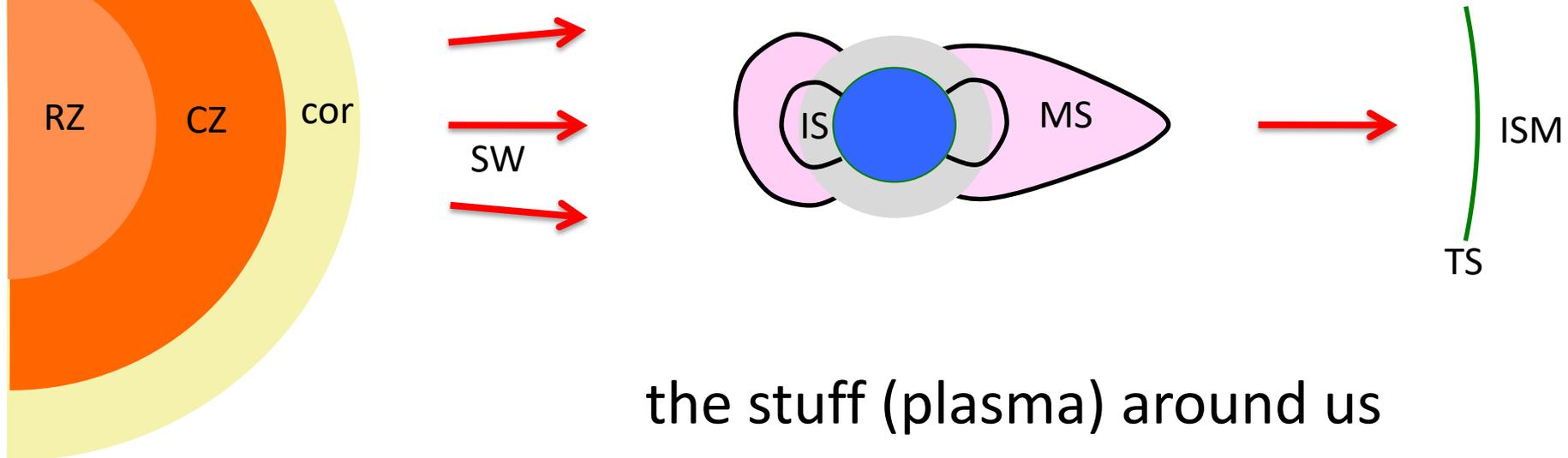
Vol. III fig. 8.5



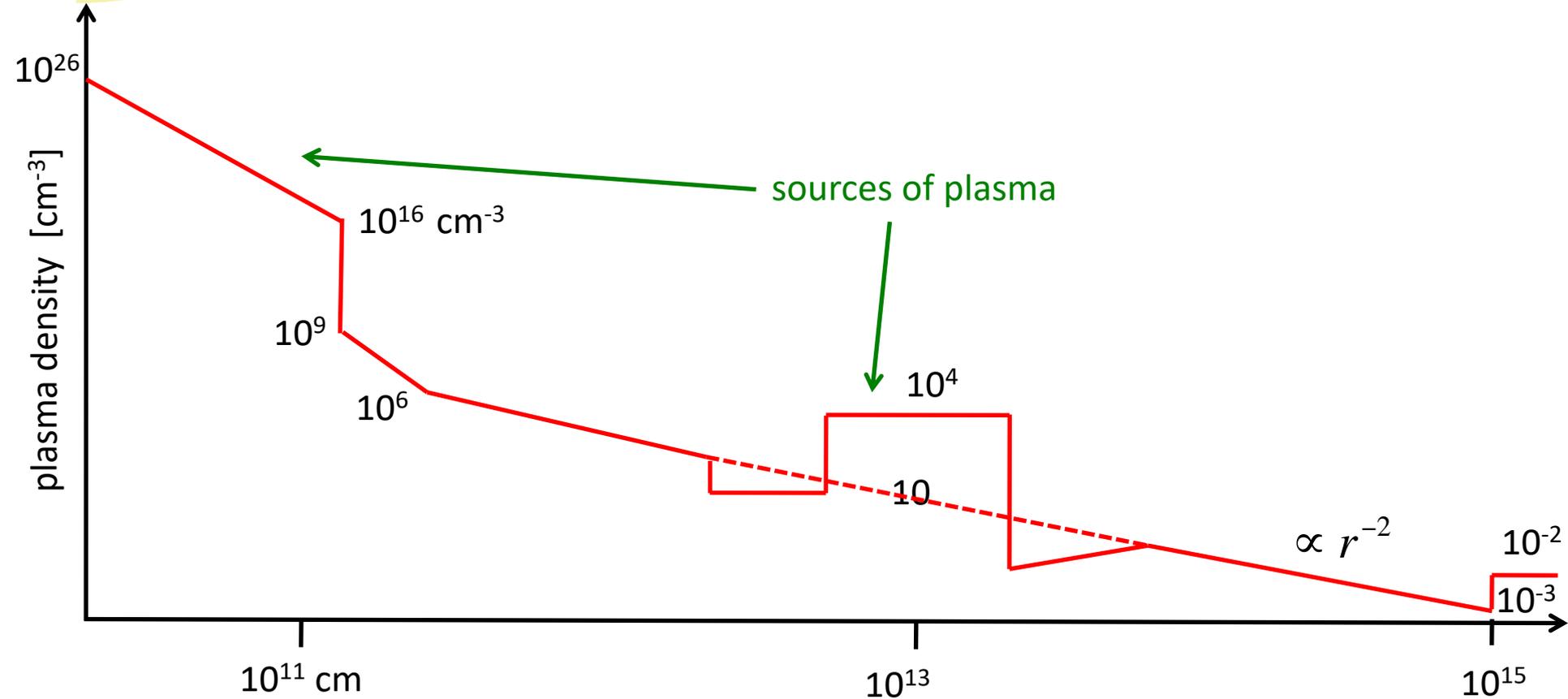
Vol. III fig. 8.5

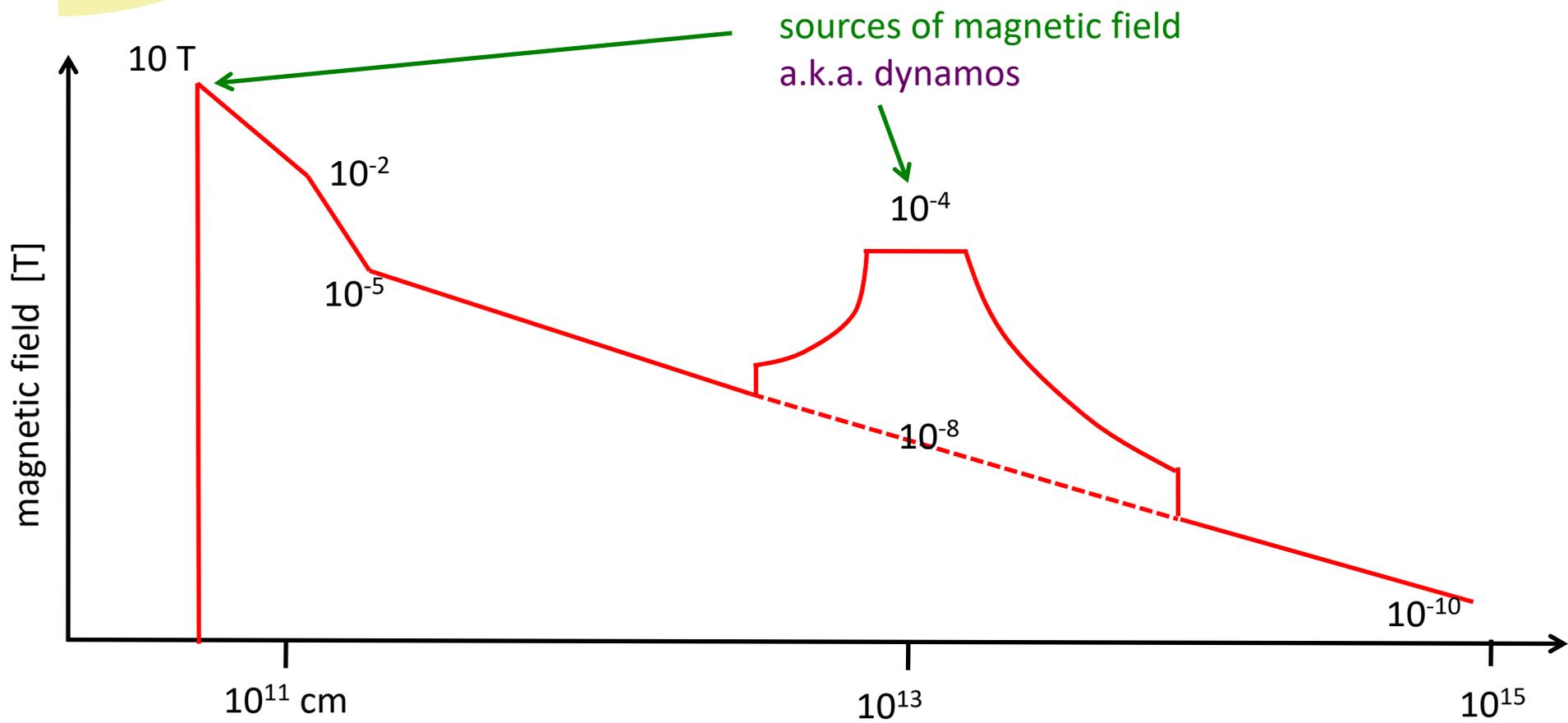
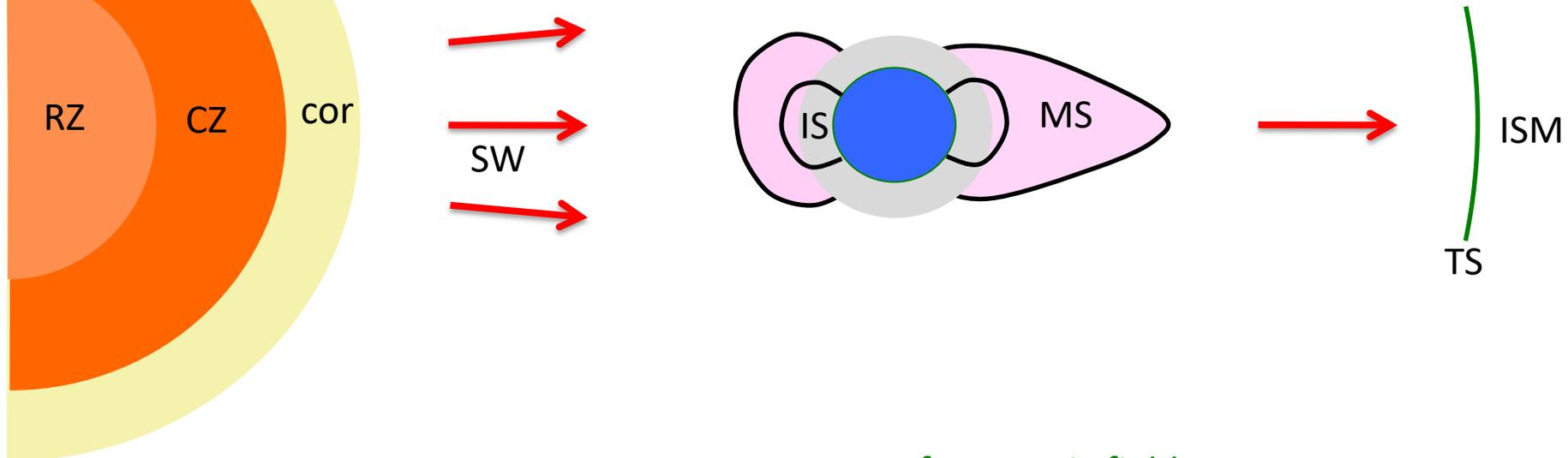


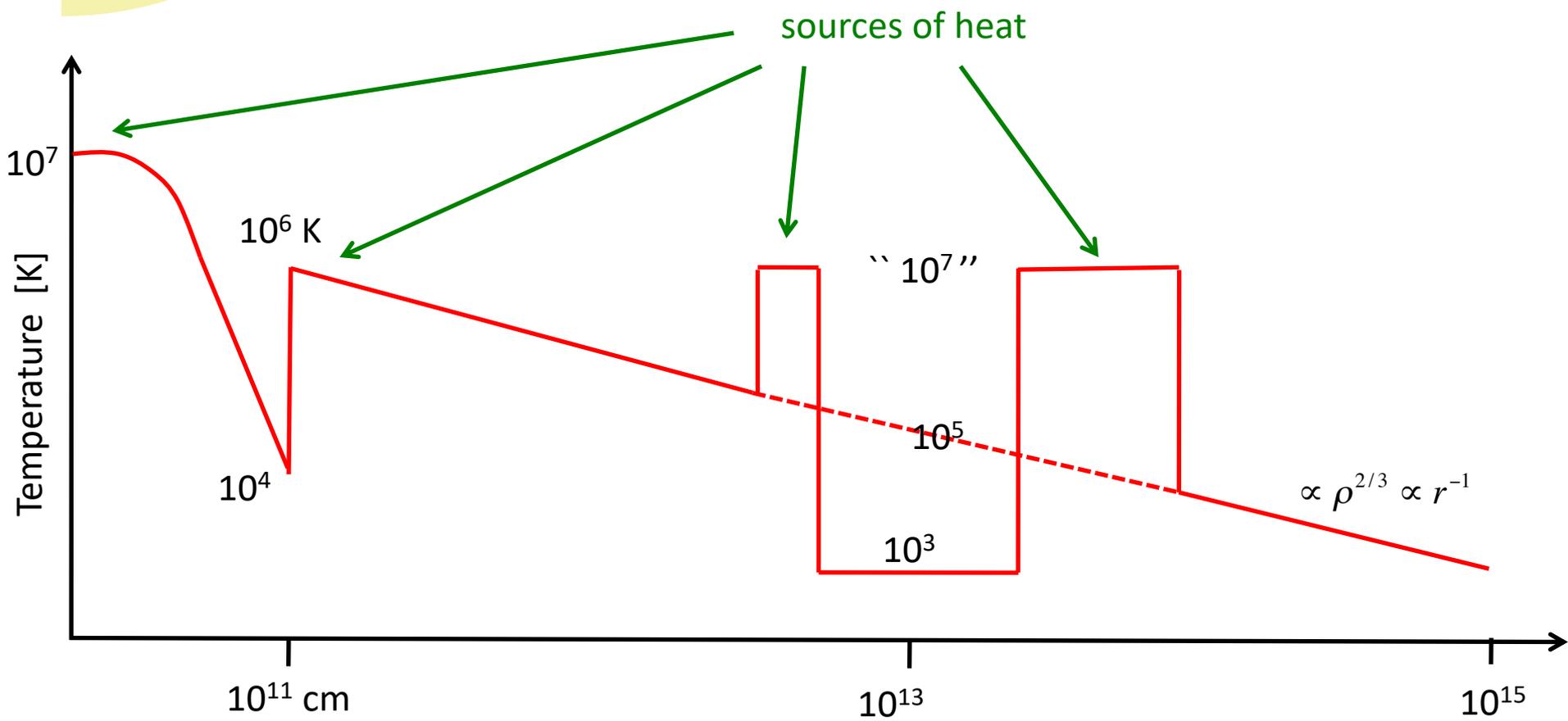
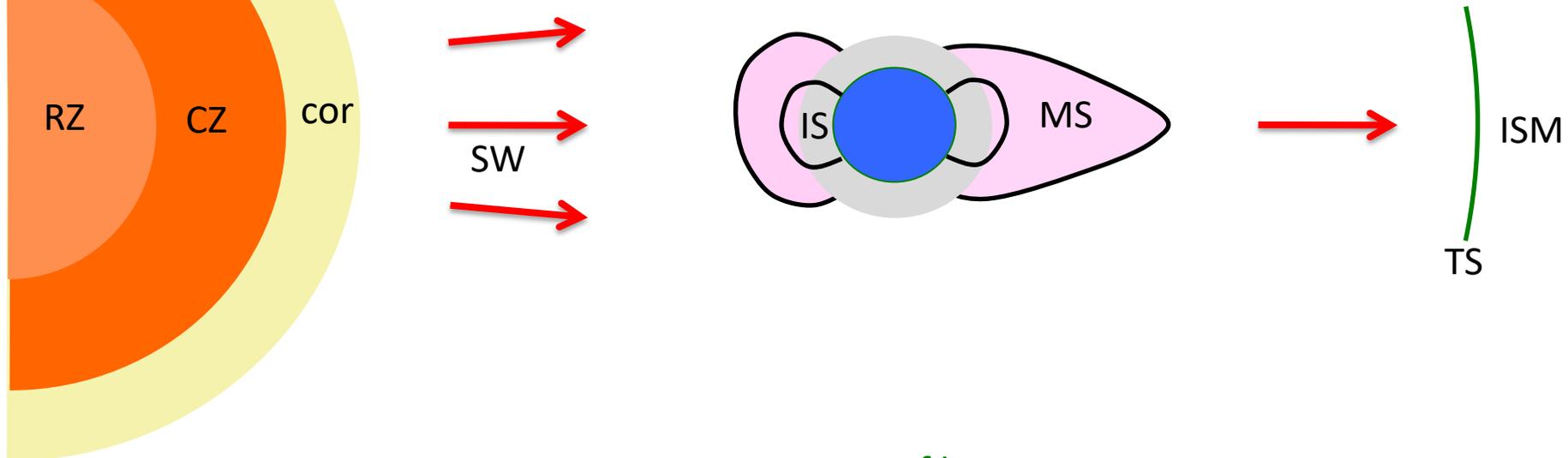
Vol. III fig. 8.4

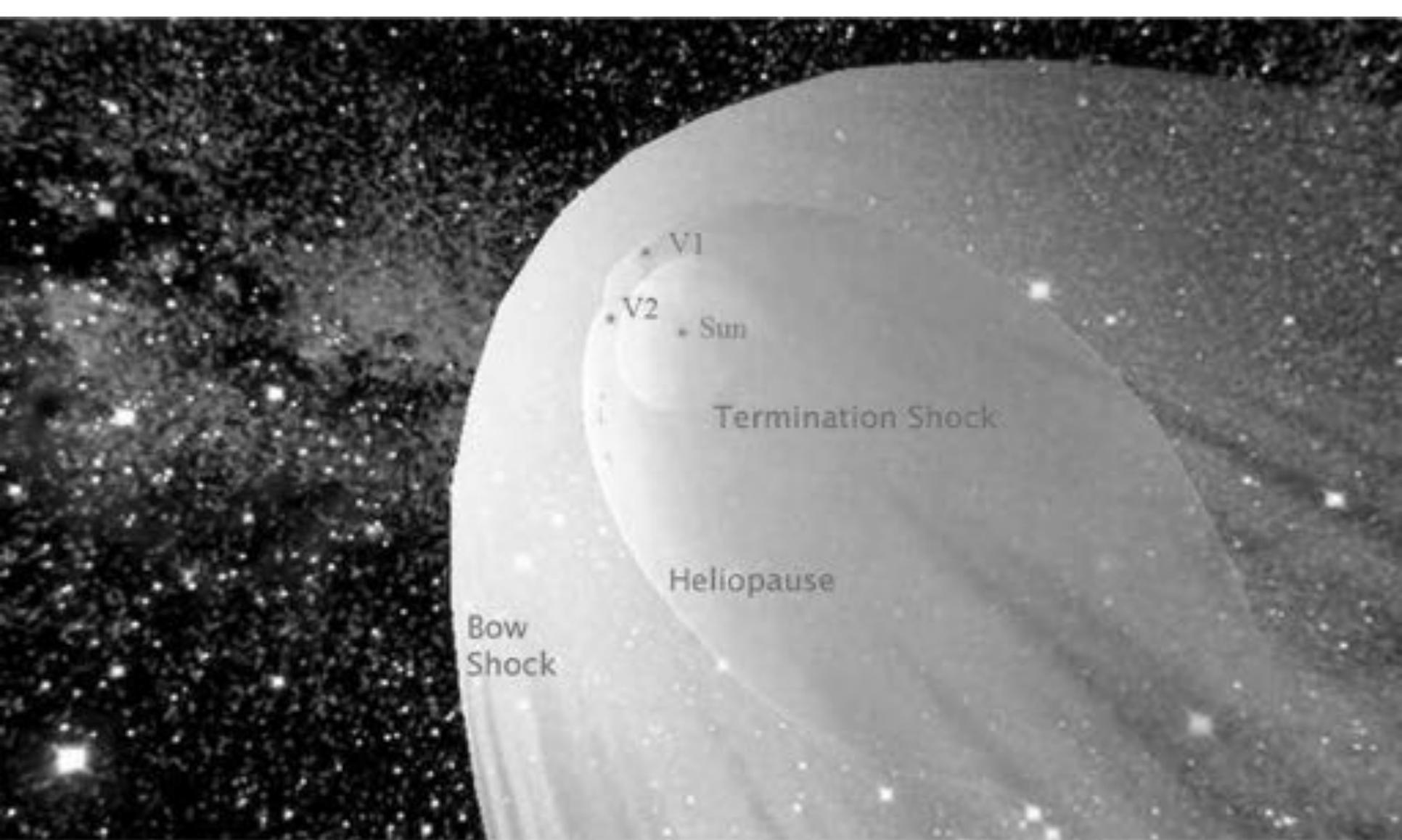


the stuff (plasma) around us









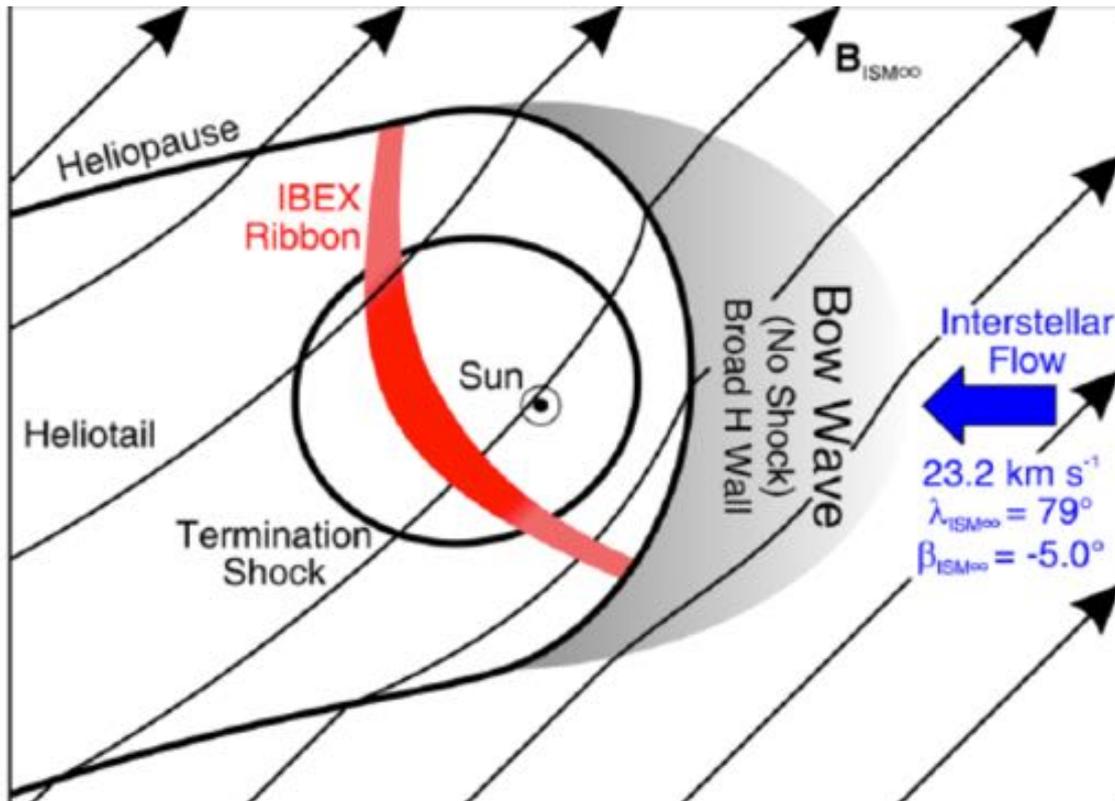
Vol. III fig. 9.1

The Heliosphere's Interstellar Interaction: No Bow Shock

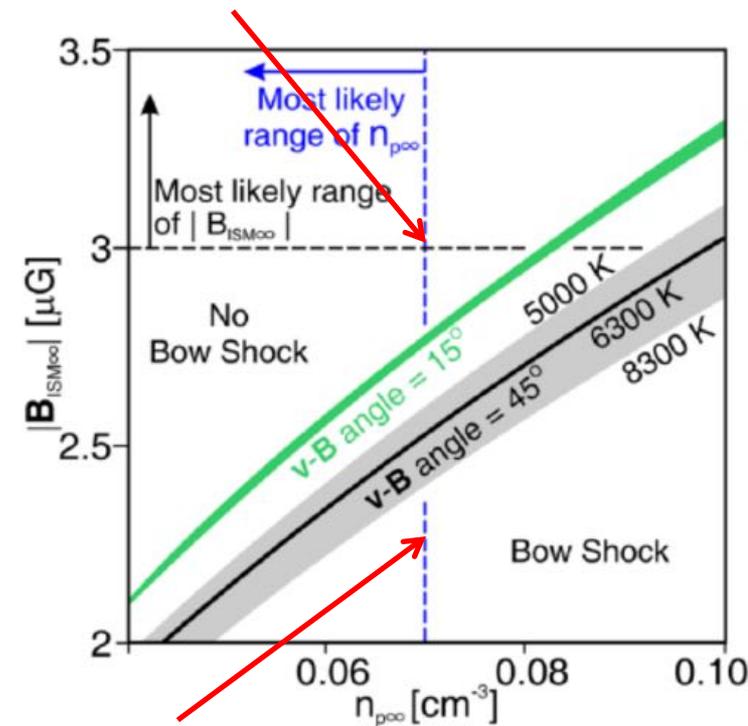
Science May 10, 2012

**Result
from
IBEX**

D. J. McComas,^{1,2*} D. Alexashov,³ M. Bzowski,⁴ H. Fahr,⁵ J. Heerikhuisen,⁶ V. Izmodenov,³ M. A. Lee,⁷ E. Möbius,^{7,8} N. Pogorelov,⁶ N. A. Schwadron,⁷ G. P. Zank⁶



$v_{fms} = 26.8 \text{ km/s}$



$v_{fms} = 21.4 \text{ km/s}$

Summary

- Corona: because there is heating – reaches high T because radiation cannot balance heating so conduction is needed
- More heat → higher density
- Wind: because there is heating – advective energy flux balances heating
- Creates heliosphere