To be continued…..

1. Neutrals vs Plasmas, Waves, Gravity, Why the Solar Wind is Supersonic

2. Solar Wind Origins and Acceleration and Solar and Stellar Winds and Magnetic Activity

Gravity, Angular Momentum -> Magnetic Fields

Sound Wave

$$\omega^2 = k^2 c_s^2$$

modified by gravity

$$\frac{\partial^2 \Delta\rho}{\partial t^2} - c_u^2 \frac{\partial^2 \Delta\rho}{\partial z^2} - \frac{c_u^2}{H}\frac{\partial \Delta\rho}{\partial z} = 0$$

$$\Rightarrow \qquad -\omega^2 = -c_u^2 k^2 + c_u^2 \frac{\mathrm{i}k}{H}$$

$$\Rightarrow \qquad \boxed{\omega^2 = c_u^2\left(k^2 - \frac{\mathrm{i}k}{H}\right)}$$

DISPERSION RELATION

$$k = \frac{\mathrm{i}}{2H} \pm \sqrt{\frac{\omega^2}{c_u^2} - \frac{1}{4H^2}}$$

$$\omega > c_u/2H \qquad \Delta\rho \propto \underbrace{e^{-z/2H}}\,\underbrace{e^{\mathrm{i}\left(\pm\sqrt{(\omega/c_u)^2-(1/2H)^2}\,z-\omega t\right)}}$$

$$\omega < c_u/2H$$

Wave damps

Internal Gravity Wave

$$\left(\frac{\partial}{\partial t} + \overline{u}\frac{\partial}{\partial x}\right)^2 \left(\frac{\partial^2 w'}{\partial x^2} + \frac{\partial^2 w'}{\partial z^2}\right) + \frac{g}{\overline{\theta}}\frac{\partial \overline{\theta}}{\partial z}\frac{\partial^2 w'}{\partial x^2} = 0$$

Square of Brunt-Väisälä frequency:
$\mathcal{N}^2$ assume to be constant

$$\left(\frac{\partial}{\partial t}+\overline{u}\frac{\partial}{\partial x}\right)^2\left(\frac{\partial^2 w'}{\partial x^2}+\frac{\partial^2 w'}{\partial z^2}\right)+\mathcal{N}^2\frac{\partial^2 w'}{\partial x^2}=0$$

Consider **wave-like solutions**:

$$\hat{w}=w_r+iw_i \quad m=m_r+im_i \quad \phi=kx+mz-\nu t$$

$$\begin{aligned} w' &= \mathrm{Re}\left[\hat{w}\exp(i\phi)\right] \\ &= \mathrm{Re}\left[(w_r+iw_i)\exp(i(kx+m_r z-\nu t))\exp(-m_i z)\right] \\ &= \left[w_r\cos(\mathrm{Re}(\phi))-w_i\sin(\mathrm{Re}(\phi))\right]\exp(-m_i z) \end{aligned}$$

Horizontal wavenumber k is real, solution is always sinusoidal

Insert $w' = \mathrm{Re}\left[\hat{w}\exp(i\phi)\right]$

into $$\left(\frac{\partial}{\partial t} + \overline{u}\frac{\partial}{\partial x}\right)^2 \left(\frac{\partial^2 w'}{\partial x^2} + \frac{\partial^2 w'}{\partial z^2}\right) + \mathcal{N}^2 \frac{\partial^2 w'}{\partial x^2} = 0$$

IGW Dispersion Relation

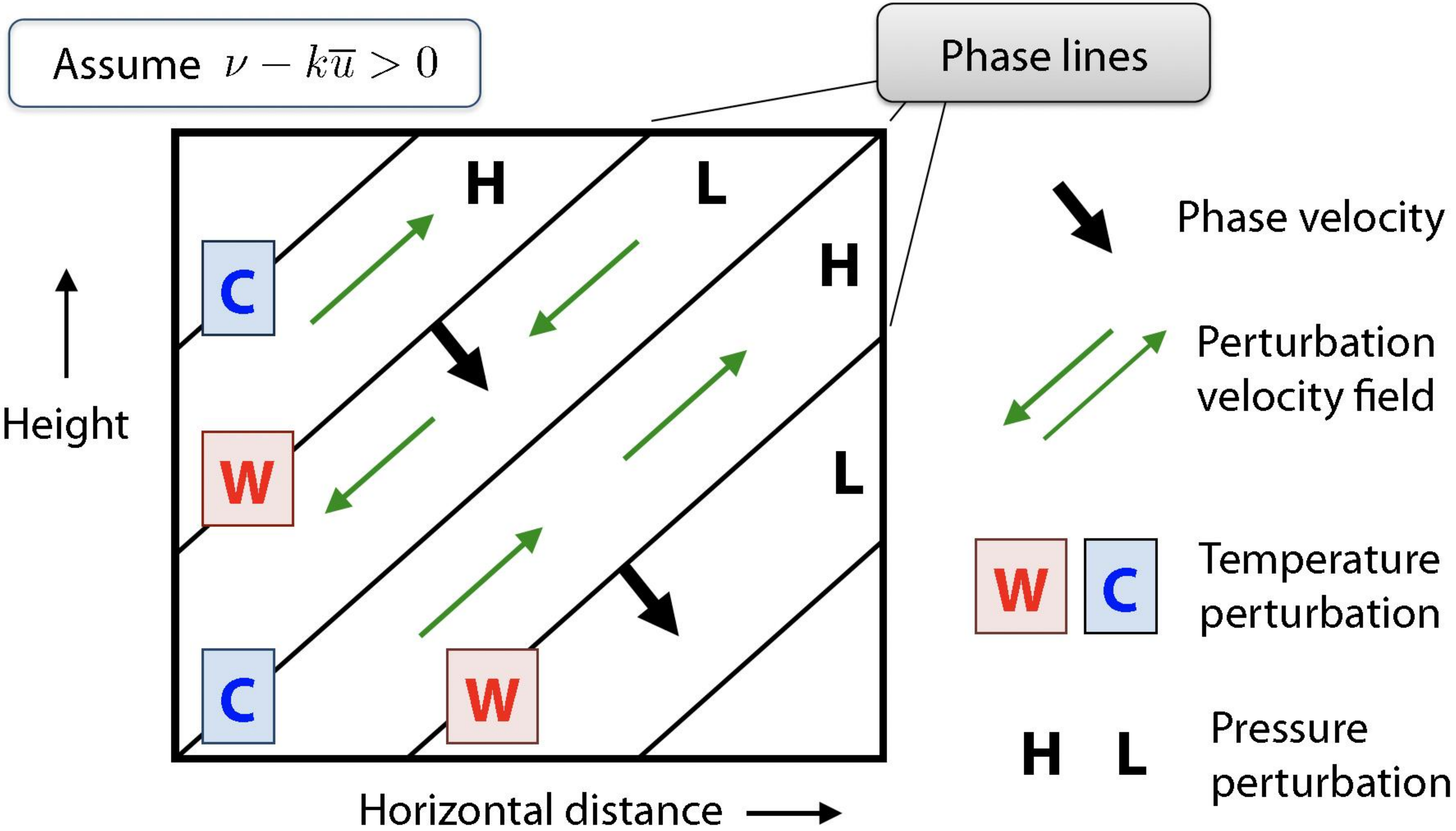
$$(\nu - \overline{u}k)^2(k^2 + m^2) - \mathcal{N}^2 k^2 = 0$$

IGW Frequency

$$\nu = \overline{u}k \pm \frac{\mathcal{N}k}{\sqrt{k^2 + m^2}} = \overline{u}k \pm \frac{\mathcal{N}k}{\kappa}$$

If we let $k > 0$ and $m < 0$, then lines of constant phase $\phi = (kx + mz)$ tilt eastward with increasing height

Assume $\nu - k\overline{u} > 0$



The zonal and vertical **phase velocities** are

$$c_x = \frac{\nu}{k} = \overline{u} \pm \frac{\mathcal{N}}{\sqrt{k^2 + m^2}}$$

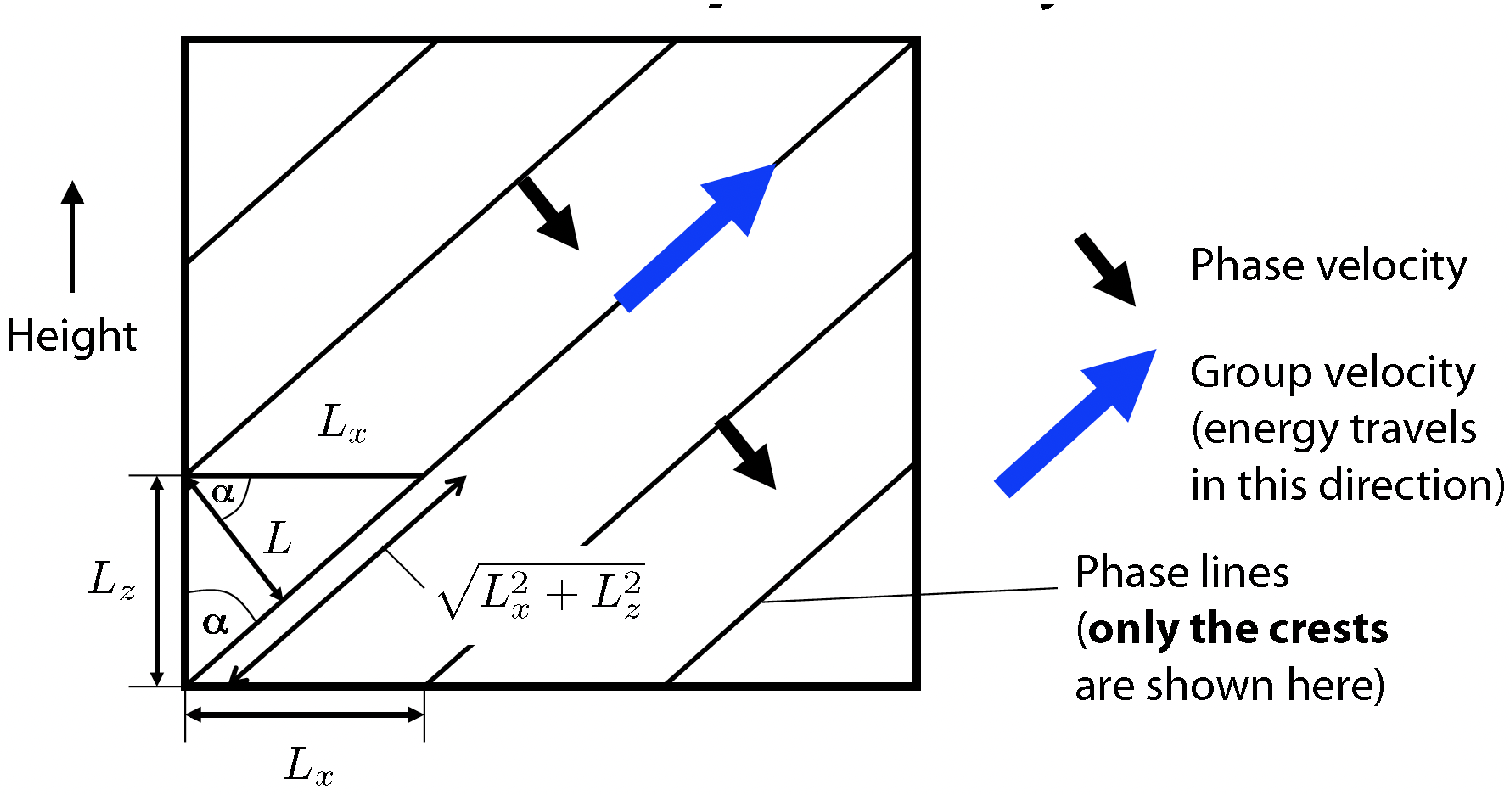
$$c_z = \frac{\nu}{m} = \frac{\overline{u}k}{m} \pm \frac{\mathcal{N}k}{m\sqrt{k^2 + m^2}}$$

The components of the **group velocity** are

$$c_{g,x} = \frac{\partial \nu}{\partial k} = \overline{u} \pm \frac{\mathcal{N}m^2}{(k^2 + m^2)^{3/2}}$$

$$c_{g,z} = \frac{\partial \nu}{\partial m} = \mp \frac{\mathcal{N}km}{(k^2 + m^2)^{3/2}}$$

Upper and lower signs chosen as above.



Angle of phase lines to the local vertical:

$$\cos\alpha = \pm\frac{L}{L_x} = \pm\frac{L_z}{\sqrt{L_x^2 + L_z^2}} = \pm\frac{\left(\frac{2\pi}{m}\right)}{\sqrt{\left(\frac{2\pi}{k}\right)^2 + \left(\frac{2\pi}{m}\right)^2}} = \pm\frac{k}{\sqrt{k^2 + m^2}} = \pm\frac{k}{\kappa}$$

FLUID THEORIES

$$\frac{\partial f}{\partial t} + \vec{\nabla} \cdot (f\vec{v}) + \vec{\nabla}_{\vec{v}} \cdot (f\vec{a}) = 0$$

$$\frac{\partial f}{\partial t} + \vec{v} \cdot \vec{\nabla} f + \frac{\vec{F}}{m} \cdot \vec{\nabla}_{\vec{v}} f = 0.$$

$$\vec{F} = \vec{F}_{lent.var.} + \vec{F}_{coll} \qquad -\frac{\vec{F}_{coll}}{m} \cdot \vec{\nabla}_{\vec{v}} f = \left(\frac{\partial f}{\partial t}\right)_{coll}$$

$$\frac{\partial f}{\partial t} + \vec{v} \cdot \vec{\vec{\nabla}} f + \frac{\vec{F}}{m} \cdot \vec{\nabla}_{\vec{v}} f = \left(\frac{\partial f}{\partial t}\right)_{coll}$$

When is a plasma a plasma

$$\lambda_D = \left(\frac{kT}{4\pi n e^2}\right)^{1/2} \qquad N_D = \frac{4\pi}{3} n \lambda_D^3 \gg 1$$

Saha equation: the ionization of a hydrogen gas is essentially complete at temperatures of order 10^4 K, much less than the temperature corresponding to the ionization potential

$$T \simeq I/k \simeq 1.58 \times 10^5 \, K$$

Also important is that a plasma reaches 90% conductivity with an ionization degree of only 8%.

Collisions in a plasma

$$\frac{Z_1 Z_2 e^2}{b} \simeq \frac{3}{2} kT,$$

The collision cross-section will therefore be given by:

$$\sigma_c = \pi b^2 = \frac{4\pi Z_1^2 Z_2^2 e^4}{(3kT)^2},$$

and the collision frequency:

$$\nu_c = n\sigma_c v_T = \frac{4\pi Z_1^2 Z_2^2 e^4 n}{m^{1/2}(3kT)^{3/2}},$$

Thermal Conductivity

$$\kappa \sim v_T^2/\nu_c \sim T^{5/2}$$

Collisions are also the way through which a plasma thermalizes, i.e. through which a plasma containing particle populations with different temperatures reaches thermal equilibrium. In a collision, energy may be transferred from the particle of higher energy to the lower energy one. Consider then the case of populations of electrons and ions both out of thermodynamic equilibrium but with comparable energies. It may be shown that collisions lead to equilibrium among particles of the same species on a different timescale compared to that required for thermal equilibrium across species. For collision between identical particles, the characteristic timescale τ required to reach equilibrium is given by

$$\tau_{ee} \simeq (\nu_{ee})^{-1} \simeq \left(\frac{m_e}{m_i}\right)^{1/2} \tau_{ii}.$$

Thermal equilibrium across species implies collisions between electrons and ions: in one collision an electron can only lose a fraction of order (m_e/m_i) of its energy. Reaching thermal equilibrium therefore requires a time

$$\tau_{ei} \simeq \left(\frac{m_i}{m_e}\right)^{1/2} \tau_{ii} \simeq \left(\frac{m_i}{m_e}\right) \tau_{ee}.$$

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \, \vec{u}) = 0$$

MOMENTS

$$\rho \frac{du_i}{dt} = -\frac{\partial P_{ik}}{\partial x_k} + n \, F_i .$$

$$P_{ik} = P \, \delta_{ik} + \Pi_{ik} ,$$

$$\frac{\partial}{\partial t}\left(\tfrac{1}{2}\rho u^2 + \tfrac{3}{2}P\right) + \frac{\partial}{\partial x_k}\left(\tfrac{1}{2}\rho u^2 + \tfrac{3}{2}P\right)u_k + u_i \, P_{ik} + q_k]$$

$$\vec{q} = n \langle \vec{w} (\tfrac{1}{2} m w^2) \rangle$$

$$-n \, F_i u_i = \left(\frac{\partial}{\partial t} (n \langle \tfrac{1}{2} m v^2 \rangle) \right)_{coll} ,$$

$$\tfrac{3}{2} \rho^{5/3} \, \frac{d}{dt}\left(P \, \rho^{-5/3} \right) = -\Pi_{ik} \frac{\partial u_i}{\partial x_k} - \frac{\partial q_k}{\partial x_k} .$$

The generalized Ohm's law

$$E_i + \frac{1}{c}(\vec{U} \times \vec{B})_i - \frac{J_i}{\sigma} = \frac{m_e}{e^2 n_e}\left[\frac{\partial J_i}{\partial t} + \frac{\partial}{\partial x_k}\Big(J_i U_k + J_k U_i\Big)\right] +$$

$$+ \frac{1}{e n_e c}\left(\vec{J} \times \vec{B}\right)_i - \frac{1}{e n_e}\frac{\partial P^{(e)}_{ik}}{\partial x_k}$$

Let us now carry out a dimensional analysis by dividing all terms in color with the first term (a generic field) The frequency is defined as the inverse of the characteristic time scale and we define the sound speed

$$\omega \simeq \tau^{-1} \quad , \quad c_s \simeq \Big(P/\rho\Big)^{\frac{1}{2}}$$

$$1:1 : \Big(\omega/\omega_{pe}\Big)\Big(\nu_{ei}/\omega_{pe}\Big)\Big(c/\mathcal{U}\Big)^2 : \Big(\omega/\omega_{pe}\Big)\Big(\omega_{ce}/\omega_{pe}\Big)\Big(c/\mathcal{U}\Big)^2 :$$

$$\Big(\omega/\omega_{pe}\Big)^2\Big(c/\mathcal{U}\Big)^2 : \Big(\omega/\omega_{cp}\Big)^2\Big(c_s/\mathcal{U}\Big)^2 :$$

$$\omega_{pe} \qquad \omega_{ce}, \omega_{cp} \qquad \sigma = \frac{e^2 n_e}{m_e \nu_{ep}}$$

The electron plasma frequency, electron and proton cyclotron frequency and the collsion frequencies also appear. It follows that to neglect the terms in color boxes we require, for the inertial term in green:

$$\left(\omega/\omega_{pe}\right) \ll \mathcal{U}/c$$

For the hall term proportional to

$$\vec{J} \times \vec{B} \qquad \left(\omega\omega_{ce}/\omega_{pe}^2\right) \ll \left(\mathcal{U}/c\right)^2$$

This may also be written differently, taking into account that the Hall term may also be written in terms of the proton cyclotron frequency and the Alfven

$$\left[\frac{1}{en_e c}\left(\vec{J} \times \vec{B}\right)_i\right]\frac{c}{\mathcal{U}\mathcal{B}} = \omega\frac{cm_p}{e\mathcal{B}}\frac{\mathcal{B}^2}{n_e m_p}\frac{1}{\mathcal{U}^2} = \frac{\omega}{\omega_{ci}}\left(\frac{V_a}{U}\right)^2 \rightarrow \quad \frac{\omega}{\omega_{ci}} \ll \left(\frac{U}{V_a}\right)^2$$

While the electron pressure gradient term may be eliminated when

$$\left(\omega/\omega_{cp}\right) \ll \left(\mathcal{U}/c\right)^2$$

DYNAMICS OF THE INTERPLANETARY GAS AND MAGNETIC FIELDS*

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Received January 2, 1958

ABSTRACT

We consider the dynamical consequences of Biermann's suggestion that gas is often streaming outward in all directions from the sun with velocities of the order of 500–1500 km/sec. These velocities of 500 km/sec and more and the interplanetary densities of 500 ions/cm^3 (10^{14} gm/sec mass loss from the sun) follow from the hydrodynamic equations for a 3×10^6 ° K solar corona. It is suggested that the outward-streaming gas draws out the lines of force of the solar magnetic fields so that near the sun the field is very nearly in a radial direction. Plasma instabilities are expected to result in the thick shell of disordered field (10^{-5} gauss) inclosing the inner solar system, whose presence has already been inferred from cosmic-ray observations.

I. INTRODUCTION

Biermann (1951, 1952, 1957*a*) has pointed out that the observed motions of comet tails would seem to require gas streaming outward from the sun. He suggests that gas is often flowing radially outward in all directions from the sun with velocities ranging from 500 to 1500 km/sec; there is no indication that the gas ever has any inward motion. Biermann infers densities at the orbit of earth ranging from 500 hydrogen atoms/cm^3 on magnetically quiet days to perhaps 10^5/cm^3 during geomagnetic storms (Unsöld and Chapman 1949). The mass loss to the sun is 10^{14}–10^{15} gm/sec. It is the purpose of this paper to explore some of the grosser dynamic consequences of Biermann's conclusions.

For instance, we should like to understand what mechanism at the sun might conceivably be responsible for blowing away the required 10^{14}–10^{15} gm of hydrogen each second, with velocities of the order of 1000 km/sec. All known mechanisms, such as

How does a hot corona expand?

$$g_s = \frac{GM_\odot}{R_s^2} \quad r = \frac{R}{R_s} \quad \frac{\partial p}{\partial r} = -\frac{2m_p n g R_s}{r^2} \quad p = 2nkT$$

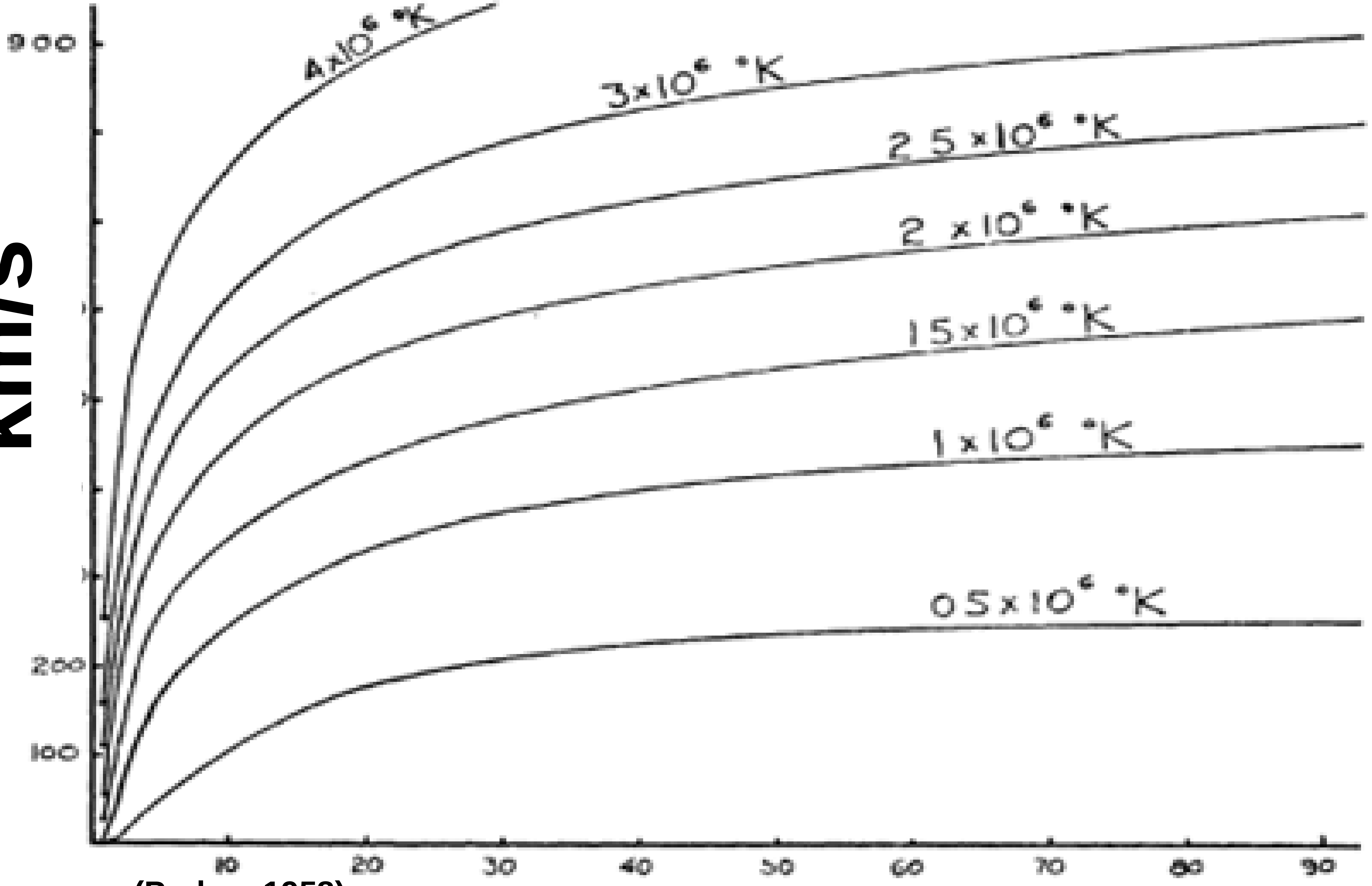
$$p(r) = p_0 \exp\left(-\int_1^r dr' \frac{m_p g_s R_s}{kT\, r^2}\right)$$

$T(r)$ falls slower than $1/r$ a finite pressure at infinity is required confine atmosphere. In a hot plasma atmosphere thermal conduction is proportional $k \sim T^{5/2}$ and therefore $T(r) \sim r^{-2/7}$

Since we know of no general pressure at infinity which could balance the $p(\infty)$ computed from equation (9) with the expected values of n, we conclude that probably it is not possible for the solar corona, or, indeed, perhaps the atmosphere of any star, to be in complete hydrostatic equilibrium out to large distances. We expect always to find some continued outward hydrodynamic expansion of gas—without considering the evaporation from the high-velocity tail of the Maxwellian distribution (Spitzer 1947; van de Hulst 1953).

Parker, 1958

wind sped
km/s



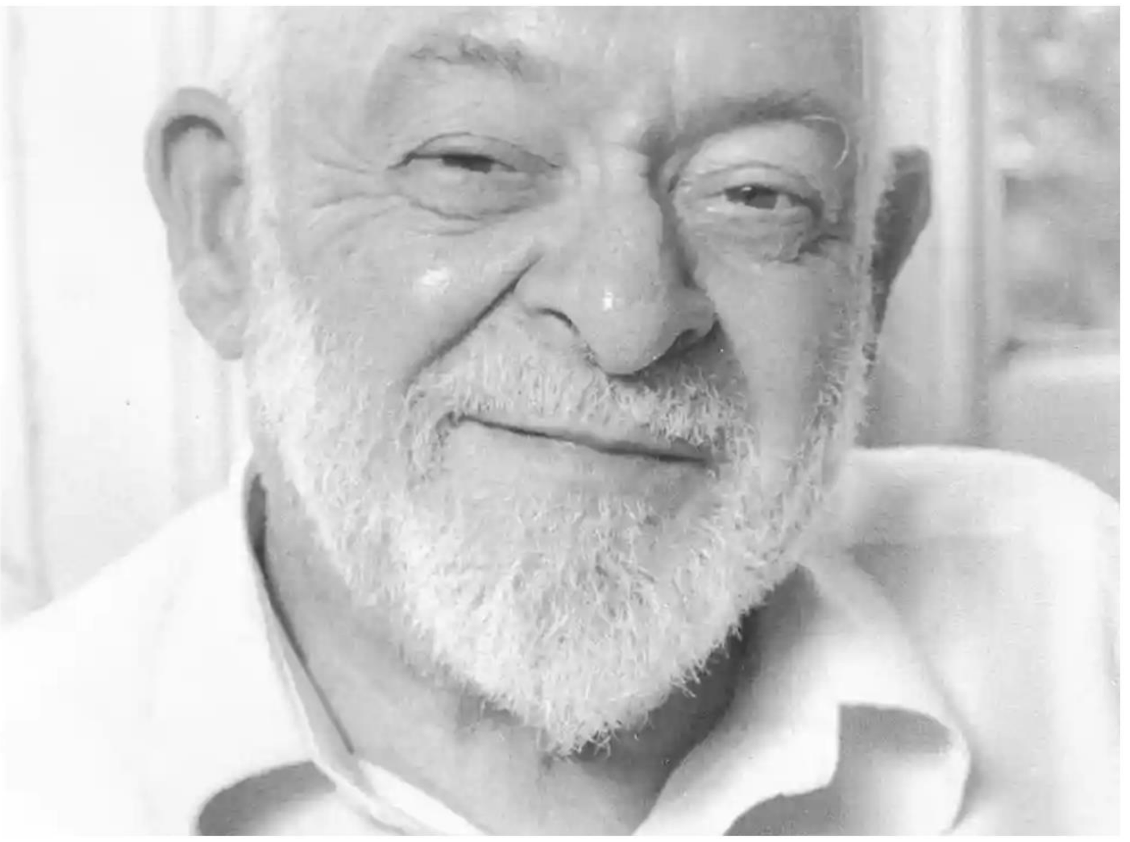
(Parker, 1958)

Distance to the Sun

- **Mestel**, *quoted in Roberts and Soward (1972)*: *"were the temperature at the base of the solar corona 10^5 K rather than the generally accepted 10^6 K the total pressure far from the sun would suffice to suppress the solar wind entirely"*

P_{ism} = 1.24 10^{-12} dyne/cm^2 confines a 10^5 K corona

Astronomer and astrophysicist who inspired generations of students and discovered the cooling law for white dwarf stars



Leon Mestel found that white dwarf stars – dead stars that are the endpoint of evolution of stars such as the sun – cooled over billions of years. Photograph: Cath Forrest

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Stellar winds and breezes

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Steady stellar winds are generally divided into two classes: (i) the winds proper, for which the energy flux per unit solid angle, E_∞, is non-zero, and (ii) the breezes, for which $E_\infty = 0$.

The breezes may be distinguished from one another by the value of the ratio, g, of kinetic to thermal energy of the particles in the limit of large distance, r, from the stellar centre, or more precisely by

$$g = \lim_{r\to\infty} \frac{mv^2}{kT},$$

where $v(r)$ is breeze velocity, $T(r)$ is temperature, m is mean particle mass, and k is the Boltzmann constant. Solutions have previously been obtained for values of g in the range $0 \leqslant g \leqslant 1$, in which the breezes are subsonic everywhere with respect to the isothermal speed of sound. It is demonstrated here that two distinct solutions exist as $g \to \frac{5}{3}$, namely (in an obvious notation) the $g = \frac{5}{3}-$ and the $g = \frac{5}{3}+$ possibilities. It is shown that, if $g > \frac{5}{3}$ ($g < \frac{5}{3}$) the solutions are everywhere supersonic (subsonic) with respect to the adiabatic speed of sound. If $1 < g < \frac{5}{3}$, they possess a critical point, at which the isothermal speed of sound and the flow speed coincide.

The winds are examined in the limit $E_\infty \to 0$, and the relation with the breezes is studied. In particular, it is shown that, for $r \leqslant O(E_\infty^{-2/5})$, the winds satisfy the stellar breeze equations to leading order, and possess a critical point at $r = O(1)$. For $r > O(E_\infty^{-2/5})$, the solutions do not obey the breeze equations. They ultimately follow the Durney asymptotic law [$T = O(r^{-4/3})$, for $r \to \infty$] for the winds. This demonstration of how the winds merge continuously into the breezes as $E_\infty \to 0$ is new.

The question of how the particle density (N_0) and temperature (T_0) at the base of the stellar corona determine the type of solution realized outside the star is examined. Even when the flow speed, v_0, at the base of the corona is subsonic, non-uniqueness can occur. In one domain of the (N_0, T_0) plane, two distinct types of breeze are possible; in another these, together with a wind ($E_\infty \neq 0$), are permissible. Elsewhere (large N_0, moderate T_0) only a unique breeze exists or (small N_0 and/or T_0) a unique wind. In some domains (large T_0) no steady solution exists, unless the requirement that the corona is subsonic is relaxed. In this case, however, the problems of non-uniqueness are severely aggravated.

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‡ The National Center for Atmospheric Research is sponsored by the National Science Foundation.
§ National Oceanic and Atmospheric Administration/University of Colorado.

Stationary, spherically symmetric flows, isothermal approximation, sound speed c, $\gamma = 1$ ($r = R/R_s$)

$$\rho U r^2 = F_m \qquad p = c^2 \rho$$

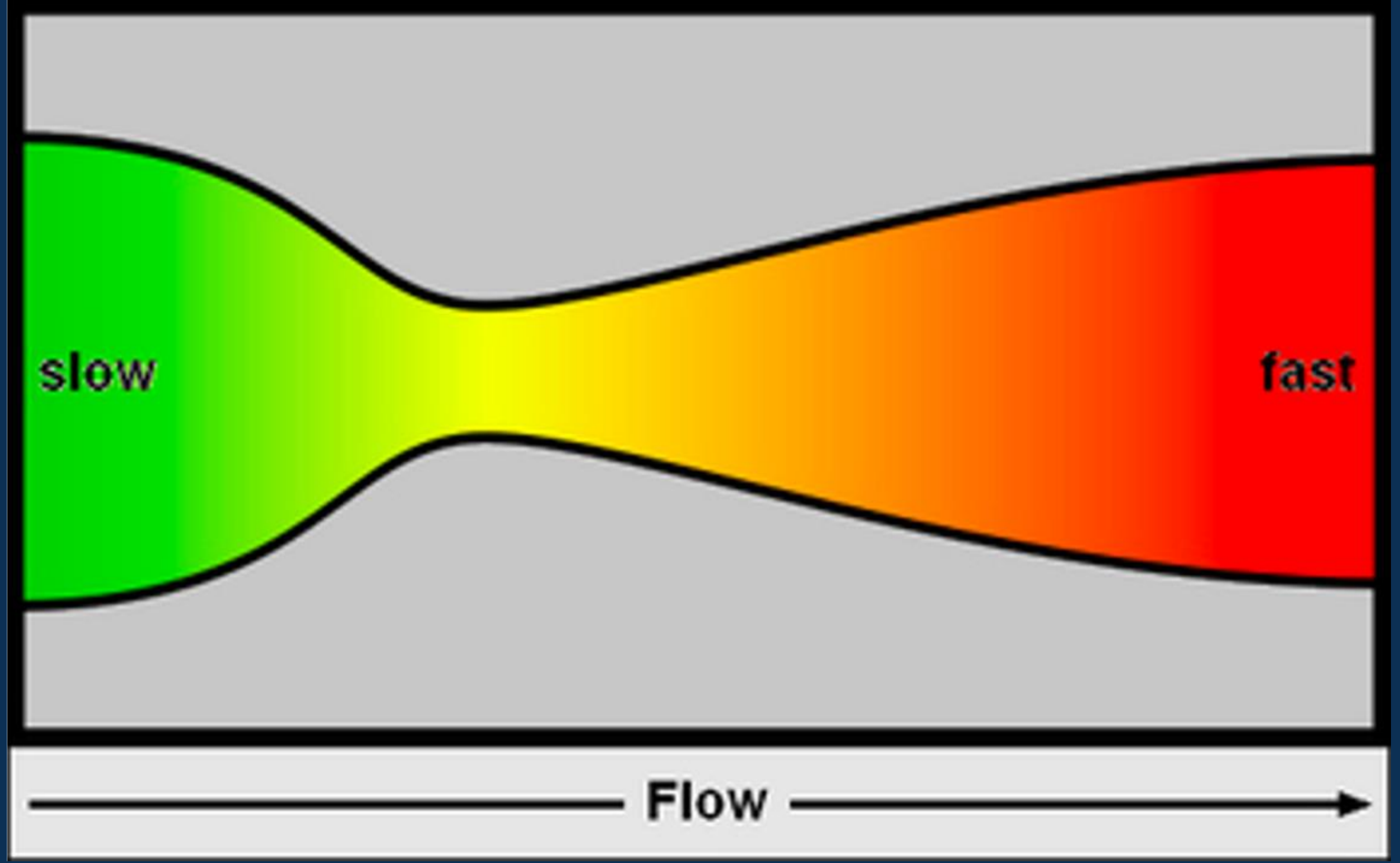
$$U \frac{\partial U}{\partial r} = -\frac{1}{\rho}\frac{\partial p}{\partial r} - \frac{g R_s}{r^2}$$

Introducing the Mach number $M = U/c$

$$\left(M - \frac{1}{M} \right) M' = \frac{2}{r} - \frac{g R_s}{r^2 c^2}$$

$$\frac{1}{2}\left(M^2 - M_0^2 \right) - \log\left(\frac{M}{M_0} \right) = 2 \log r + \frac{g R_s}{c^2}\left(-1 + \frac{1}{r} \right)$$

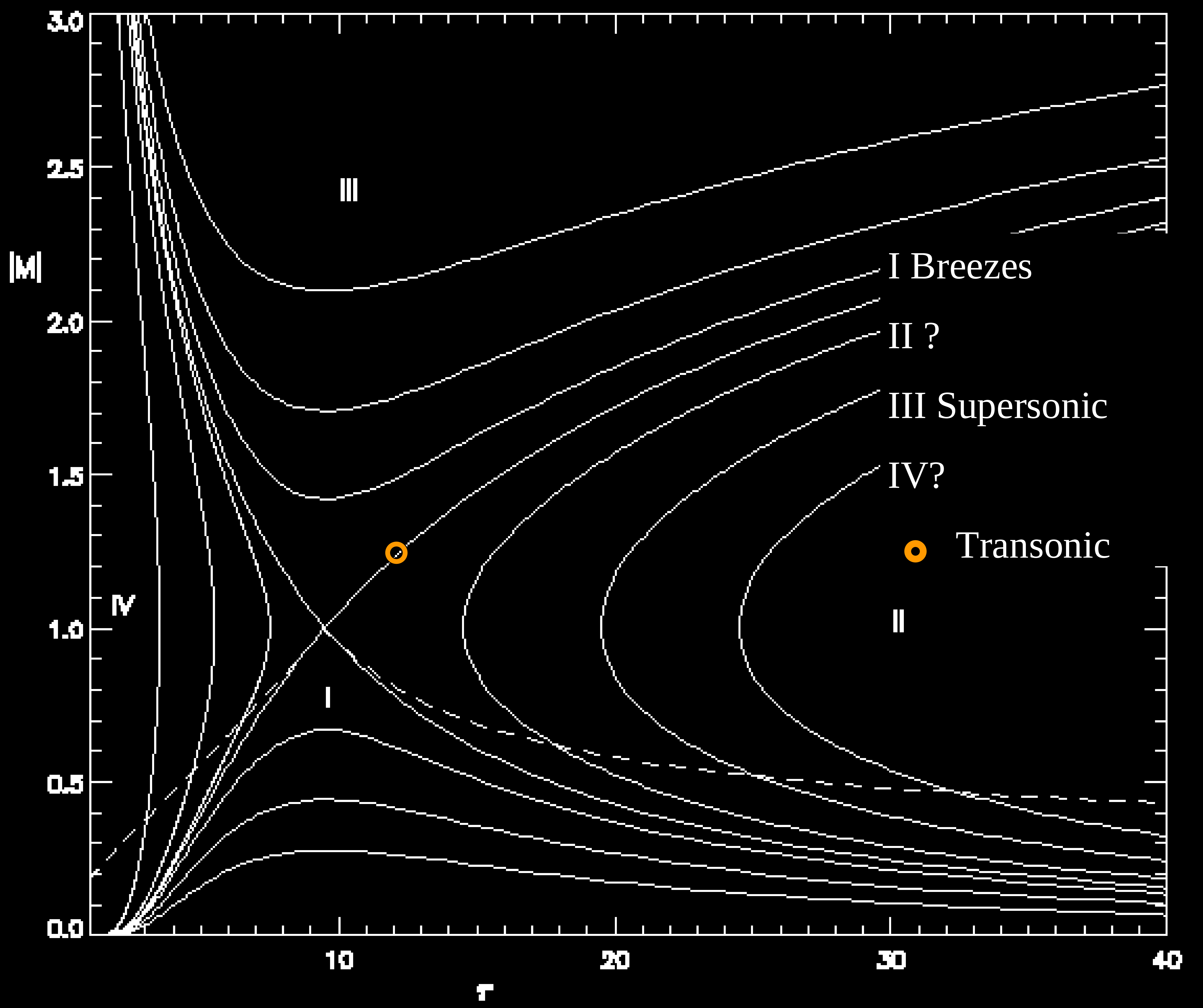
$$\frac{1}{2}\left(M^2 - M_0^2 \right) + \log\left(\frac{p}{p_0} \right) = \frac{g R_s}{c^2}\left(-1 + \frac{1}{r} \right)$$



$$(U - \frac{V_T^2}{U})\frac{dU}{dr} = \frac{V_T^2}{A}\frac{dA}{dr} - \frac{V_g^2}{2}\frac{1}{r^2}$$

$$\frac{1}{2}\left(M^2 - M_0^2\right) - \log\left(\frac{M}{M_0}\right) = 2\log r + \frac{gR_s}{c^2}\left(-1+\frac{1}{r}\right)$$

$$\frac{1}{2}\left(M^2 - M_0^2\right) + \log\left(\frac{p}{p_0}\right) = \frac{gR_s}{c^2}\left(-1+\frac{1}{r}\right)$$



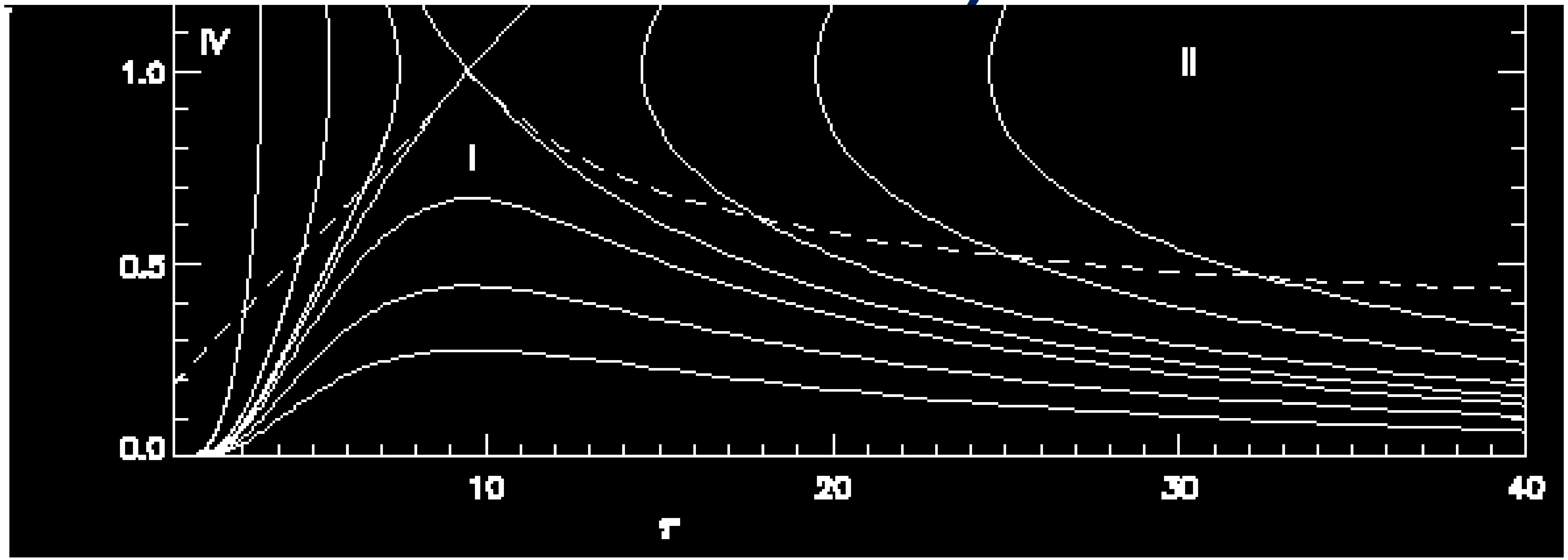
Pressure as a function of distance from the star

$$p = p_0 \exp((M_0^2 - M^2)/2 - gR_s / c^2)$$

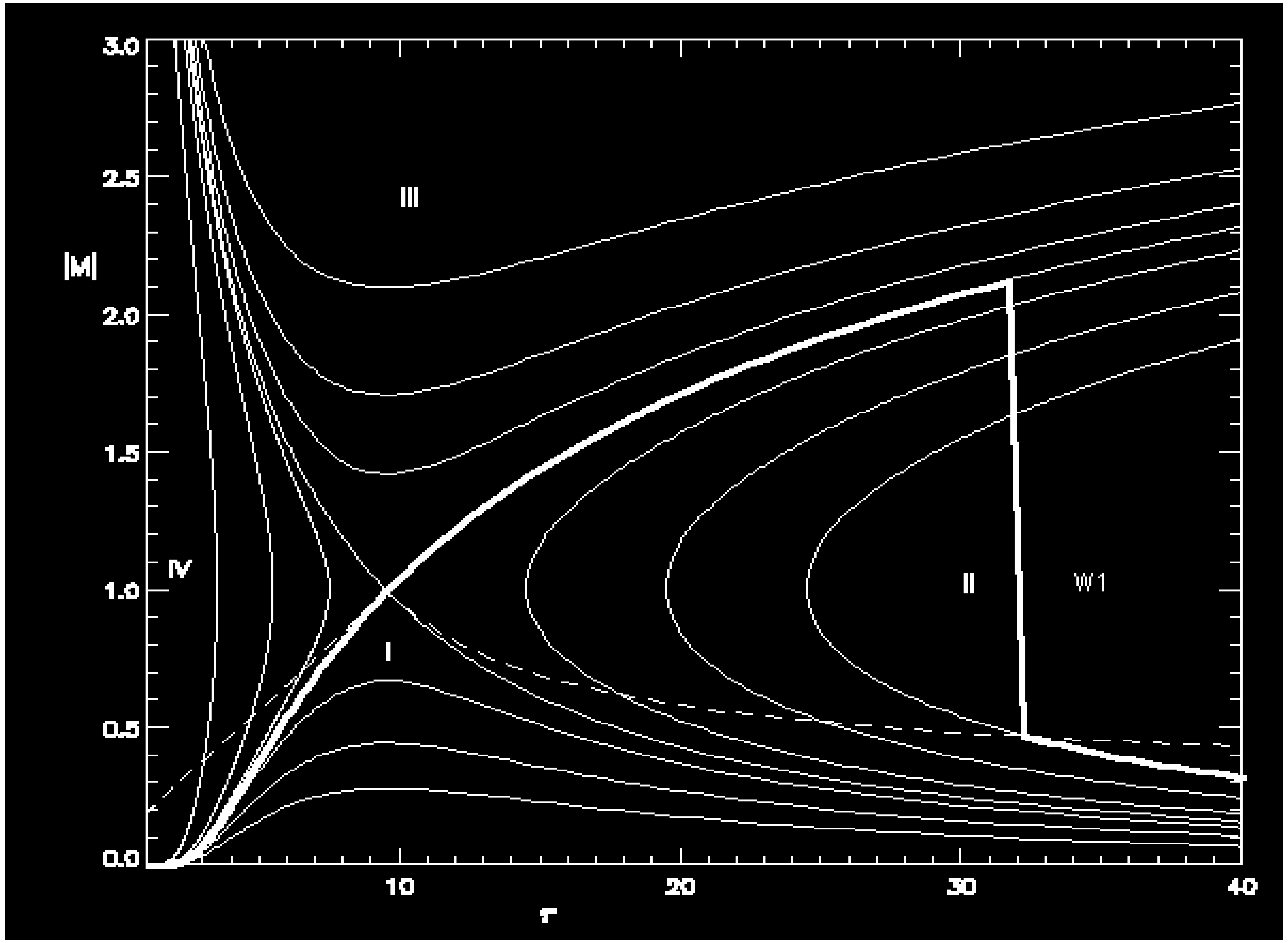
Goes to zero for transonic, for breezes varies from:

$$p_{stat} = p_0 \exp(- gR_s / c^2)$$ **STATIC**

$$p_{crit} = p_0 \exp(M_*^2 / 2 - gR_s / c^2)$$ **CRITICAL BREEZE (upward + downward transonic)**



Among flows which are subsonic at the atmospheric base the accelerating transonic has the special property that density and pressure tend to zero at large distances: because of the small but finite values of the pressure of the ambient external medium a terminal shock transition connecting to the lower branch of the double valued solutions filling region II will in general be present (McCrea 1956, Holzer and Axford 1970)



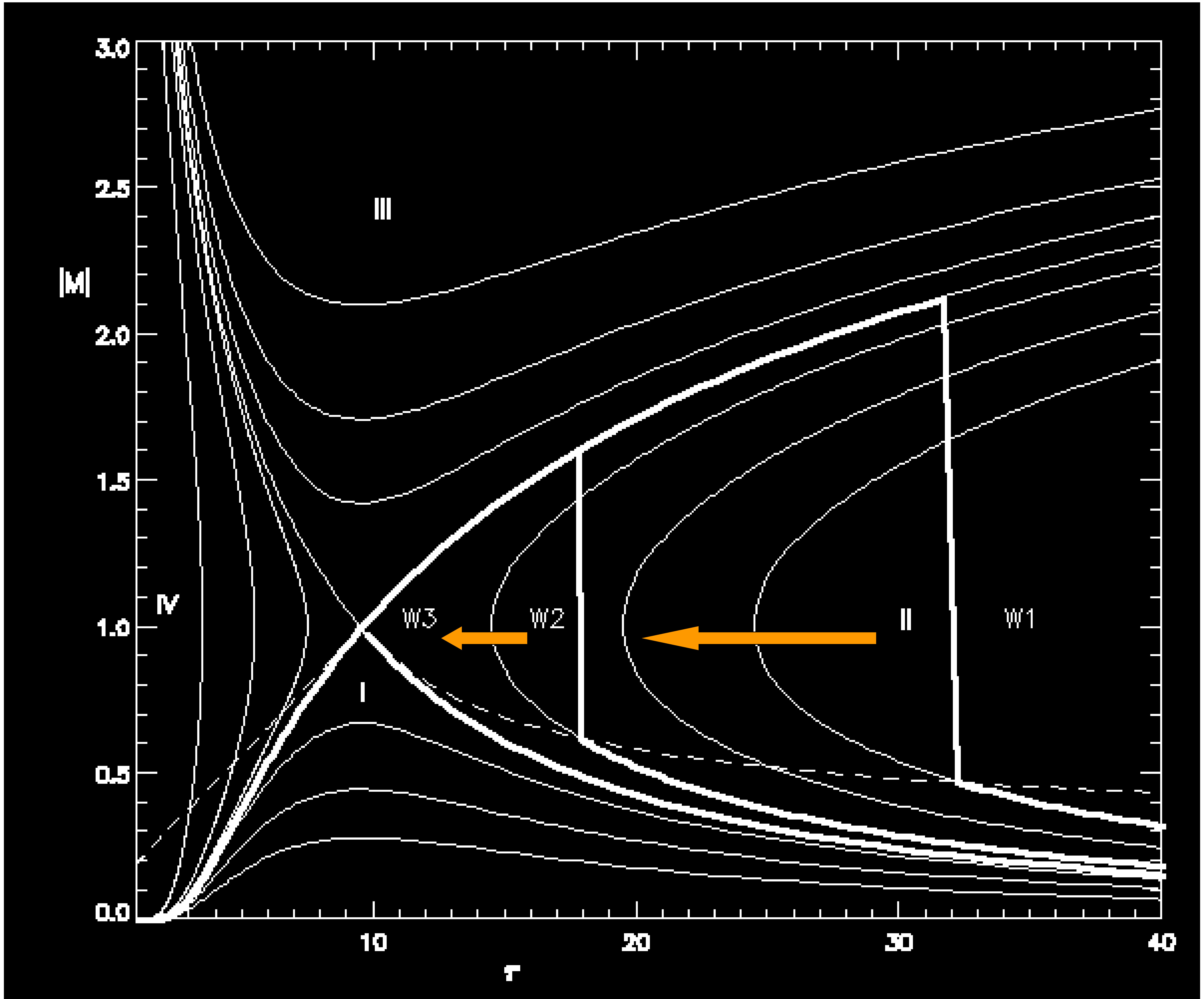
Shock position is determined by the pressure at infinity via the jump conditions.

$$\rho^+(M^+)^2 + \rho^+ = \rho^-(M^-)^2 + \rho^-,$$

$$\rho^- M^- = \rho^+ M^+ \longrightarrow M^- M^+ = 1$$

For given base values of the pressure, the position of the shock is uniquely determined by the pressure of the interstellar medium, and the distance from the critical point to the shock decreases as the pressure increases.

As p_∞ increases the shock moves in (obvious + algebra is simple).



SO for intermediate pressures at infinity

there are two solutions: a wind and a breeze.

$$p_{stat} \le p_\infty \le p_{crit}$$

Multiple solutions often mean INSTABILITY . Are breezes REALLY STABLE?

$$y^\pm = dU/c \pm dp/r c^2$$

$$y^\pm = y^\pm(r)\exp(-\, i(w + i g)t)$$

$$\left(M \pm 1\right) y^{\pm\prime} -\, i(w + i g) y^\pm + \frac{1}{2}(y^\pm + y^\mp)\frac{M'}{M}(M \mp 1) = 0$$

Look for solutions with vanishing pressure perturbations at R_0 and infinity

For waves in a flowing medium one defines the conserved WAVE ACTION (not energy: waves do work on flow)

$$S = \frac{(M+1)^2}{M}|y^+|^2 - \frac{(M-1)^2}{M}|y^-|^2$$

However instabilities may change the wave action (extract energy from the flow) so equation looks like this:

$$\left[\frac{(M+1)^2}{M}|y^+|^2 - \frac{(M-1)^2}{M}|y^-|^2\right]' + 2\frac{\gamma}{M}\left[(M+1)|y^+|^2 - (M-1)|y^-|^2\right] = 0$$

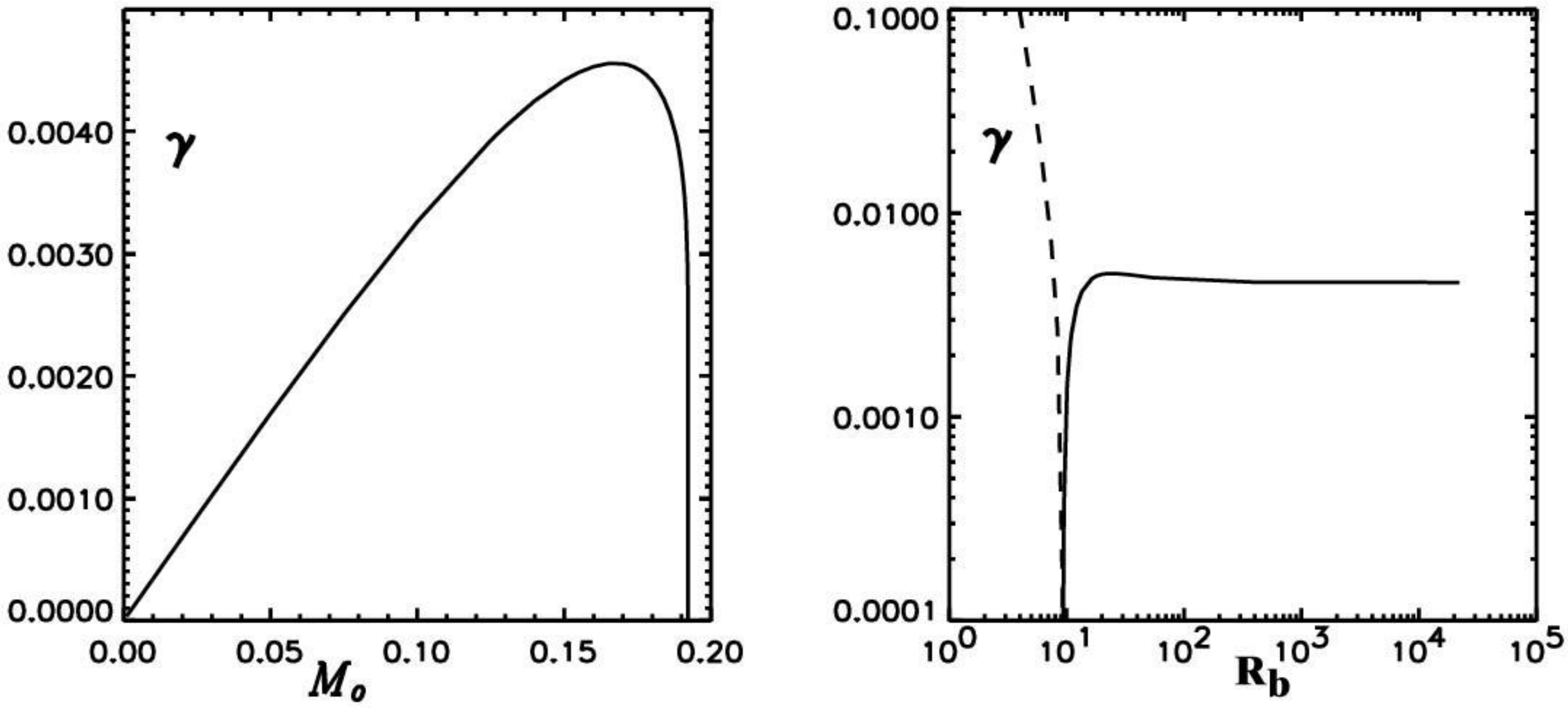
Integrating this equation between 1 and r and imposing the boundary condition that the pressure perturbation vanish (i.e. $y^+ = y^-$) both at the solar surface and at great distances, we find

$$\gamma = \frac{2\left(|y^+|_0^2 - |y^+|_r^2\right)}{\int_1^r dr\, M^{-1}\left[(M+1)|y^+|^2 - (M-1)|y^-|^2\right]}$$

But the asymptotics for breezes is obvious…..

$$y^+ \sim \frac{e^{\mp\gamma r}}{r}\left(1 \pm \frac{1}{2\gamma r}\right), \qquad y^- \sim \pm\frac{e^{\mp\gamma r}}{2\gamma r^2}$$

Boundary conditions are satisfied amplitudes tend to zero at great distances, and BREEZES ARE UNSTABLE Growth rate as a function of Base Mach Number



Why are breezes UNSTABLE? Wait a minute, let's look back at the asymptotic pressures ……

$$p_\infty = p_0 \exp\left(M_0^2/2 - g/c^2\right)$$

So pressure at infinity INCREASES with INCREASING BASE MACH NUMBER……

If you have a static atmosphere and increase pressure at infty, you would expect flow to GO IN, NOT OUT – Bondi, 1952

ON SPHERICALLY SYMMETRICAL ACCRETION

H. Bondi

(Received 1951 October 3)

Summary

The special accretion problem is investigated in which the motion is steady and spherically symmetrical, the gas being at rest at infinity. The pressure is taken to be proportional to a power of the density. It is found that the accretion rate is proportional to the square of the mass of the star and to the density of the gas at infinity, and varies inversely with the cube of the velocity of sound in the gas at infinity. The factor of proportionality is not determined by the steady-state equations, though it is confined within certain limits. Arguments are given suggesting that the case physically most likely to occur is that with the maximum rate of accretion.

Bondi Diagram

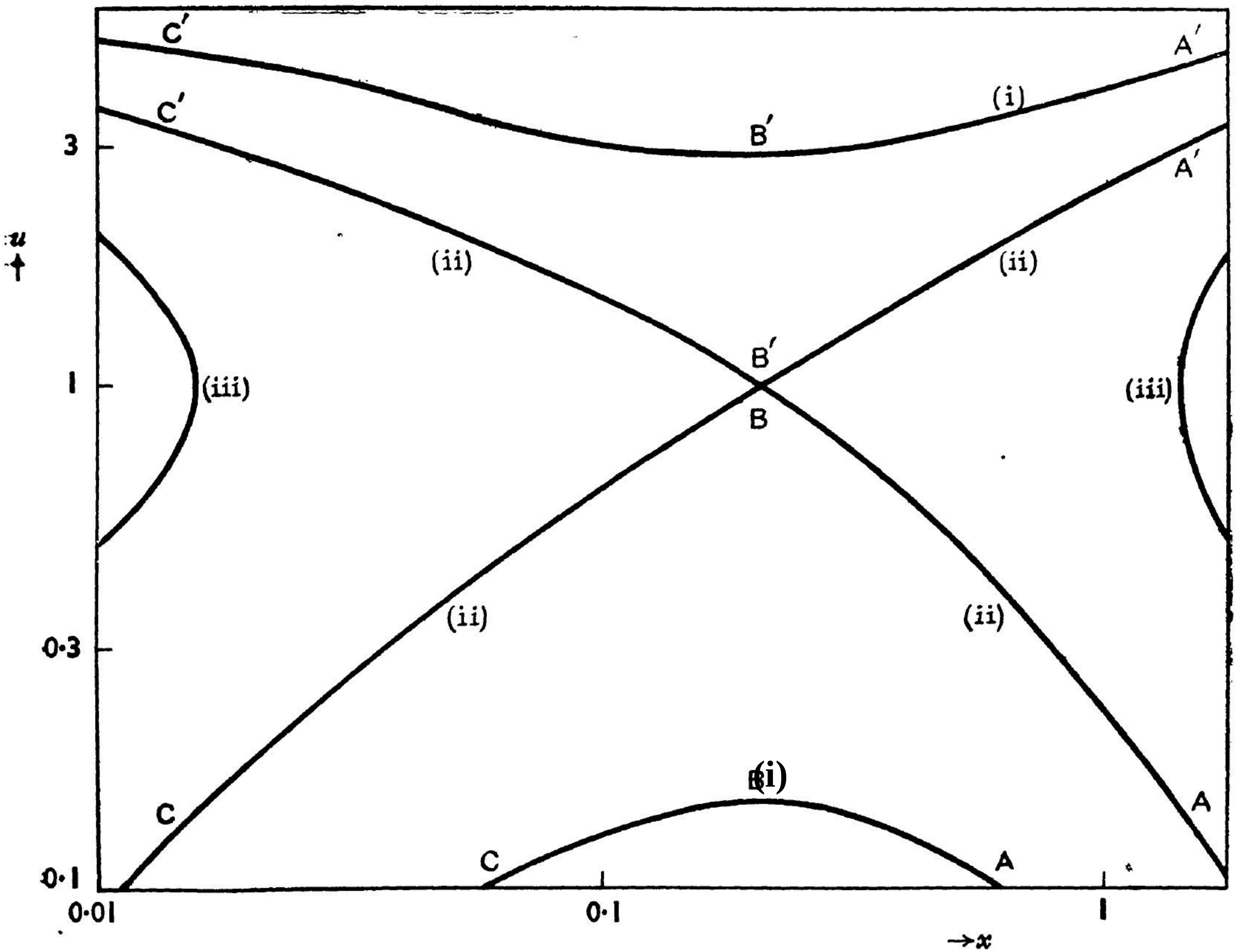


FIG. 2.—*u* as function of *x* for $\gamma = \frac{7}{5}$.
(i) $\lambda = \frac{1}{4}\lambda_c$;
(ii) $\lambda = \lambda_c$;
(iii) $\lambda = 4\lambda_c$.

SHOCK WAVES IN STEADY RADIAL MOTION UNDER GRAVITY*

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Received May 7, 1956

ABSTRACT

In the steady radial flow of a polytropic gas toward a center of gravitational attraction, it is shown that a standing shock wave can, in general, exist within a certain distance of the center. This possibility elucidates certain features of Bondi's investigation of such radial motion and, in particular, helps to resolve an indeterminacy which he had noted Reasons are given for concluding that the phenomenon may have application to accretion by a binary star.

I. INTRODUCTION

The steady spherically symmetric motion of a gas toward a center of gravitational attraction has been studied by Bondi (1952). The main purpose of the present work is to show that a standing spherical shock wave may occur in such motion. If it does, the motion on the supersonic side is given by a particular solution discovered by Bondi, while the motion on the subsonic side is given by one of a set of solutions which he found but which had appeared to be without physical significance. In this and other ways the work assists in the interpretation of Bondi's investigation.

VIII. NUMERICAL ILLUSTRATION

In order to illustrate the hydrodynamical theory for a value of γ in the range $1 < \gamma < \frac{5}{3}$, it is convenient to use $\gamma = \frac{7}{5}$. This value was also used by Bondi, and Figure 1 reproduces some features of Bondi's Figure 2, though the present calculations have been done afresh.

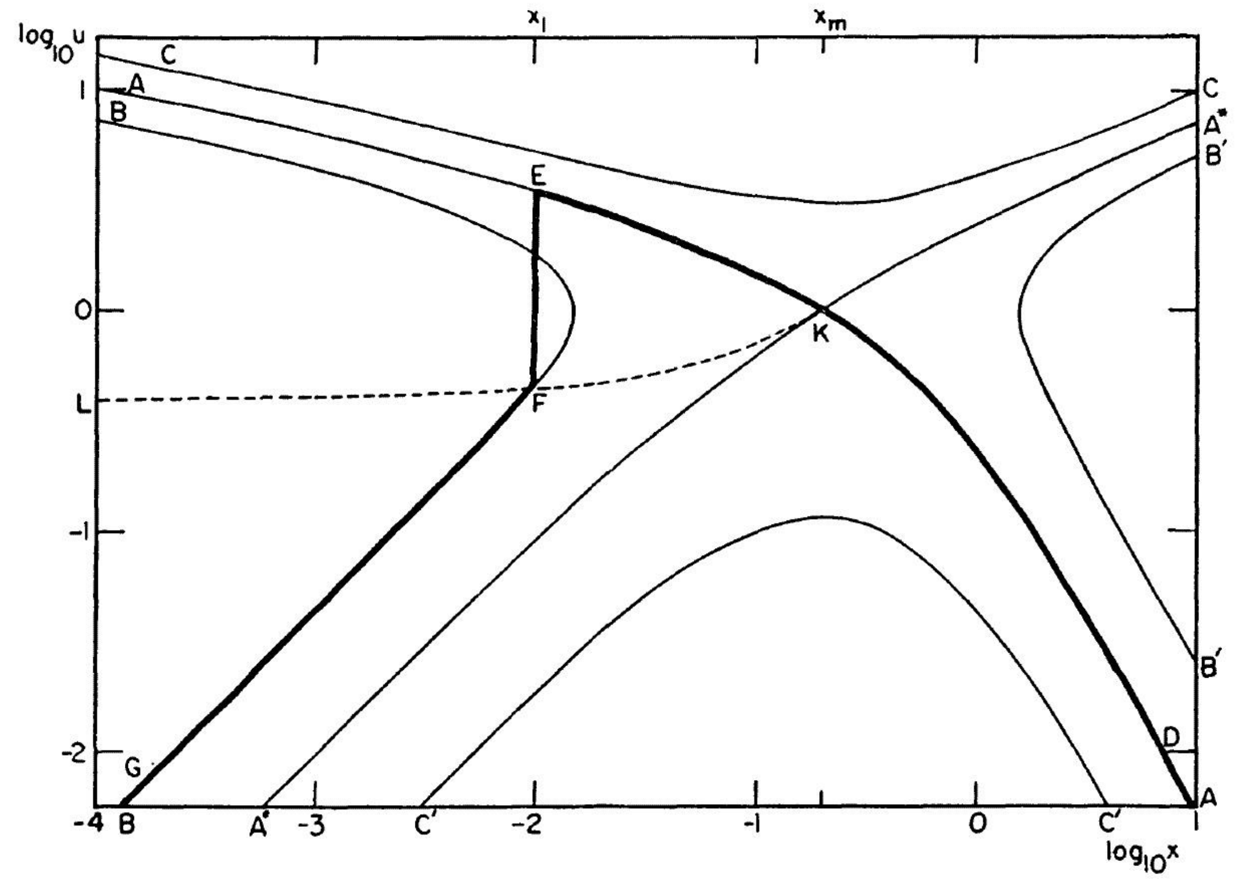
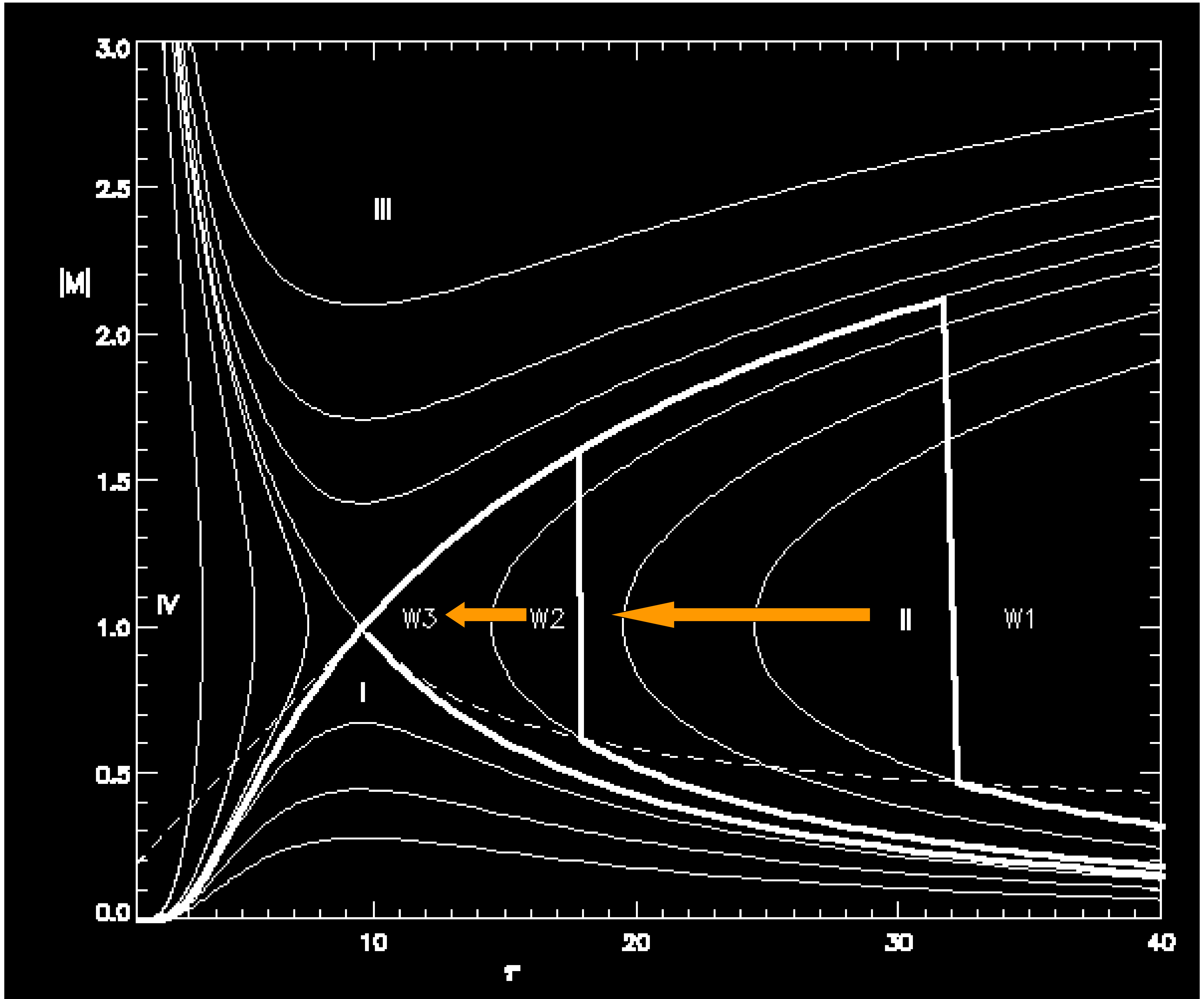


Fig. 1.—Example of motion with shock wave, $\gamma = \frac{7}{5}$. *AA*, *A*A**, solution of equation (8 1) for $\kappa = \frac{5}{8}$; *BB*, *B′B′*, solution for $\kappa \doteqdot 2.77$; *DEFG*, motion with shock *EF; LFK*, values of u_2 corresponding to u_1 given by *AEK;* and *CC*, *C′C′*, solution for $\kappa = \frac{1}{8}$. Abscissa $\log_{10} x$; ordinate $\log_{10} u$.

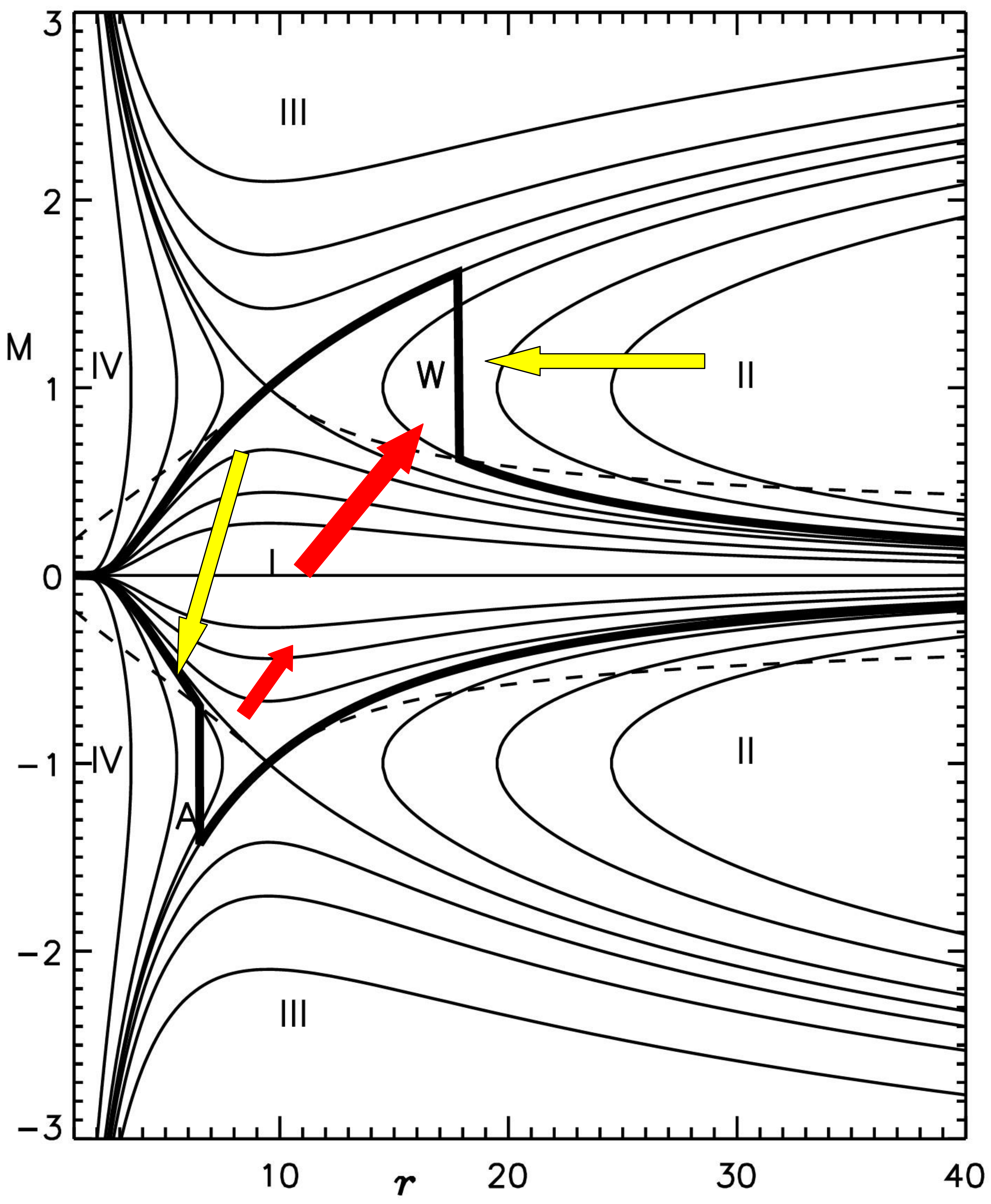
As p_∞ increases above p_{crit} What HAPPENS ??? Can't go to BREEZES ($p_\infty < p_{crit}$ and they're unstable ANYWAY)



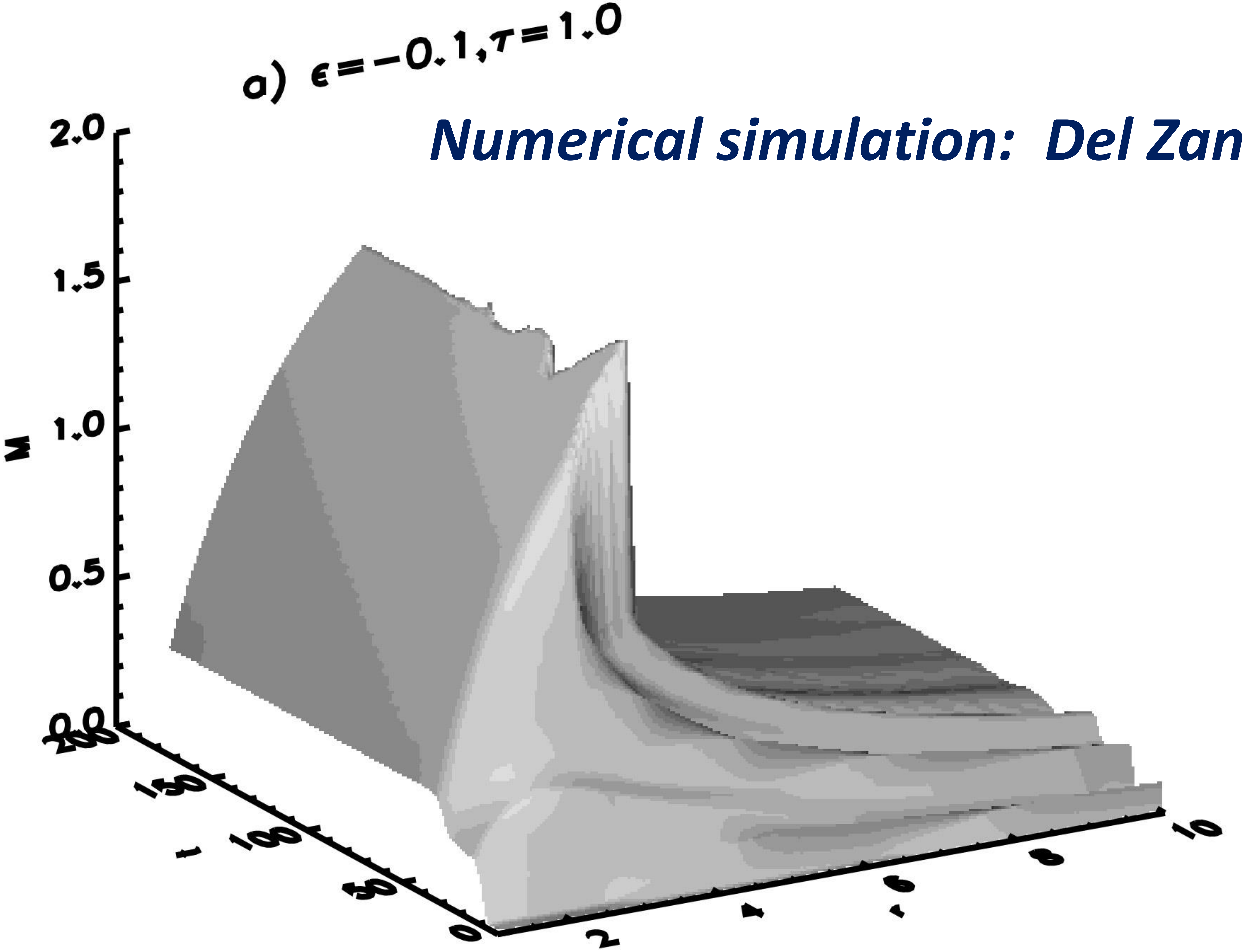
Parker to Bondi And back. Hysteresis cycle (Velli, 1994)

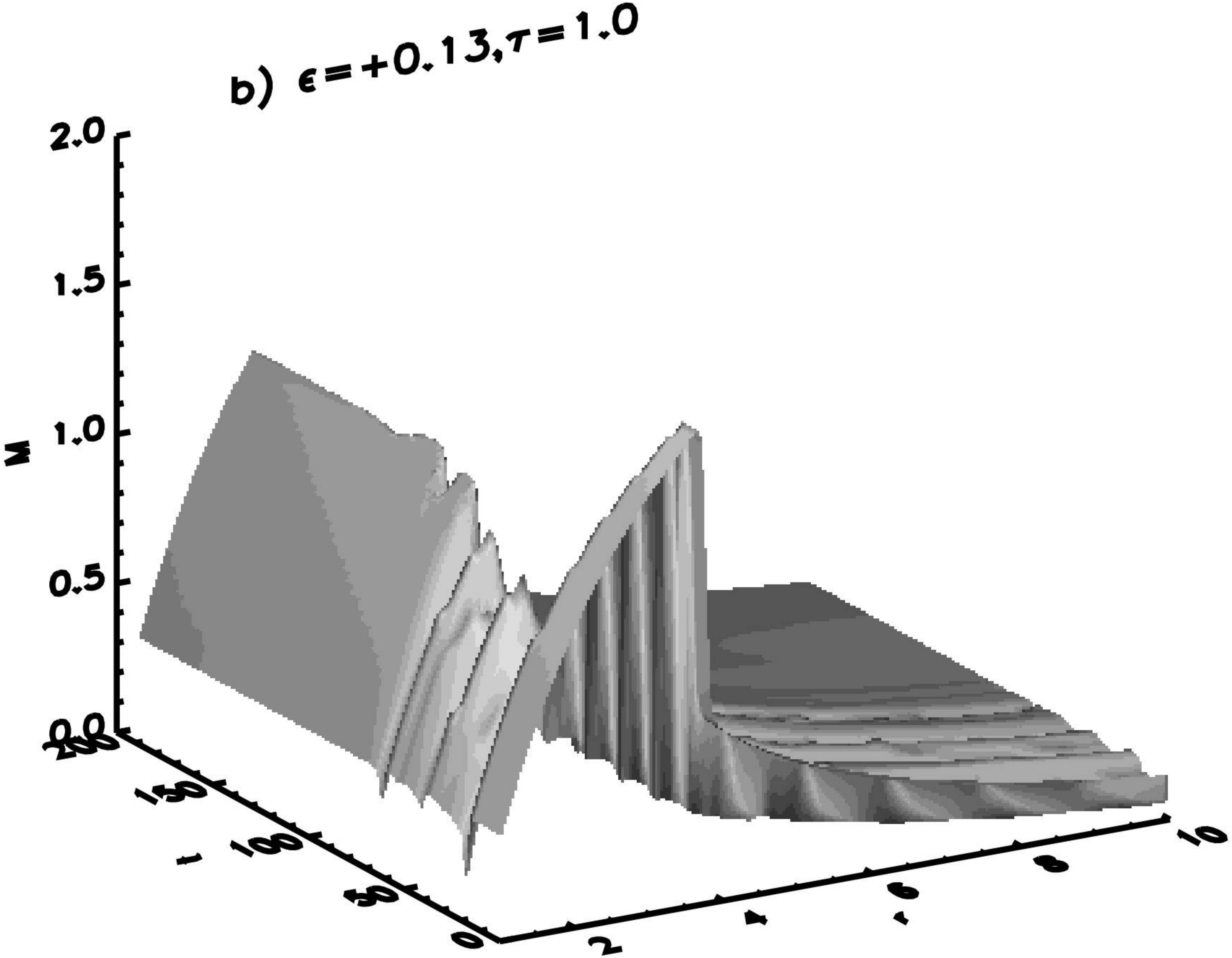
Solves inconsistencies in numerical simulations

Galactic fountains
Supergiant and stellar winds

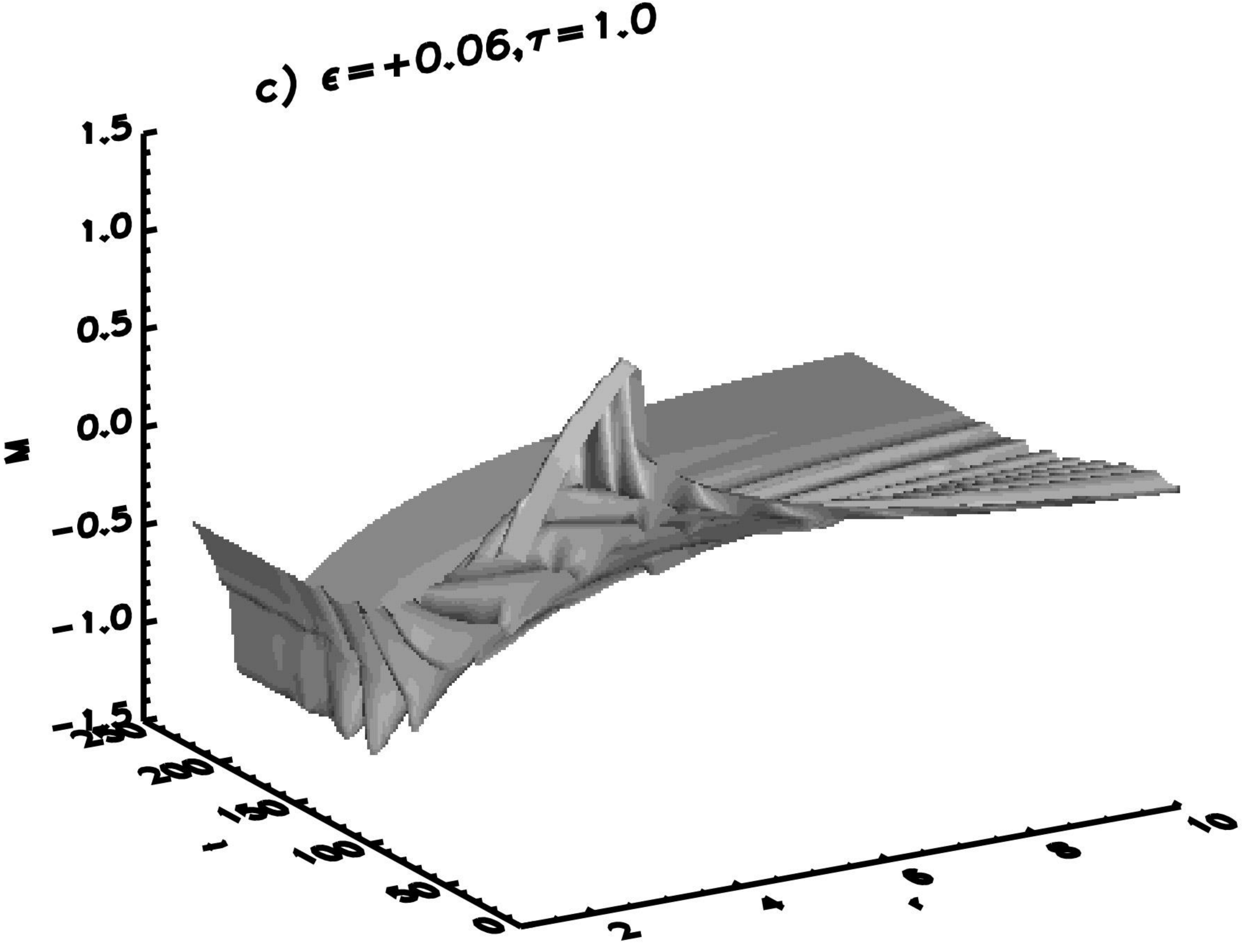


Numerical simulation: Del Zanna et al. 1998

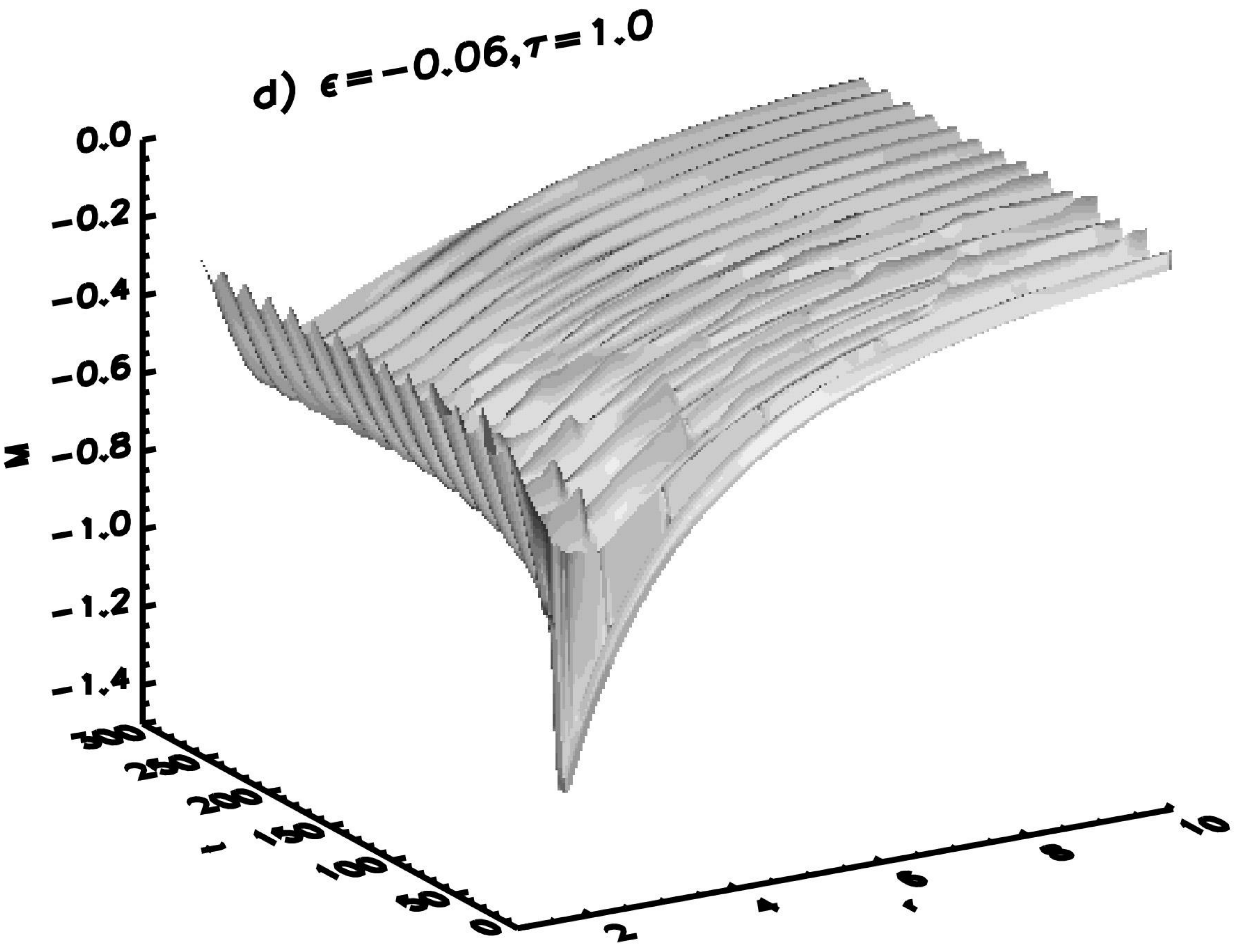


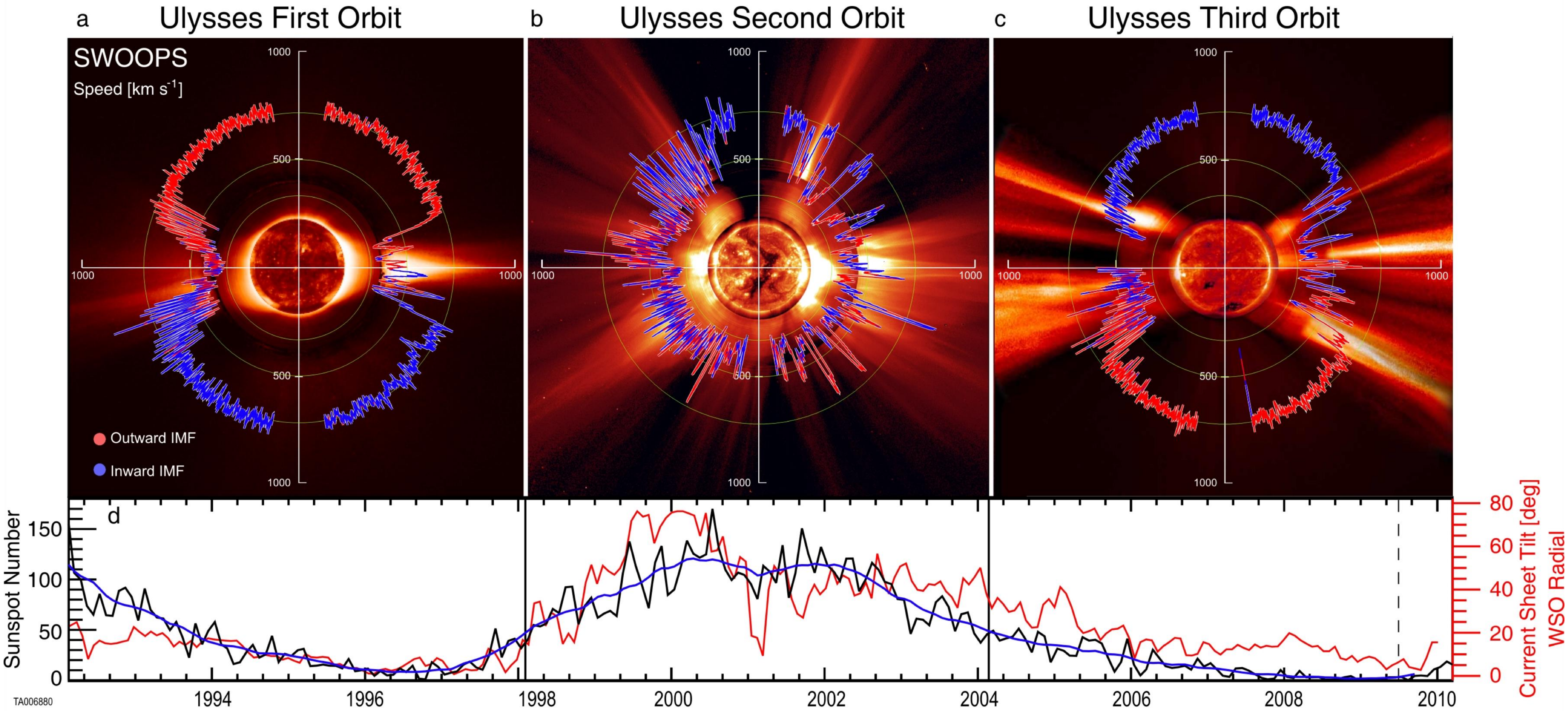


b) ε=+0.13,τ=1.0
2.0
1.5
1.0
0.5
0.0
M
200
150
100
50
0
2
4
6
8
10

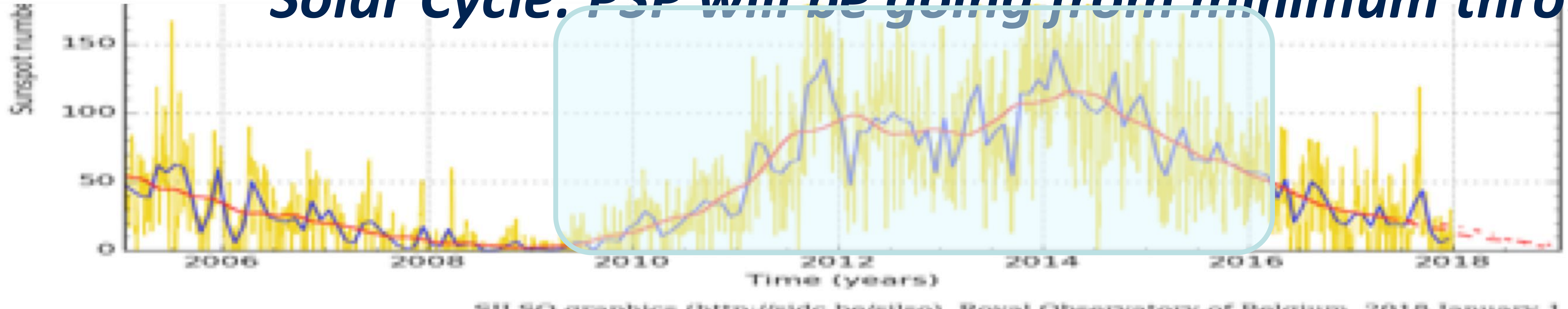


c) ϵ=+0.06,τ=1.0
1.5
1.0
0.5
0.0
−0.5
−1.0
−1.5
M
250
200
150
100
50
0
t
2
4
6
8
10
r

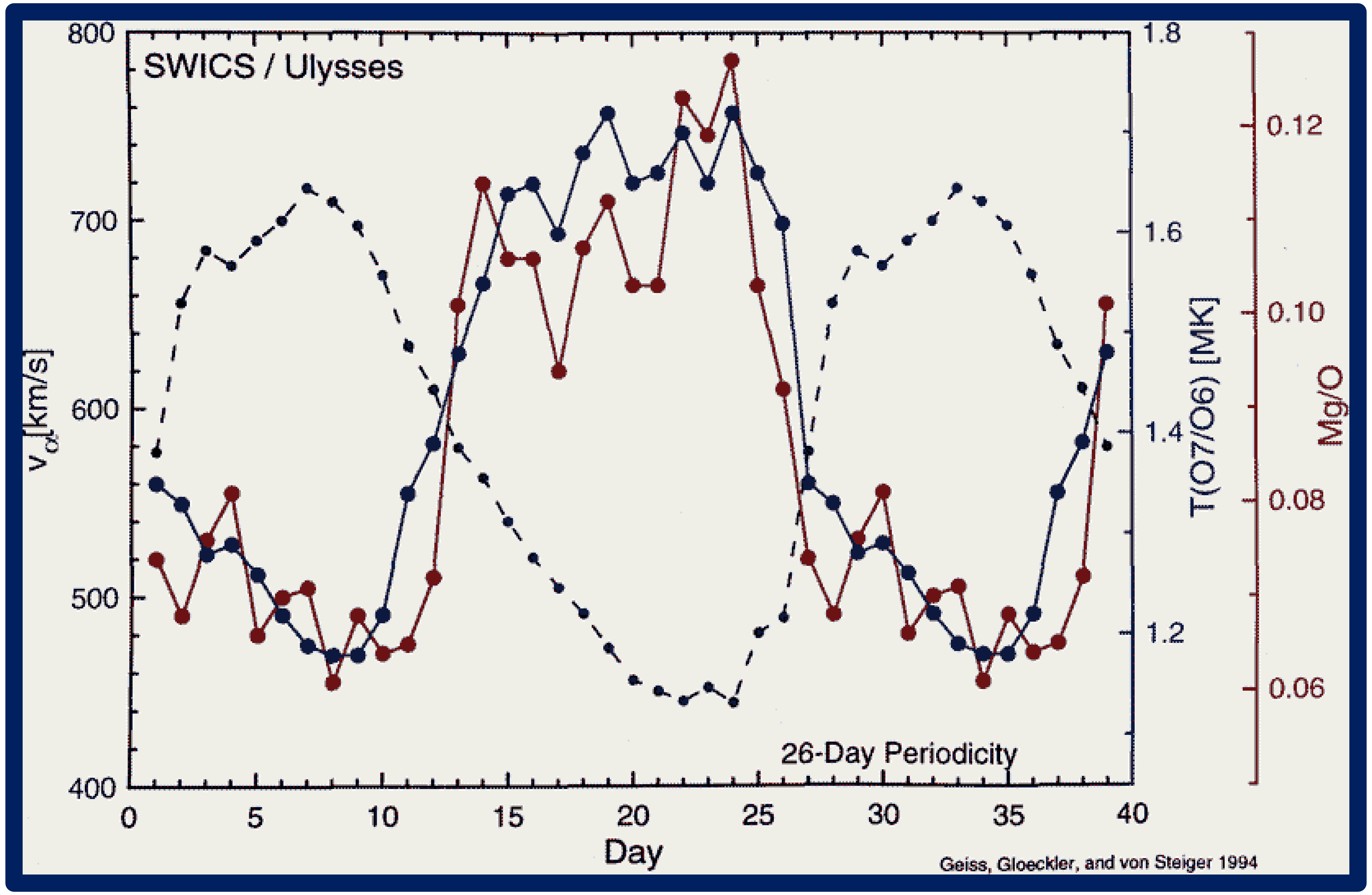

d) ϵ=−0.06,τ=1.0
0.0
−0.2
−0.4
−0.6
−0.8
−1.0
−1.2
−1.4
M
300
250
200
150
100
50
0
t
2
4
6
8
10
r

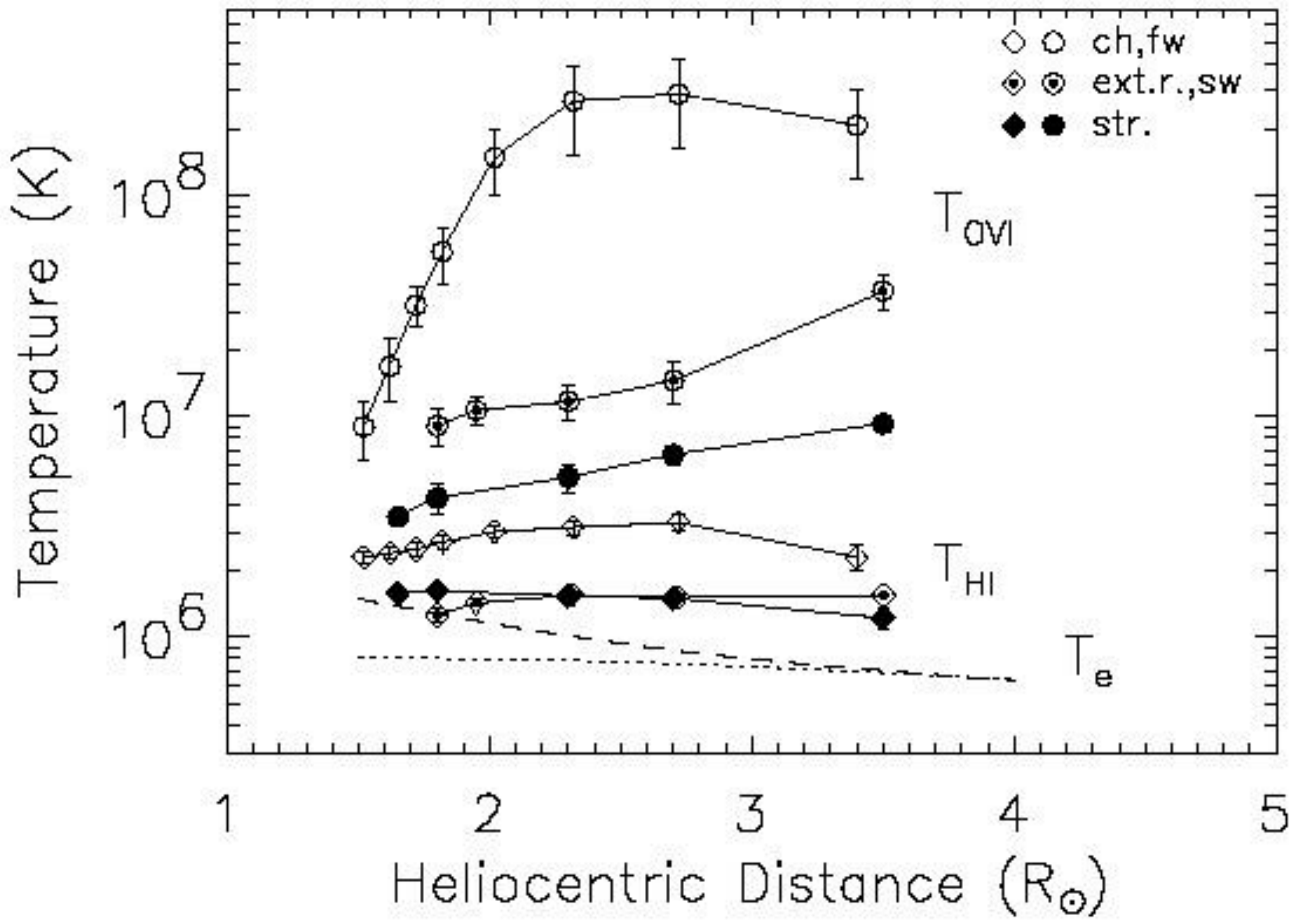


Solar Cycle: PSP will be going from minimum through ascending



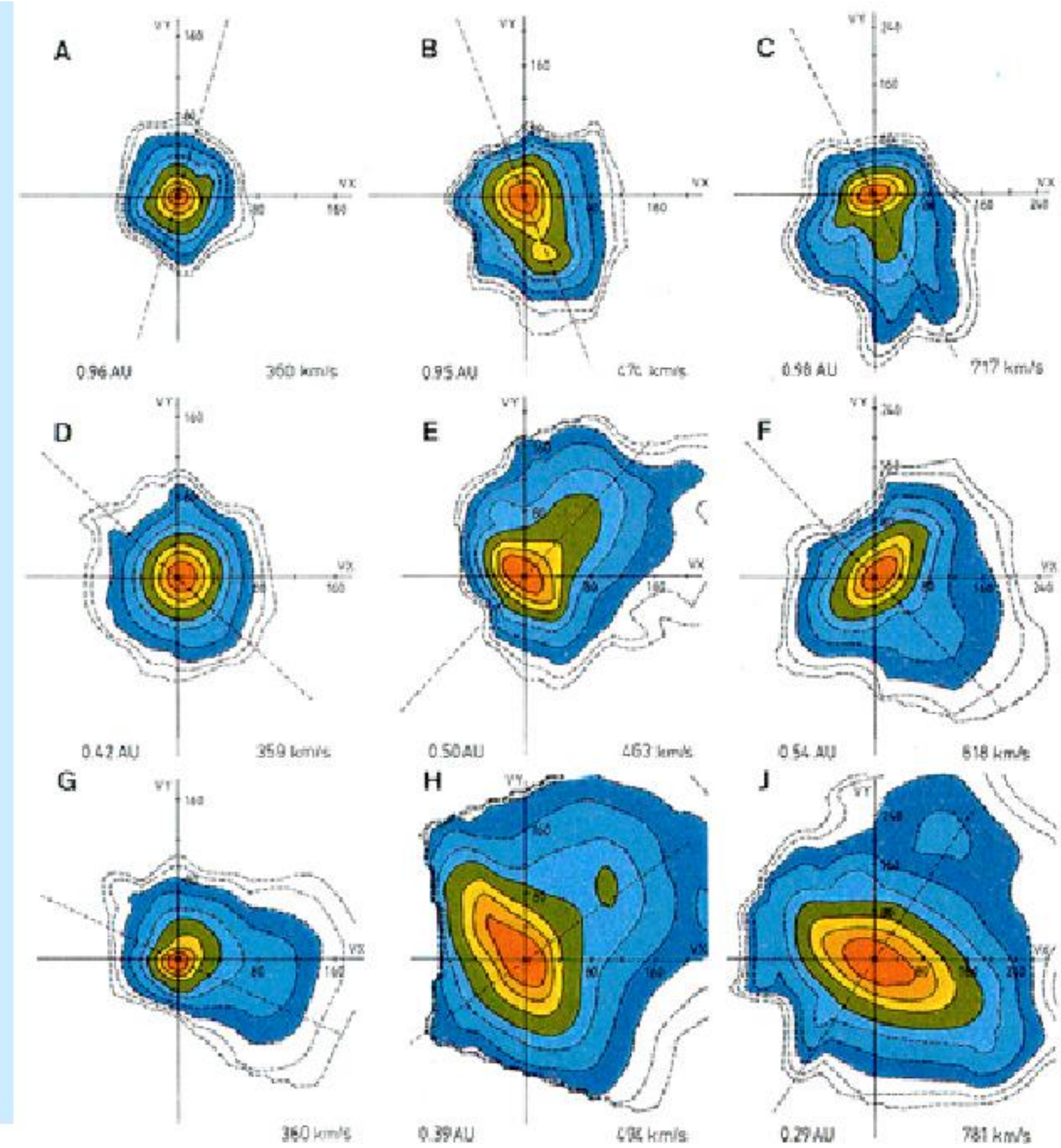
Given the corona, do we understand the wind? Not quite…. Fast Wind is 1) Too FAST 2) Temperature and speed OPPOSITE TO EXPECTED!!!!!





	fast	slow
speed (km/s)	600–800	300–500
T_p (10^5 K)	2.4	0.4
T_e (10^5 K)	1.0	1.3
T_{ion} / T_p	> m_{ion}/m_p	< m_{ion}/m_p
O^{7+}/O^{6+},Mg/O	low	high

Proton solar wind distribution functions Marsch et al., JGR, 87, 52, 1982 (Helios data)



To be continued…..

2. Solar Wind Origins and Acceleration and Solar and Stellar Winds and Magnetic Activity